

FUNCTIONAL SKILLS CERTIFICATE Functional Mathematics

Level 2

Mark Scheme

4368

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Version: 1.0 Final

Mark schemes are prepared by the Lead Assessment Writer and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation events which all associates participate in and is the scheme which was used by them in this examination. The standardisation process ensures that the mark scheme covers the students' responses to questions and that every associate understands and applies it in the same correct way. As preparation for standardisation each associate analyses a number of students' scripts. Alternative answers not already covered by the mark scheme are discussed and legislated for. If, after the standardisation process, associates encounter unusual answers which have not been raised they are required to refer these to the Lead Assessment Writer.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of students' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

Further copies of this mark scheme are available from aga.org.uk

Glossary for Mark Schemes

Examinations are marked to award positive achievement.

Marks are awarded for demonstrating the following interrelated **process skills**.

Representing Selecting the mathematics and information to model a situation.

- **R.1** Candidates recognise that a situation has aspects that can be represented using mathematics.
- **R.2** Candidates make an initial model of a situation using suitable forms of representation.
- **R.3** Candidates decide on the methods, operations and tools, including ICT, to use in a situation.
- **R.4** Candidates select the mathematical information to use.

Analysing Processing and using mathematics.

- **A.1** Candidates use appropriate mathematical procedures.
- **A.2** Candidates examine patterns and relationships.
- **A.3** Candidates change values and assumptions or adjust relationships to see the effects on answers in models.
- **A.4** Candidates find results and solutions.

Interpreting Interpreting and communicating the results of the analysis.

- **I.1** Candidates interpret results and solutions.
- **I.2** Candidates draw conclusions in light of situations.
- **1.3** Candidates consider the appropriateness and accuracy of results and conclusions.
- **I.4** Candidates choose appropriate language and forms of presentation to communicate results and solutions.

In particular, individual marks are mapped onto the following skills standards.

Representing Making sense of the situations and representing them.

A learner can:

Ra Understand routine and non-routine problems in familiar and unfamiliar contexts and situations.

Rb Identify the situation or problems and identify the mathematical methods needed to solve them.

Rc Choose from a range of mathematics to find solutions.

Analysing Processing and using the mathematics.

A learner can:

Aa Apply a range of mathematics to find solutions.

Ab Use appropriate checking procedures and evaluate their effectiveness at each stage.

Interpreting Interpreting and communicating the results of the analysis. A learner can:

Interpret and communicate solutions to multistage practical problems in familiar and unfamiliar contexts and situations.

Ib Draw conclusions and provide mathematical justifications.

To facilitate marking, the following categories are used:

M Method marks are awarded for a correct method which could lead to a correct answer.

A Accuracy marks are awarded when following on from a correct method. It is not necessary to always see the method. This can be implied.

B Marks awarded independent of method.

ft Follow through marks. Marks awarded following a mistake in an earlier step.

Special case. Marks awarded within the scheme for a common misinterpretation which has some mathematical worth.

oe Or equivalent. Accept answers that are equivalent.

eg, accept 0.5 as well as $\frac{1}{2}$

Q	Ans	wer	Mark	Comments
	their 270 ÷ 0.5 or their 270 × 2 or 540	or their 24 ÷ 0.3 or 80	M1 Ra	
	540 or 620		A1 Rc	
1 (a)	200 + 15 × 2 or 230		M1 <i>Aa</i>	
	100 + 100 + 100 +	- their 230	M1 <i>Aa</i>	Allow one error but must include 4 exits only - not the 1250 mm exit
	530		A1 Rc	
	Clearly identifies t 540 or 620 and the		A1ft <i>Ib</i>	ft from 1 st and 3 rd M marks

1 (b)	600 – 3 × 80 or 600 – 240 or 360	M1	
		Ra	

Q	Answer their $360 \div (5 + 4) \times 5$ or 40×5	Mark	Comments		
	or 200	Rc			
	or				
	their 360 ÷ (5 + 4) × 4 or 40 × 4 or 160				
		A1	Must see £ symbol and names		
	Liz \rightarrow £200 and Omar \rightarrow £160	la	SC2 Liz \rightarrow £333.33 and Omar \rightarrow £267.67		
			SC1 333.33 and 267.67		
	their 200 ÷ 5 = 40	B1ft			
	and their 160 ÷ 4 = 40	Ab			
	or				
Check	their 200 ÷ 40 = 5 and their 160 ÷ 40 = 4				
	or				
	200 : 160 = 5 × 40 : 4 × 40				
	Additional Guidance				
	To award the mark for the check mus	st show a cl	ear understanding of ratio		

