

# UNIVERSITY OF CAMBRIDGE INTERNATIONAL EXAMINATIONS International General Certificate of Secondary Education

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CANDIDATE NAME					
CENTRE NUMBER			CANDIDATE NUMBER		

#### **ADDITIONAL MATHEMATICS**

0606/11

Paper 1

October/November 2012

2 hours

Candidates answer on the Question Paper.

Additional Materials:

Electronic calculator.

#### READ THESE INSTRUCTIONS FIRST

Write your Centre number, candidate number and name on all the work you hand in.

Write in dark blue or black pen.

You may use a pencil for any diagrams or graphs.

Do not use staples, paper clips, highlighters, glue or correction fluid.

Answer all the questions.

Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place in the case of angles in degrees, unless a different level of accuracy is specified in the question.

The use of an electronic calculator is expected, where appropriate.

You are reminded of the need for clear presentation in your answers.

At the end of the examination, fasten all your work securely together.

The number of marks is given in brackets [ ] at the end of each question or part question.

The total number of marks for this paper is 80.

For Examiner's Use	
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This document consists of 16 printed pages.



#### Mathematical Formulae

#### 1. ALGEBRA

## Quadratic Equation

For the equation  $ax^2 + bx + c = 0$ ,

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Binomial Theorem

$$(a+b)^n = a^n + \binom{n}{1}a^{n-1}b + \binom{n}{2}a^{n-2}b^2 + \dots + \binom{n}{r}a^{n-r}b^r + \dots + b^n,$$

where *n* is a positive integer and  $\binom{n}{r} = \frac{n!}{(n-r)!r!}$ 

#### 2. TRIGONOMETRY

#### Identities

$$\sin^2 A + \cos^2 A = 1$$
$$\sec^2 A = 1 + \tan^2 A$$
$$\csc^2 A = 1 + \cot^2 A$$

## Formulae for $\triangle ABC$

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^{2} = b^{2} + c^{2} - 2bc \cos A$$
$$\Delta = \frac{1}{2} bc \sin A$$

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(i) Sketch the graph of y = |3 + 5x|, showing the coordinates of the points where your general meets the coordinate axes. 1

(ii) Solve the equation |3 + 5x| = 2.

[2]

2 Find the values of k for which the line y = k - 6x is a tangent to the curve y = x(2x + k). [4]

[2]

[5]

- 3 Given that  $p = \log_q 32$ , express, in terms of p,
  - (i)  $\log_q 4$ ,

(ii) 
$$\log_q 16q$$
.

4 Using the substitution 
$$u = 5^x$$
, or otherwise, solve

$$5^{2x+1} = 7(5^x) - 2.$$

(ii) the approximate change in y when x increases from  $\frac{\pi}{4}$  to  $\frac{\pi}{4} + p$ , where p is small. [2] 6 (i) Find the first 3 terms, in descending powers of x, in the expansion of  $\left(x + \frac{2}{x^2}\right)^6$ .

(ii) Hence find the term independent of x in the expansion of  $\left(2 - \frac{4}{x^3}\right) \left(x + \frac{2}{x^2}\right)^6$ . [2]

[1]

# 7 Do not use a calculator in any part of this question.

(a) (i) Show that  $3\sqrt{5} - 2\sqrt{2}$  is a square root of  $53 - 12\sqrt{10}$ .

(ii) State the other square root of  $53 - 12\sqrt{10}$ .

**(b)** Express  $\frac{6\sqrt{3} + 7\sqrt{2}}{4\sqrt{3} + 5\sqrt{2}}$  in the form  $a + b\sqrt{6}$ , where a and b are integers to be found. [4]

δ	a.
8 The points $A(-3, 6)$ , $B(5, 2)$ and $C$ lie on a straight line such that $B$ is the mid-point of $A(-3, 6)$ .	AC.
8 The points $A(-3, 6)$ , $B(5, 2)$ and $C$ lie on a straight line such that $B$ is the mid-point of $AC$ (i) Find the coordinates of $C$ .	Abridge com
The point $D$ lies on the $y$ -axis and the line $CD$ is perpendicular to $AC$ .	
(ii) Find the area of the triangle ACD.	[5]

(ii) Find 
$$g^{-1}(x)$$
.

