

#### **Cambridge International Examinations**

Cambridge International General Certificate of Secondary Education

#### **CAMBRIDGE INTERNATIONAL MATHEMATICS**

0607/42

Paper 4 (Extended) May/June 2017

MARK SCHEME
Maximum Mark: 120

#### **Published**

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#### MARK SCHEME NOTES

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

#### Types of mark

- M Method marks, awarded for a valid method applied to the problem.
- A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. For accuracy marks to be given, the associated Method mark must be earned or implied.
- B Mark for a correct result or statement independent of Method marks.

When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. The notation 'dep' is used to indicate that a particular M or B mark is dependent on an earlier mark in the scheme.

#### **Abbreviations**

awrt answers which round to cao correct answer only

dep dependent

FT follow through after error isw ignore subsequent working nfww not from wrong working

oe or equivalent

rot rounded or truncated

SC Special Case soi seen or implied

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| Question  | Answer   | Marks | Partial Marks  |
|-----------|--|-------|--|
| 1(a)      | 1598 final answer  | 3     | <b>M2</b> for (23 970 × 0.8) ÷ 12 oe<br>or <b>M1</b> for 23 970 × 0.2 or better<br>or for 23 970 ÷ 12  |
| 1(b)(i)   | 23 500 nfww  | 3     | <b>M2</b> for 23 970 ÷ 1.02 oe<br>or <b>M1</b> for 23 970 = 102%   |
| 1(b)(ii)  | 2024 nfww  | 3     | M2 for $\frac{\log\left(\frac{30000}{23970}\right)}{\log 1.03}$ oe soi by 7.59or sketch leading to 7.59 or 2 trials, one giving 7 and one giving 8 or M1 for $23970 \times \left(1 + \frac{3}{100}\right)^n$ [= 30 000] oe seen or reasonable sketch or 3 trials of $23970 \times 1.03^n$ or 1 trial giving 8. |
| 2(a)(i)   | Reflection, $y = x$  | 1     |  |
| 2(a)(ii)  | Enlargement [with centre] (2, 1) [scale factor] $\frac{1}{4}$ oe | 2     | B1 for each  |
| 2(a)(iii) | Translation $ \begin{pmatrix} 3 \\ -5 \end{pmatrix} $            | 2     | B1 for each  |
| 2(b)(i)   | Correct triangle (0, 0), (0, 2), (-2, 3)                         | 2     | SC1 for rotation 90° clockwise about (0, 0) or rotation 90° anti-clockwise about different centre  |
| 2(b)(ii)  | Correct triangle (0, 0), (4, 0), (6, 2)                          | 2     | SC1 for stretch with s.f. = $2$ , $x$ -axis invariant or stretch with $y$ -axis invariant with different scale factor.   |
| 3(a)      | 6 points correct   | 3     | B2 for 4 or 5 correct<br>or B1 for 2 or 3 correct  |
| 3(b)      | Positive   | 1     |  |
| 3(c)(i)   | y = 0.787x + 0.356 final answer                                  | 2     | 0.7874 to $0.7875$ , $0.3555$ to $0.3556B1 for one corrector for y = 0.79x + 0.36 final answer$  |
| 3(c)(ii)  | 5.4[0]   | 1     | FT from their (c)(i)   |