	Alternative method 1		
1 (c)	70 ÷ 40 or 1.75 or 1 hour 45 minutes	M1 <i>Ra</i>	

Q	Answer their 1 hour 45 minutes + 50 minutes	Mark	Com	ments
	or 2 hours 35 minutes	Aa	5.30 + their 1 hour 48	5 minutes or 7.15
	5.30 + their 2 hours 35 minutes	M1 <i>Rc</i>	their 7.15 + 50 minutes	8.00 – 50 minutes
	8.05 and No or 7.15 and 7.10 and No	A2 Ib	A1 8.05 or 7.15 an or A1ft correct decisior (only if M3 scored)	
	Alternative method 2			
	70 ÷ 40 or 1.75 or 1 hour 45 minutes	M1 <i>Ra</i>		
	their 1 hour 45 minutes + 50 minutes or 2 hours 35 minutes	M1 Aa	8.00 – 50 minutes or	7.10
	8.00 – their 2 hour 35 minutes	M1 Rc	their 7.10 – their 1 hour 45 minutes	5.30 + their 1 hour 45 minutes
	5.25 and No or 7.15 and 7.10 and No	A2 Ib	A1 5.25 or 7.15 an or A1ft correct decisior (only if M3 scored)	

	Alternative method 3	Alternative method 3				
1(c)	70 ÷ 40 or 1.75 or 1 hour 45 minutes	M1 Ra				
	their 1 hour 45 minutes + 50 minutes	M1				

Q	or 2 hours 35 Amswer	Mark	Comments
	8.00 – 5.30 or 2 hours 30 minutes	M1 Rc	
	2 hours 35 minutes and 2 hours 30 minutes and No	A2 Ib	A1 2 hours 35 minutes and 2 hours 30 minutes or A1ft correct decision for their values (only if M3 scored)

Additional Guidance

Other alternatives

There are other alternative mark schemes, e.g. showing that the actual speed to arrive on time > 40 mph

Arrival time 7.10

Journey time 1 hour 40 minutes (1.66 ... hours)

Required speed 70 ÷ 1.66 ... = 42 mph

Decimal times

Students who convert between a time as a decimal to hours and minutes incorrectly (or vice versa) can score method marks only.

e.g. their 1.75 hours = 2 hours 15 minutes from 1.75 hours \rightarrow 1 hour 75 minutes

e.g 1.75 hours + 50 minutes = 2 hours 25 minutes from 1.75 + 0.50 \rightarrow 2.25

Q	Answer	Mark	Comments
2 (a)	560	B1 Aa	

	Alternative method 1				
	$300 \div 750 \text{ or } \frac{2}{5} \text{ or } 0.4$	M1 Ra	or 750 ÷300 or 2.5		
	their $\frac{2}{5} \times 60$ or their 0.4×60	M1 Rc	or 60 ÷ 2.5		
0 (h)	24	A1 Aa			
2 (b)	Alternative method 2				
	750 ÷ 60 or 12.5	M1 Ra	calories per minute		
	300 ÷ their 12.5	M1 <i>Rc</i>			
	24	A1 <i>Aa</i>			
	reverse or alt method	B1ft			
	e.g.	Ab			
	24 ÷ 60 × 750 = 300 or				
Check	300 ÷ 24 × 60 = 750				
	or				
	24 × 12.5 = 300				
	and 60 × 12.5 = 750				
	Additional Guidance				
	Misread				
	Award a maximum of M2 for any other	n table used instead of 750, eg			
2 (b)	840 ÷ 60 = 14		M1		
	300 ÷ 14		M1		
	21.4			A0	
	Award marks for main question if working/answer seen in Check				

Q	Answer	Mark			Com	ments		
	works out correct calories for given	B1		any ti	me for any macl	nine		
	time for one machine	Aa		level	can be omitted			
	attempts to work out calories for each	D4		implie	ed from calories			
	of three or four different machines compatible with specified level and time	B1 <i>Aa</i>		must	be at level 1	stair climber which		
	ume				use a correct me crical slips	ethod but allow		
	between 5 and 20 minutes on all machines chosen	B1 la la		must	be at least 3 ma	chines		
	their total calories for all machines	B1ft			rect method for o	•		
	chosen between 850 and 1000	la la			not need to be g be at least 3 ma			
	total time 60 minutes	B1 Aa			not need to be g	iven		
	fully correct plan clearly communicated using all four machines	B2 la la		B1	two errors/omis	our machines with up to sions		
	Additional Guidance							
2 (c)	Treadmill	Level 2	1	5 min	225 calories			
	Bike	Level 2	20	0 min	280 calories			
	Stair climber	Level 1	10	0 min	160 calories			
	Rower	Level 2	1	5 min	262.5 calories			
	Totals		60	0 min	927.5 calories			
	For fully correct plan (for B2) must see							
	Use of at least one of each mach	nine						
	all times between 5 minutes and			•	,			
	levels for each machine with Lev							
	all times totalling 60 minutes (total			_	•			
	correct total caloring between %5				•	nn)		
		correct total calories between 850 and 1000 (total need not be given)						
	•	Examples of errors and omissions						
	•	number of calories incompatible with level and/or time one Level missing or Stair climber used at Level 2						
	total time not 60 minutes							
	total calories out of given range							
	Wrong method for calculating calories	(all mach	nine	es) car	n score B0B0B1I	30B1B0 max		
	Not giving levels (all machines) can score B1B0B1B1B0 max							
	Not giving levels or times can score 1st	B1 only						
	Using stair climber at Level 2 can score B1B1B1B1B1B1							

