CANDIDATE NAME

## CENTRE NUMBER



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$\square$

## CAMBRIDGE INTERNATIONAL MATHEMATICS

0607/03
Paper 3 (Core)
October/November 2011
1 hour 45 minutes
Candidates answer on the Question Paper
Additional Materials: Geometrical Instruments
Graphics Calculator

## READ THESE INSTRUCTIONS FIRST

Write your Centre number, candidate number and name on all the work you hand in.
Write in dark blue or black pen.
Do not use staples, paper clips, highlighters, glue or correction fluid.
You may use a pencil for any diagrams or graphs.
DO NOT WRITE IN ANY BARCODES.

Answer all the questions.
Unless instructed otherwise, give your answers exactly or correct to three significant figures as appropriate. Answers in degrees should be given to one decimal place.
For $\pi$, use your calculator value.
You must show all the relevant working to gain full marks and you will be given marks for correct methods, including sketches, even if your answer is incorrect.
The number of marks is given in brackets [ ] at the end of each question or part question.
The total number of marks for this paper is 96 .


This document consists of 16 printed pages.

Area, $A$, of triangle, base $b$, height $h$.
$A=\frac{1}{2} b h$

Area, $A$, of circle, radius $r$.
$A=\pi r^{2}$

Circumference, $C$, of circle, radius $r$.

Curved surface area, $A$, of cylinder of radius $r$, height $h$.
$A=2 \pi r h$

Curved surface area, $A$, of cone of radius $r$, sloping edge $l$.
$A=\pi r l$

Curved surface area, $A$, of sphere of radius $r$.

Volume, $V$, of prism, cross-sectional area $A$, length $l$.
$C=2 \pi r$

Volume, $V$, of pyramid, base area $A$, height $h$.
$V=\frac{1}{3} A h$

Volume, $V$, of cylinder of radius $r$, height $h$.
$V=\pi r^{2} h$

Volume, $V$, of cone of radius $r$, height $h$.
$V=\frac{1}{3} \pi r^{2} h$

Volume, $V$, of sphere of radius $r$.
$V=\frac{4}{3} \pi r^{3}$

Answer all the questions.
1 A bookcase is full of books.
One shelf holds exactly 35 books. Each book is 3.2 cm wide.

(a) Calculate $l$, the length of one shelf.

$$
\text { Answer(a) } l=
$$

$\qquad$ cm
(b) The bookcase contains 6 of these shelves.

Calculate the total number of books in the bookcase.

> Answer(b)
(c) The books cost $\$ 6$ each or $\$ 9$ each.

The ratio of $\$ 6$ books to $\$ 9$ books in the bookcase is $6: 9$.
(i) Write this ratio in its simplest form.
Answer(c)(i)
:
(ii) Find the number of $\$ 6$ books in the bookcase.

## Answer(c)(ii)

(iii) Find the total cost of all the books in the bookcase.

2 The monthly wages, in dollars, of 10 people are listed below.

| 1000 | 1400 | 1100 | 900 | 1050 |
| :--- | ---: | ---: | ---: | ---: |
| 1500 | 900 | 800 | 950 | 1300 |

(a) Calculate the mean.
Answer(a) \$
(b) Write down the mode.
(c) Find the range.
Answer(c) \$
(d) Calculate the percentage of these people with wages greater than $\$ 1100$.
$\qquad$ [2]
(e) One person is chosen at random.

Find the probability that this person's wage is less than $\$ 1100$.

Answer(e)
(f) The largest wages, $\$ 1500, \$ 1400$ and $\$ 1300$ are removed from the list.

Find the median of the remaining seven wages.

3 (a) Expand and simplify.

$$
2(x-3)+3(2 x+4)
$$

(b) Factorise completely.

$$
3 x^{2}-9 x y
$$

Answer(b)
(c) Solve the equation.

$$
3 x+5=x+12
$$

$$
\text { Answer(c) } x=
$$

(d) If $a=3$ and $b=-2$ find the value of $2 a-3 b$.

4 (a) On the axes, sketch the graph of the function $y=x^{2}-4$ for $-3 \leqslant x \leqslant 3$.

(b) Write down the co-ordinates of the minimum point of this graph.

> Answer(b)
(c) Write down the equation of the line of symmetry of this graph.

> Answer(c)
(d) Write down the range of this function.

> Answer(d)
(e) Write down the co-ordinates of the zeros of this function.
(f) On the same axes, sketch the graph of $y=\frac{1}{2} x+2$ for $-3 \leqslant x \leqslant 3$.
(g) Find the co-ordinates of the points where $x^{2}-4=\frac{1}{2} x+2$. Give each answer correct to 2 decimal places.

( .................. , .................... )

5 Surya has $\$ 5000$ in her bank account.
The bank pays interest at a rate of $3 \%$ each year.
(a) Find how much interest Surya receives at the end of the first year.

$$
\text { Answer }(a) \$
$$

(b) Surya does not remove the interest from her account.

Show that the total amount of money in her account at the end of the second year is $\$ 5304.50$.
(c) Surya does not remove any money from her account.
(i) Calculate the total amount of money in her account at the end of the fourth year.

