

Cambridge IGCSE[™]

CANDIDATE NAME		
CENTRE NUMBER		CANDIDATE NUMBER
ADDITIONAL MATHEMATICS 06		0606/11
Paper 1		October/November 2020
		2 hours

You must answer on the question paper.

No additional materials are needed.

INSTRUCTIONS

- Answer **all** questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do **not** write on any bar codes.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

INFORMATION

- The total mark for this paper is 80.
- The number of marks for each question or part question is shown in brackets [].

Mathematical Formulae

1. ALGEBRA

Quadratic Equation

For the equation $ax^2 + bx + c = 0$,

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Binomial Theorem

$$(a+b)^{n} = a^{n} + \binom{n}{1}a^{n-1}b + \binom{n}{2}a^{n-2}b^{2} + \dots + \binom{n}{r}a^{n-r}b^{r} + \dots + b^{n}$$

where *n* is a positive integer and $\binom{n}{r} = \frac{n!}{(n-r)!r!}$

Arithmetic series
$$u_n = a + (n-1)d$$

 $S_n = \frac{1}{2}n(a+l) = \frac{1}{2}n\{2a + (n-1)d\}$

Geometric series $u_n = ar^{n-1}$ $S_n = \frac{a(1-r^n)}{1-r} \ (r \neq 1)$ $S_{\infty} = \frac{a}{1-r} \ (|r| < 1)$

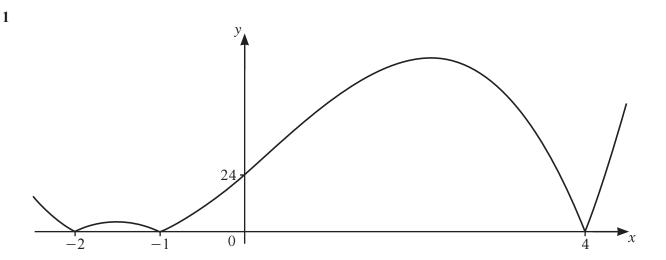
2. TRIGONOMETRY

Identities

$$\sin^2 A + \cos^2 A = 1$$
$$\sec^2 A = 1 + \tan^2 A$$
$$\csc^2 A = 1 + \cot^2 A$$

Formulae for $\triangle ABC$

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$
$$a^{2} = b^{2} + c^{2} - 2bc \cos A$$
$$\Delta = \frac{1}{2}bc \sin A$$

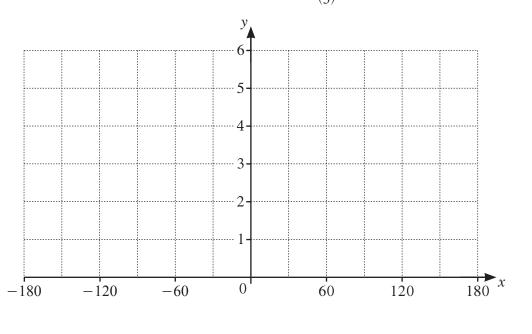


The diagram shows the graph of y = |p(x)|, where p(x) is a cubic function. Find the two possible expressions for p(x). [3]

2 (a) Write down the amplitude of
$$1 + 4\cos\left(\frac{x}{3}\right)$$
. [1]

(b) Write down the period of $1 + 4\cos\left(\frac{x}{3}\right)$. [1]

(c) On the axes below, sketch the graph of $y = 1 + 4\cos\left(\frac{x}{3}\right)$ for $-180^\circ \le x^\circ \le 180^\circ$.



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[3]

[3]

3 (a) Write
$$\frac{\sqrt{p}(qr^2)^{\frac{1}{3}}}{(q^3p)^{-1}r^3}$$
 in the form $p^a q^b r^c$, where *a*, *b* and *c* are constants. [3]

(b) Solve
$$6x^{\frac{2}{3}} - 5x^{\frac{1}{3}} + 1 = 0$$
.

4 It is given that $y = \frac{\tan 3x}{\sin x}$.

(a) Find the exact value of
$$\frac{dy}{dx}$$
 when $x = \frac{\pi}{3}$.