Q	Answer	Mark	Comments	
2 (d)	30 × 2.5 or 30 + 30 + 15 or 75 180 ÷ 4 or 45 their 75 + their 45 + 112 or	M1 Ra M1 Rb		
	250 – their 75 – their 45 – 112 75 + 45 + 112 = 232 or 250 – 75 – 45 – 112 = 18	Aa A1 Ib Additional (can be implied from correct totals Guidance	
	Award 4 marks if 232 seen with no working			

Q	Answer	Mark	Comments			
	any one of patio, vegetable patch, lawn, path or flower bed shown with correct size but not necessarily in correct position	B1 Ra	Labels not necessary Patio → 10 cm by 3 cm Vegetable patch → 10 cm by 1 cm			
	any two of patio, vegetable patch, lawn, path or flower bed shown with correct sizes but not necessarily in correct position	Lawn \rightarrow 10 cm by 8 cm Path \rightarrow 10 cm by 1 cm Lawn \rightarrow circle radius 2 cm				
	patio, vegetable patch, lawn and path shown with correct sizes and positions	B1 <i>Aa</i>				
3 (a)	circular flower bed shown within or at edge of lawn – can be any radius	B1 <i>Aa</i>				
	patio, vegetable patch, lawn, path and circular flower bed with correct sizes, in correct position and labelled correctly	B1 <i>la</i>				
	Additional Guidance					
	Allow freehand attempt at circle for 4 th B1 but not 5 th B1 Diagram with front and back reversed can score B1B1B0B1B1 Allow 'horizontal vegetable patch' with ends touching fence					

3 (b)	Alternative method 1
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Q	Ans	wer	Mark	Comments
	15 × 4.5 or 67.5	5	Ra	
	their 67.5 ÷ 7.4 o or their 67.5 ÷ 8.6 o	•	M1 <i>Rb</i>	
	their 10 × 128.50 c or their 8 ×139.75 or		M1 la	their 10 must be from their [9.1, 9.122] their 8 must be from their [7.8, 7.85] both must be rounded up to an integer
	their 1285 – their 1	118	M1 Aa	or 1285 – 175 or 1118 + 175
	167 and No or 1110 and 1118 and or 1293 and 1285 and		A2 Ib Ib	A1 167 or 1110 and 1293 or A1ft correct decision for their values (only if 1 st and 4 th M marks scored)
	Alternative metho	od 2		
	15 × 4.5 or 67.5	5	M1 Ra	
	their 67.5 ÷ 7.4 or or their 67.5 ÷ 8.6 or	-	M1 Rb	or 10 × 7.4 or 8 × 8.6
	their 10 × 128.50 – 175 or 1110	their 10 × 128.50 – 175 or 1110	M1 la	their 10 must be from their [9.1, 9.122] their 8 must be from their [7.8, 7.85] both must be rounded up to an integer
	their 1110 ÷ 8	their 1110 ÷ 139.75	M1 <i>Aa</i>	
	138(.75) or 139 and No	7.9(4) and No	A2 Ib Ib	A1 138(.75) or 139 or 7.9(4) A1ft correct conclusion for their values (only if 1 st and 4 th M marks scored)

	Additional Guidance	
3(b)	Example (common error)	
	15 × 4.5 = 67.5	M1

Q	8.6 ² = 73.96 — Answeand 7.42 = 54.76 — Mablexes Comments	M0
	1 × 139.75 = 139.75 and 2 × 128.50 = 257	M0
	257 – 139.75 = 117.25	M1
	No	A1ft
	Example (another common error)	
	15 + 4.5 = 19.5	MO
	19.5 ÷ 8.6 = 2.23 and 19.5 ÷ 7.4 = 2.64	M1
	3 × 139.75 = 419.25 and 3 × 128.50 = 385.50	M1
	419.25 – 385.50 = 33.75	M1
	No	A1ft
	Failing to round up the number of boxes can score M1M1M0M1A1ft	1