| Question  | Answer   | Marks | Partial Marks  |
|-----------|--|-------|--|
| 4(a)(i)   | $\begin{pmatrix} -1.5\\1 \end{pmatrix}$ oe         | 1     |  |
| 4(a)(ii)  | $\begin{pmatrix} 10 \\ -1 \end{pmatrix}$           | 2     | B1 for each  |
| 4(a)(iii) | $\sqrt{13}$ final answer                           | 2     | M1 for $(-3)^2 + 2^2$ oe soi by 3.61 or 3.605 to 3.606 $\sqrt{13}$ in working implies M1   |
| 4(b)      | Correct B clearly indicated                        | 2     | <b>B1</b> for vector $\begin{pmatrix} 1 \\ 5 \end{pmatrix}$ drawn not from $A$ or $\begin{pmatrix} 1 \\ 5 \end{pmatrix}$ seen or correctly following through, from $A$ , their incorrect vector seen. or either $\begin{pmatrix} -3 \\ 2 \end{pmatrix}$ or $\begin{pmatrix} 4 \\ 3 \end{pmatrix}$ correctly drawn <b>only</b> if one starts from $A$ . |
| 5(a)      | 2500   | 2     | <b>M1</b> for 119050 ÷ 47.62   |
| 5(b)(i)   | [0]610 or 610 am oe                                | 2     | <b>B1</b> for [0]025 or [0]340 or 28 h 130 min oe seen   |
| 5(b)(ii)  | 722 or 721.7                                       | 3     | M1 for 4150 ÷ <i>their</i> 5h 45 min<br>B1 for 5.75 oe   |
| 5(b)(iii) | 5 h 32 (or 31.8 to 32[.0]) min                     | 3     | M1 for 4150 ÷ 750 soi by 5.53 or 5.53 B1FT for correct conversion to hours and minutes   |
| 6(a)(i)   | [x =] cv oe  | 1     |  |
| 6(a)(ii)  | $[y =] kv^2$ oe                                    | 1     |  |
| 6(a)(iii) | $[d =] cv + kv^2 \text{ or } v(c + kv) \text{ oe}$ | 1     | FT   |
| 6(b)(i)   | $750 = 12c + 12^2 k \text{ oe}$                    | M1    | isw any cancelling   |
| 6(b)(ii)  | $2050 = 20c + 20^2 k \text{ oe}$                   | 1     | isw any cancelling   |
| 6(c)      | [c =] 2.5  oe cao $[k =] 5  cao$                   | 3     | <ul> <li>M1 for correctly eliminating one variable from their equations in this part. or sketches of lines</li> <li>A1 for either solution</li> <li>If zero scored SC1 for their values satisfying one equation.</li> </ul>  |
| 6(d)      | 8100   | 2     | M1 for correct substitution of 40 into their (a)(iii) containing their values of $c$ and $k$ .   |

| Question | Answer   | Marks | Partial Marks  |
|----------|--|-------|--|
| 7(a)     | Correct sketch showing bearings and distances  | 3     | B1 for 310° bearing approx correct (270 to 360) and marked B1 for 250° bearing approx correct (180 to 270) and marked B1 for distances correctly marked  |
| 7(b)     | 120  | 1     |  |
| 7(c)     | $40^2 + 65^2 - 2 \times 40 \times 65 \times \cos their$ 120  | M1    | their 120 must be between 0 and 180<br>Allow $\cos 120 = \frac{40^2 + 65^2 - [\ ]^2}{2 \times 40 \times 65}$   |
|          | 91.78 to 91.79   | A2    | <b>A1</b> for 8425 or $5\sqrt{337}$  |
| 7(d)     | 288 or 287.8   | 4     | M2 for $\frac{40\sin(their120)}{91.8}$ oe  |
|          |  |       | or M1 for $\frac{\sin \theta}{40} = \frac{\sin(their 120)}{91.8}$ oe  If cosine rule used, M2 for explicit expression or M1 for implicit.  |
|          |  |       | <b>A1</b> for 22.2 or 22.16 to 22.17   |
|          |  |       | If 0 scored SC2 for answer 108 or 107.8  |
| 8(a)     | To the second se | 3     | With correct shape with two max on right of <i>y</i> -axis and one on left, all above <i>x</i> -axis and reasonable quality or <b>B2</b> for correct shape and all above <i>x</i> -axis or <b>B1</b> for correct shape |
|          | Correct sketch   |       |  |
| 8(b)     | -270, 90, 450  | 3     | B1 for each SC2 for all correct but with y co-ords or SC1 for two correct with y co-ords   |
| 8(c)     | 750, 870   | 2     | B1 for each  |
| 8(d)     | x < 54.7   | 1     | 54.74 to 54.75   |
|          | 164 < x < 267  | 2     | 163.5 to 163.6, 266.6  B1 for one inequality or B1 for both values seen  |
|          |  |       | If 0 scored, <b>B1</b> for straight line with negative gradient crossing curve three times between $x = 0$ and $x = 400$ . May be freehand.  |