> Answer(c)(i) \$
(ii) Find the total interest she receives.

6 One kilogram of apples costs $\$ x$. One kilogram of oranges costs $\$ y$.
(a) Write down the cost, in terms of $x$, of 6 kg of apples.

> Answer(a) \$
(b) Sami buys 6 kg of apples and 4 kg of oranges.

The total cost is $\$ 27$.
Use this information to write down an equation in $x$ and $y$.

> Answer(b)
(c) Terri buys 2 kg of apples and 3 kg of oranges.

The total cost is $\$ 14$.
Use this information to write down an equation in $x$ and $y$.

## Answer(c)

(d) Solve the two equations to find the cost of 1 kg of apples and the cost of 1 kg of oranges. Show all your working.

7 A ship sails 50 km from a point $S$ to a point $A$ on a bearing of $040^{\circ}$.


NOT TO
SCALE
(a) The ship took 2 hours 30 minutes to sail from $S$ to $A$.

Find the average speed of the ship in $\mathrm{km} / \mathrm{h}$.

Answer(a)
km/h
(b) Calculate the distance that $A$ is north of $S$.

Answer(b) $\qquad$ km
(c) Find the bearing of $S$ from $A$.

8 (a)


NOT TO
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The diagram shows a triangle $A B C$.
$A B$ is parallel to $P Q$ and $A B D$ is a straight line.
Angle $C A B=60^{\circ}$ and angle $C B D=140^{\circ}$.
Find the values of $x$ and $y$.

$$
\text { Answer(a) } x=
$$

$$
\begin{equation*}
y= \tag{2}
\end{equation*}
$$

(b)

$T A$ and $T B$ are tangents at $A$ and $B$ to the circle, centre $O$.
Angle $A T B=30^{\circ}$.
Find the values of $p$ and $q$.

$$
\begin{align*}
\text { Answer(b) } p & =. . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . ~ \\
~ & = \\
q & . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . ~ \tag{2}
\end{align*}
$$

(c)


NOT TO
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The straight lines $A D$ and $B E$ cross at $O$.
Angle $C O D=40^{\circ}$ and angle $D O E=60^{\circ}$.
Find the size of
(i) angle $A O B$,

> Answer(c)(i)
(ii) angle $A O E$,

> Answer(c)(ii)
(iii) angle $B O C$.

Answer(c)(iii)
(d)


NOT TO
SCALE

The diagram shows a circle, radius 10 cm , centre $O$.
A chord $A B$ is drawn so that its midpoint is 6 cm from $O$.
Calculate the length of the chord $A B$.

9 The cumulative frequency curve shows the marks that students scored in an examination.

(a) Write down how many students took the examination.
Answer(a)
(b) Find how many students scored less than 60 marks.

Answer(b)
(c) The top $10 \%$ of students received a prize.
(i) Find how many students received a prize.
Answer(c)(i)
(ii) Find the lowest possible mark for receiving a prize.
Answer(c)(ii)


A quadrilateral $P$ is drawn on the grid.
(a) Write down the geometrical name for the quadrilateral $P$.
Answer(a)
(b) Describe fully the single transformation that maps $P$ onto $Q$.
$\qquad$
$\qquad$
(c) Describe fully the single transformation that maps $P$ onto $R$.
$\qquad$
$\qquad$
(d) On the grid, draw the image of $P$ after a rotation of $90^{\circ}$ anticlockwise about $(0,0)$.
(e) On the grid, draw the image of $P$ after an enlargement centre $(0,0)$, scale factor 2 .


A train tunnel is in the shape of a semicircle on top of a rectangle.
The width of the tunnel is 6 m .
The total height of the tunnel is 7 m .
(a) (i) Find the radius of the semicircle.

> Answer(a)(i)
m
[1]
(ii) Find the value of $x$.

$$
\text { Answer(a)(ii) } x=
$$

(b) Calculate the area of the rectangle.

> Answer(b)
$\qquad$ $\mathrm{m}^{2}$
(c) Calculate the area of the semicircle.

Give your answer correct to 2 significant figures.
(d) The length of the tunnel is $\mathbf{3 5}$ kilometres.

Calculate the volume of earth, in cubic metres, that was removed to make the tunnel.

> Answer(d)
$\qquad$ $\mathrm{m}^{3}$
(e) A train travels at an average speed of $105 \mathrm{~km} / \mathrm{h}$ through the tunnel.
(i) Calculate the time, in minutes, it takes the train to travel through the tunnel.

Answer(e)(i) minutes
(ii) The train enters the tunnel at 1110 .

It arrives at the next station at 1202 .
Find the number of minutes between the train leaving the tunnel and arriving at the station.

12 A bag contains 4 green beads and 8 red beads. One bead is chosen at random from the bag.
(a) Find the probability that the bead chosen is red.

> Answer(a)
(b) The bead is not returned to the bag.

Find the probability that a second bead chosen at random from the bag is also red.
Answer(b)
(c) Use your answers to parts (a) and (b) to help you complete the tree diagram.

(d) Calculate the probability that two beads chosen at random are different colours.
Answer(d)