	50 (cm)		B1 <i>Aa</i>	
	246 300 × their 50	or 12 315 000	M1 <i>Rb</i>	allow digits 12315
	their 12 315 000 ÷ 1000 or 12 315	their 12 315 000 ÷ 800 or 15 393.75	M1 <i>Rc</i>	or 800 × 1000 or 800 000
3 (c)	their 12 315 ÷ 800 or 15.3(9) or 15.4	their 15 393.7 ÷ 1000 or 15.3(9) or 15.4	M1 <i>Aa</i>	or their 12 315 000 ÷ 800 000 or 15.3(9) or 15.4
	16		A1 <i>Ib</i>	
	Additional Guidance			
	Multiplying by their	50 can be done at a	ny stage ii	n the calculation

4 (a)	2 × 1 (+) 3 × 4 (+) 4 × 9 (+) 5 × 12 (+) 6 × 12 (+) 7 × 15 (+) 8 × 33 (+) 9 × 698 (+) 10 × 512 or 2 (+) 12 (+) 36 (+) 60 (+) 72 (+) 105 (+) 264 (+) 6282 (+) 5120	M1 Ra	at least 4 correct
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Q	Answer 2 × 1 + 3 × 4 + 4 × 9 + 5 × 12 + 6 × 12	Mark	Comments
	+ 7 × 15 + 8 × 33 + 9 × 698 + 10 × 512		
	or	M1	
	2 + 12 + 36 + 60 + 72 + 105 + 264 + 6282 + 5120	Ra	allow two errors
	or		
	11 953		
	their 11 953 ÷ 1296 or [9.2, 9.23]	M1	
		Rc	
		A1ft	ft their [9.2, 9.23]
	[92, 92.3]	Aa	can be implied from plotted point
	their [92, 92.3] plotted for July ± ½	B1ft	SC2 correct value plotted with no or
	small square	Aa	incomplete working

4 (b)	Full description e.g. rating increases by about their 11% rating increases (from 81%) to their 92%	B2ft Ib Ib	B1 Part description e.g. rating increases ft their 4(a)		
	Additional Guidance				
	Mark from answer in 4(a) working space Mark positively if answer in 4(a) working Award B1 for 'rating increases' oe withou	space is	incompatible with graph		

Q	Answer	Mark	Comments
	Alternative method 1		
4 (c)	678 + 411 or 1089 or 12 + 18 + 56 + 54 or 140	M1 Ra	happy and unhappy customers
	their 1089 ÷ 1296 (× 100) or 0.84 or 84.0 or their 140 ÷ 1296 (× 100) or [0.108, 0.109] or [10.8, 10.9]	M1 Aa	
	73.2 or 73 and No or 0.732 or 0.73 and 0.75 and No	A2 Ib	A1 73.2 or 73 or 0.732 or 0.73 and 0.75 or A1ft correct conclusion for their values (only if M2 scored)
	Alternative method 2		
	1296 ÷ 100 × 75 or 972	M1 Aa	
	(678 + 411) – (12 + 18 + 56 + 54) or 1089 – 140 or 949	M1 Ra	
	972 and 949 and No	A2 Ib	A1 972 and 949 or A1ft correct conclusion for their values (only if M2 scored)

4(c)	Alternative method 3	
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Q	678 + 411 or 1089	Mark	Comments
	or 12 + 18 + 56 + 54 or 140	M1 Ra	happy and unhappy customers
	(their 1089 – their 140) ÷ 1296 (× 100) or 949 ÷ 1296 (× 100) or 0.732 or 0.73	M1 <i>Ra</i>	
	73.2 or 73 and No or 0.732 or 0.73 and 0.75 and No	A2 Ib	A1 73.2 or 73 or 0.732 or 0.73 and 0.75 or A1ft correct conclusion for their values (only if M2 scored)

	Additional Guidance	
	Example (common error - rounding 10.8% down to 10)	
4(c)	1089 and 140	M1
.(0)	0.84 = 84% and 0.108 = 10%	M1
	74% and No	A1ft
	Any answer that does not include the conversion to or from a % → M1 max	1

	Alternative method 1		
4 (d)	55 ÷ 100 × 1128 or 620(.4)	M1 <i>Ra</i>	

Q	Answer	Mark A1	Comments
	620(.4) and No	lb	
	Alternative method 2	1	
	615 ÷ 1128 (× 100)	M1	
		Ra	
	54(.5) and No	A1	
	54(.5) and NO	lb	
	Alternative method 3		
	615 ÷ (55 ÷ 100) or 1118	M1	
		Ra	
	1118 and No	A1	
		lb	