| Question  | Answer  | Marks | Partial Marks   |
|-----------|---|-------|---|
| 9(a)(i)   | $\frac{1}{2} \times x \times (x+2) \times \frac{\sqrt{3}}{2} \text{ oe or better}$ final answer | 2     | <b>M1</b> for $\frac{1}{2} \times x \times (x+2) \times \sin 60$  |
| 9(a)(ii)  | equating to $18\sqrt{3}$ and correct elimination of $\sqrt{3}$                                  | M1    | Dependent on correct answer used from (a)(i) or answer to (a)(i) contains sin60 but is otherwise correct.   |
|           | Completion with at least one step   | A1    | No errors or omissions  |
| 9(b)(i)   | 7.54 or 7.544, –9.54 or –9.544  | 2     | <b>B1</b> for each If 0 scored, <b>M1</b> for substitution in formula or sketch or $(x + 1)^2 - 73$ or better   |
| 9(b)(ii)  | 6.53 or 6.54 or 6.529 to 6.536  | 2     | M1 for $\sin 60 = \frac{[]}{their7.54}$ oe  |
| 10(a)(i)  | $[y=] \frac{1}{2}x + 1$   | 3     | M1 for gradient = $\frac{8-2}{14-2}$ oe  M1 for correct substitution of (2, 2) or (14, 8) into $y = (their \ m)x + c$ oe soi  |
| 10(a)(ii) | [y=]-2x+26  | 3     | M1 for gradient = $\frac{-1}{their} \frac{1}{\frac{1}{2}}$<br>M1 for substituting (11, 4) into $y = (their - 2)x + c$ oe soi  |
| 10(b)     | Correct substitution and completion of (10, 6) for both lines oe                                | 2     | B1 for either  OR  M1 for correct elimination of x or y from equations A1 for completion to solution (10, 6)  |
| 10(c)     | (9, 8)  | 1     |   |
| 10(d)     | 30 cao  | 4     | M3 for $\left[\frac{1}{2}\right] \times \sqrt{12^2 + 6^2} \times \sqrt{2^2 + 4^2}$ oe<br>or B2 for two of $\sqrt{12^2 + 6^2}$ oe $(AC)$ , $\sqrt{2^2 + 4^2}$ oe<br>$(BD \text{ or } MC)$ , $\sqrt{8^2 + 4^2}$ oe $(AM)$ , $\sqrt{2^2 + 1^2}$ oe $(MD \text{ or } MB)$<br>or B1 for one of these. $(M \text{ is the intersection of } AC \text{ and } BD)$<br>OR<br>M3 for full area e.g. $[0.5 \times 12 \times 6 - 0.5 \times 6 \times 7] \times 2$<br>or B2 for 2 correct areas evaluated |

| Question  | Answer   | Marks          | Partial Marks   |
|-----------|--|----------------|---|
| 11(a)     | 12.9 or 12.86 to 12.87                                   | 2              | M1 for evidence of at least three mid-interval values 9.5, 11, 13, 15.5 soi by 95, 550, 845, 697.5 or 2187.5  |
| 11(b)     | Correct Histogram  | 4              | B1 for correct bar widths no gaps   |
|           |  |                | B3 for 4 correct heights and corresponding scale from 0 or B2 for 3 correct heights and corresponding scale from 0 or B1 for 2 correct heights and corresponding scale from 0 |
|           |  |                | or <b>B1</b> for 3 correct frequency densities soi  |
| 11(c)(i)  | $\frac{198}{2873}$ oe                                    | 2              | <b>M1</b> for $\frac{45}{170} \times \frac{44}{169}$  |
| 11(c)(ii) | $\frac{100}{2873}$ oe                                    | 3              | <b>M2</b> for $\frac{10}{170} \times \frac{50}{169} + \frac{50}{170} \times \frac{10}{169}$ oe or <b>M1</b> for $\frac{10}{170} \times \frac{50}{169}$                        |
| 12(a)     | 11   | 1              |   |
| 12(b)     | 6  | 2              | <b>B1</b> for h(2) = 1 soi or $4(x^2 - 3) + 2$ or better  |
| 12(c)     | -3   | 2              | <b>M1</b> for $4x = -10 - 2$  |
| 12(d)     | $h(x) \geqslant -3$                                      | 1              | Allow $y \ge -3$  |
| 12(e)     | $\frac{x-2}{4}$ oe final answer                          | 2              | <b>M1</b> for $y - 2 = 4x$ or $x = 4y + 2$ or $\frac{y}{4} = x + \frac{2}{4}$   |
| 12(f)     | Stretch x-axis invariant [Scale factor] 2 OR             | 3              | B1 for each   |
|           | Reflection $y = -2.70 + 6.75$                            | M1<br>A2       |   |
|           | OR   |                |   |
|           | Rotation (2.5, 0) 167 (167.47) or 12.5 (12.53) clockwise | M1<br>A1<br>A1 |   |
| 12(g)     | $[y =] x^2 - 4x + 1$                                     | 3              | M2 for $y = (x - 2)^2 - 3$<br>or M1 for $x - 2$ seen in a quadratic<br>If 0 scored, SC1 for $y = x^2 + 4x + 1$  |