(iii) Write down the domain of 
$$g^{-1}(x)$$
.

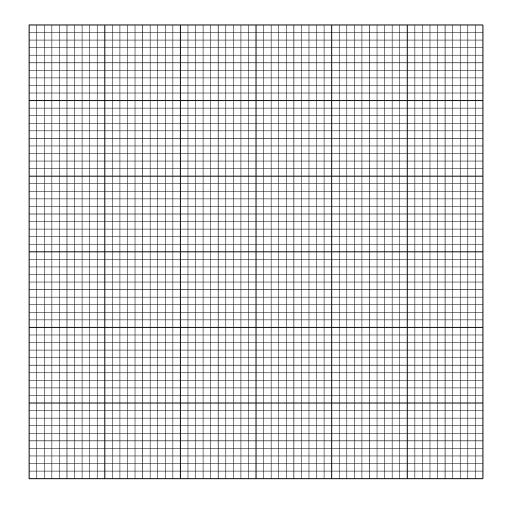
(iv) Solve 
$$g^2(x) = 3$$
.

10 The table shows values of the variables x and y.

х	10°	30°	45°	60°	80°
y	11.2	16	19.5	22.4	24.7

(i) Using the graph paper below, plot a suitable straight line graph to show that, for  $10^{\circ} \le x \le 80^{\circ}$ ,

$$\sqrt{y} = A \sin x + B$$
, where A and B are positive constants. [4]



(ii) Use your graph to find the value of A and of B.

(iii) Estimate the value of y when x = 50.

(iv) Estimate the value of x when y = 12.

[2]

[2]

11 (a) Solve cosec  $\left(2x - \frac{\pi}{3}\right) = \sqrt{2}$  for  $0 < x < \pi$  radians.

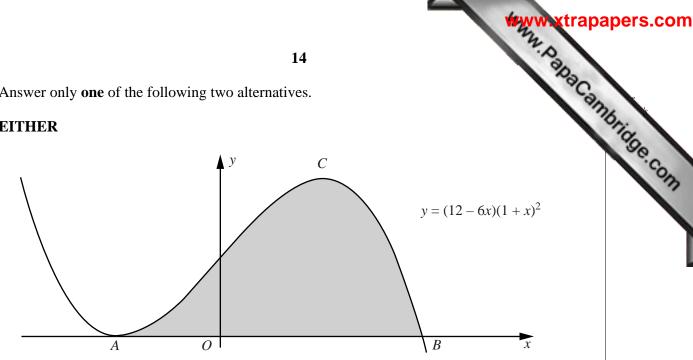
(b) (i) Given that  $5(\cos y + \sin y)(2\cos y - \sin y) = 7$ , show that  $12\tan^2 y - 5\tan y - 3 = 0$ . [4]

(ii) Hence solve  $5(\cos y + \sin y)(2\cos y - \sin y) = 7 \text{ for } 0^{\circ} < x < 180^{\circ}$ .

13

Answer only **one** of the following two alternatives.

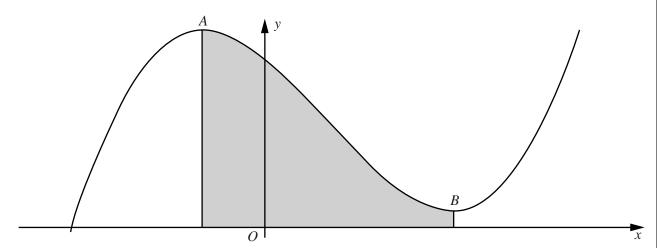
## **EITHER**



The diagram shows part of the graph of  $y = (12 - 6x)(1 + x)^2$ , which meets the x-axis at the points *A* and *B*. The point *C* is the maximum point of the curve.

- Find the coordinates of each of *A*, *B* and *C*. [6]
- Find the area of the shaded region. [5]

OR



The diagram shows part of a curve such that  $\frac{dy}{dx} = 3x^2 - 6x - 9$ . Points A and B are stationary points of the curve and lines from A and B are drawn perpendicular to the x-axis. Given that the curve passes through the point (0, 30), find

(ii) the x-coordinate of A and of B, 
$$[3]$$

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