

UNIVERSITY OF CAMBRIDGE INTERNATIONAL EXAMINATIONS
GCE Ordinary Level

MARK SCHEME for the May/June 2012 question paper
for the guidance of teachers

4037 ADDITIONAL MATHEMATICS

4037/11

Paper 1, maximum raw mark 80

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes must be read in conjunction with the question papers and the report on the examination.

- Cambridge will not enter into discussions or correspondence in connection with these mark schemes.

Cambridge is publishing the mark schemes for the May/June 2012 question papers for most IGCSE, GCE Advanced Level and Advanced Subsidiary Level syllabuses and some Ordinary Level syllabuses.

Page 2	Mark Scheme: Teachers' version	Syllabus
	GCE O LEVEL – May/June 2012	4037

Mark Scheme Notes

Marks are of the following three types:

M Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.

A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).

B Accuracy mark for a correct result or statement independent of method marks.

- When a part of a question has two or more “method” steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly when there are several B marks allocated. The notation DM or DB (or dep*) is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.
- The symbol $\checkmark$ implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only. A and B marks are not given for fortuitously “correct” answers or results obtained from incorrect working.
- Note: B2 or A2 means that the candidate can earn 2 or 0.
B2, 1, 0 means that the candidate can earn anything from 0 to 2.

Page 3	Mark Scheme: Teachers' version	Syllabus	4037
	GCE O LEVEL – May/June 2012		

The following abbreviations may be used in a mark scheme or used on the scripts:

AG	Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)
BOD	Benefit of Doubt (allowed when the validity of a solution may not be absolutely clear)
CAO	Correct Answer Only (emphasising that no “follow through” from a previous error is allowed)
ISW	Ignore Subsequent Working
MR	Misread
PA	Premature Approximation (resulting in basically correct work that is insufficiently accurate)
SOS	See Other Solution (the candidate makes a better attempt at the same question)

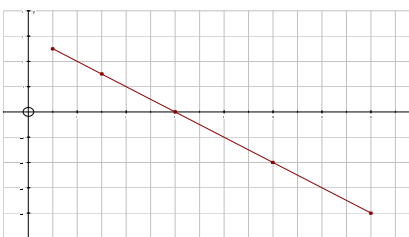
Penalties

MR –1	A penalty of MR –1 is deducted from A or B marks when the data of a question or part question are genuinely misread and the object and difficulty of the question remain unaltered. In this case all A and B marks then become “follow through $\sqrt{}$ ” marks. MR is not applied when the candidate misreads his own figures – this is regarded as an error in accuracy.
OW –1,2	This is deducted from A or B marks when essential working is omitted.
PA –1	This is deducted from A or B marks in the case of premature approximation.
S –1	Occasionally used for persistent slackness – usually discussed at a meeting.
EX –1	Applied to A or B marks when extra solutions are offered to a particular equation. Again, this is usually discussed at the meeting.

Page 4	Mark Scheme: Teachers' version	Syllabus
	GCE O LEVEL – May/June 2012	4037

1 (i)  (ii) $2x - 5 = \pm 3$, leading to $x = 1, 4$	B1 B1 B1, B1 [4]	B1 for shape B1 for both intercepts
2 $f(-2) : 4a - 2b = 46$ $f\left(\frac{1}{2}\right) : a + 2b = -21$ $a = 5, b = -13$	M1 M1 M1 A1 A1 [5]	M1 for substitution of $x = -2$ and equating to zero M1 for substitution of $x = 0.5$ and equating to -35 M1 for solution of equations
3 $x^2 + x(k - 2) + (5 - k) = 0$ Using '$b^2 > 4ac$', $(k - 2)^2 > 4(5 - k)$ $k^2 > 16$ $k > 4, k < -4$	M1 DM1 A1 A1 A1, A1 [6]	M1 for equating line and curve DM1 for use of $b^2 > 4ac$ $b = k - 2$ and $c = 5 - k$ Accept $< = \geq$ etc. A1 for each
4 (a) (i) 15120 (ii) 210 (b) (i) 15504 (ii) ${}^{12}C_{10} \times {}^8C_5$ $= 3696$ (iii) 56	B1 B1 B1 B1, B1 B1 B1 [7]	
5 (i) (0, 4) $\frac{dy}{dx} = 3x^2 + 4x - 3$ When $x = 0$, $\frac{dy}{dx} = -3$ $y - 4 = -3x$ (ii) $4 - 3x = x^3 + 2x^2 - 3x + 4$ leading to, $0 = x^3 + 2x^2$, (-2, 10)	B1 M1 M1 A1 M1 M1 A1 [7]	M1 for differentiation M1 for attempt at line equation M1 for equating line and curve M1 for solution of cubic A1 need x and y