[4]

(b) Hence find the approximate change in y as x increases from $\frac{\pi}{3}$ to $\frac{\pi}{3} + h$, where h is small. [1]

(c) Given that x is increasing at the rate of 3 units per second, find the corresponding rate of change in y when $x = \frac{\pi}{3}$, giving your answer in its simplest surd form. [2]

5 (a) (i) Find how many different 4-digit numbers can be formed using the digits 1, 3, 4, 6, 7 and 9. Each digit may be used once only in any 4-digit number. [1]

(ii) How many of these 4-digit numbers are even and greater than 6000? [3]

- (b) A committee of 5 people is to be formed from 6 doctors, 4 dentists and 3 nurses. Find the number of different committees that could be formed if
 - (i) there are no restrictions, [1]
 - (ii) the committee contains at least one doctor, [2]

(iii) the committee contains all the nurses.

[1]

[3]

- 6 A particle *P* is initially at the point with position vector $\begin{pmatrix} 30\\10 \end{pmatrix}$ and moves with a constant speed of $10 \,\mathrm{ms}^{-1}$ in the same direction as $\begin{pmatrix} -4\\3 \end{pmatrix}$.
 - (a) Find the position vector of *P* after *t* s.

As *P* starts moving, a particle *Q* starts to move such that its position vector after *t*s is given by $\binom{-80}{90} + t\binom{5}{12}.$

(b) Write down the speed of Q.

[1]

(c) Find the exact distance between P and Q when t = 10, giving your answer in its simplest surd form. [3]

[1]

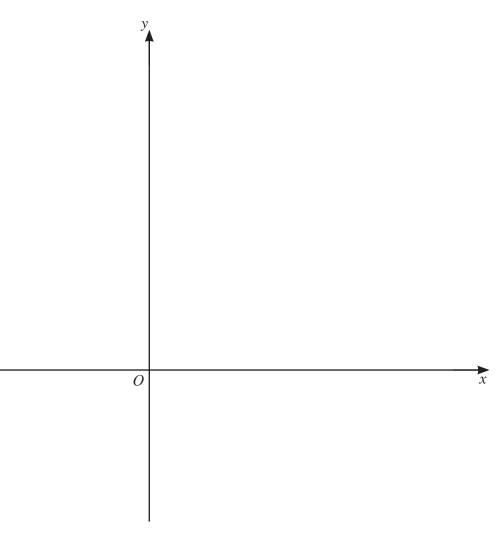
[3]

7 It is given that $f(x) = 5\ln(2x+3)$ for $x > -\frac{3}{2}$.

(a) Write down the range of f.

(b) Find f^{-1} and state its domain.

(c) On the axes below, sketch the graph of y = f(x) and the graph of $y = f^{-1}(x)$. Label each curve and state the intercepts on the coordinate axes.



8 (a) (i) Show that
$$\frac{1}{(1 + \csc \theta)(\sin \theta - \sin^2 \theta)} = \sec^2 \theta.$$
 [4]

(ii) Hence solve $(1 + \csc \theta)(\sin \theta - \sin^2 \theta) = \frac{3}{4}$ for $-180^\circ \le \theta \le 180^\circ$. [4]

(b) Solve $\sin\left(3\phi + \frac{2\pi}{3}\right) = \cos\left(3\phi + \frac{2\pi}{3}\right)$ for $0 \le \phi \le \frac{2\pi}{3}$ radians, giving your answers in terms of π . [4]

9 (a) Given that $\int_{1}^{a} \left(\frac{1}{x} - \frac{1}{2x+3}\right) dx = \ln 3$, where a > 0, find the exact value of a, giving your answer in simplest surd form. [6]

(b) Find the exact value of
$$\int_0^{\frac{\pi}{3}} \left(\sin\left(2x + \frac{\pi}{3}\right) - 1 + \cos 2x \right) dx.$$
 [5]

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10 (a) An arithmetic progression has a second term of 8 and a fourth term of 18. Find the least number of terms for which the sum of this progression is greater than 1560. [6]

- (b) A geometric progression has a sum to infinity of 72. The sum of the first 3 terms of this progression is $\frac{333}{8}$.
 - (i) Find the value of the common ratio.

[5]

(ii) Hence find the value of the first term.

[1]

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