Page 5	Mark Scheme: Teachers' version	Syllabus
	GCE O LEVEL – May/June 2012	4037

6 (i) $15 + 2 \frac{\sin^2 \theta}{\cos^2 \theta} = \frac{7}{\cos^2 \theta}$ $15 + 2 \tan^2 \theta = 7 \sec^2 \theta$ $15 + 2 \tan^2 \theta = 7(1 + \tan^2 \theta)$ leading to $\tan^2 \theta = \frac{8}{5}$ or $15 \cos^2 \theta + 2 \sin^2 \theta = 7(\cos^2 \theta + \sin^2 \theta)$ $8 \cos^2 \theta = 5 \sin^2 \theta$ leading to $\tan^2 \theta = \frac{8}{5}$ (ii) $\tan \theta = \pm \sqrt{\frac{8}{5}}$ leading to $\theta = 0.902, 2.24$ (also, $\sin \theta = \pm \sqrt{\frac{8}{13}}, \cos \theta = \pm \sqrt{\frac{5}{13}}$)	M1 M1 M1 A1 [M1] [M1] [M1] [A1] M1 A1, A1 [M1] [7]	M1 for dividing by $\cos^2 \theta$ M1 for $\frac{1}{\cos^2 \theta} = \sec^2 \theta$ M1 for $\sec^2 \theta = 1 + \tan^2 \theta$ A1 for rearrangement to get required result M1 for use of identity M1 for simplification M1 for use of $\tan \theta = \frac{\sin \theta}{\cos \theta}$ M1 for attempt to solve M1 for attempt to solve												
7 (i) $\frac{y}{x} = A + Bx$ <table border="1" style="margin-left: auto; margin-right: auto;"> <tr> <td>x</td> <td>1</td> <td>3</td> <td>6</td> <td>10</td> <td>14</td> </tr> <tr> <td>y/x</td> <td>2.5</td> <td>1.5</td> <td>0</td> <td>-2</td> <td>-4</td> </tr> </table>  (ii) Grad = $B = -0.5$ Intercept = $A = 3$	x	1	3	6	10	14	y/x	2.5	1.5	0	-2	-4	B1 M1 A2, 1, 0 M1, A1 M1, A1 [8]	M1 for attempt to calculate points and plot -1 each error M1 for grad = B M1 for intercept = A
x	1	3	6	10	14									
y/x	2.5	1.5	0	-2	-4									
8 (a) $2 \lg x - \lg(5x + 60) = \lg 10$ $\frac{x^2}{5x + 60} = 10$ leading to $x^2 - 50x - 600 = 0$ $x = 60$ (b) $\log_5 y = \frac{4 \log_5 5}{\log_5 y}$ $(\log_5 y)^2 = 4$ $\log_5 y = \pm 2$ $y = 25, \frac{1}{25}$	B1 B1 M1 DM1 A1 M1 M1 A1, A1 [9]	B1 for $\lg 10$ B1 for dealing with 'power' M1 for dealing with division DM1 for attempt to solve quadratic M1 for change of base M1 for valid attempt to solve												

Page 6	Mark Scheme: Teachers' version	Syllabus
	GCE O LEVEL – May/June 2012	4037

9 $120(p^7q^3)$ and $(45)(p^8q^2)$ $120p^7q^3 = 270p^8q^2$ $252p^5q^5 = 252$ $pq = 1$ and $4q = 9p$ leading to $p = \frac{2}{3}, q = \frac{3}{2}$	B3,2,1,0 M1 B1 B1 A1, A1 [8]	–1 per element (of 4) incorrect M1 for equating and multiplying by 6 B1 for $252p^5q^5$ B1 for $pq = 1$ OR $4p = 9q$ A1 for each
10 (i) $\frac{dy}{dx} = 2e^{2x} - 2e^{-2x}$ (ii) $3 = 2e^{2x} - 2e^{-2x}$ $2e^{4x} - 3e^{2x} - 2 = 0$ $(2e^{2x} + 1)(e^{2x} - 2) = 0$ $e^{2x} = 2, y = \frac{5}{2}$ (iii) $\frac{dx}{dt} = -0.5,$ $\frac{dy}{dt} = (2e^2 - 2e^{-2}) \times (-0.5)$ $= -7.25$	B1,B1 M1 DM1 M1 A1 M1, M1 A1 [9]	One per term M1 for attempt to obtain in ‘quadratic’ form DM1 for attempt to solve M1 for attempt to solve for y M1 for substitution of $x = 1$ M1 for correct application of chain rule
11 EITHER (i) $\frac{dy}{dx} = 18x - 3x^2$ When $\frac{dy}{dx} = 0, 0 = 3x(6 - x)$ Turning points when $x = 0, 6$ When $x = 6, y = 108$ (ii) Area $\left[3x^3 - \frac{x^4}{4} \right]_0^9$ $= 546.75$ $B(0, -18)$ Area of triangle = 81 Total Area = 628 Or: Area = $\int_0^9 9x^2 - x^3 - 2x + 18 \, dx$ $\left[3x^3 - \frac{x^4}{4} - x^2 + 18x \right]_0^9 = 628$	M1 M1 M1 A1 M1, A1 DM1,A1 B1 A1 [M1] [A3,2,1,0] [DM1,A1] [10]	M1 for differentiation M1 for equating to zero and attempt to solve M1 for finding y M1 for attempt to integrate DM1 for correct application of limits B1 for area of triangle

Page 7	Mark Scheme: Teachers' version	Syllabus
	GCE O LEVEL – May/June 2012	4037

11 OR (i) $\frac{dy}{dx} = 6 \cos 3x$ When $x = \frac{\pi}{9}$, $\frac{dy}{dx} = 3$, $y = \sqrt{3}$ Equation of normal $y - \sqrt{3} = -\frac{1}{3}\left(x - \frac{\pi}{9}\right)$ When $x = 0$, $y = 1.85$ (ii) $\frac{1}{2}(\sqrt{3} + 1.85)\frac{\pi}{9} - \int_0^{\frac{\pi}{9}} 2 \sin 3x dx$ $0.6251 - \left[-\frac{2}{3} \cos 3x\right]_0^{\frac{\pi}{9}}$ $0.6251 - \left(-\frac{1}{3}\right) = 0.292$ Alt method: $\text{Area} = \int_0^{\frac{\pi}{9}} \sqrt{3} - \frac{1}{3}\left(x - \frac{\pi}{9}\right) - 2 \sin 3x dx$ $\left[\sqrt{3}x - \frac{x^2}{6} + \frac{\pi x}{27} + \frac{2}{3} \cos 3x\right]_0^{\frac{\pi}{9}} = 0.292$	B1 B1 M1 M1 A1 B1 M1 A1 M1, A1 [M1] [A2,1,0] [DM1] [A1] [10]	B1 for differentiation For y Use of $m_1 m_2 = -1$ M1 for equation of normal and attempt to solve when $x = 0$ B1 for trapezium – allow unsimplified M1 for attempt to integrate A1 correct integration M1 for correct application of limits
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