## Cambridge IGCSE ${ }^{\text {TM }}$

CANDIDATE NAME

CENTRE NUMBER


## ADDITIONAL MATHEMATICS

0606/22
Paper 2
October/November 2020
2 hours
You must answer on the question paper.
No additional materials are needed.

## INSTRUCTIONS

- Answer all questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do not use an erasable pen or correction fluid.
- Do not write on any bar codes.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.


## INFORMATION

- The total mark for this paper is 80 .
- The number of marks for each question or part question is shown in brackets [ ].


## Mathematical Formulae

## 1. ALGEBRA

Quadratic Equation
For the equation $a x^{2}+b x+c=0$,

$$
x=\frac{-b \pm \sqrt{b^{2}-4 a c}}{2 a}
$$

Binomial Theorem

$$
(a+b)^{n}=a^{n}+\binom{n}{1} a^{n-1} b+\binom{n}{2} a^{n-2} b^{2}+\ldots+\binom{n}{r} a^{n-r} b^{r}+\ldots+b^{n}
$$

where $n$ is a positive integer and $\binom{n}{r}=\frac{n!}{(n-r)!r!}$

Arithmetic series

$$
\begin{aligned}
& u_{n}=a+(n-1) d \\
& S_{n}=\frac{1}{2} n(a+l)=\frac{1}{2} n\{2 a+(n-1) d\}
\end{aligned}
$$

Geometric series

$$
\begin{aligned}
& u_{n}=a r^{n-1} \\
& S_{n}=\frac{a\left(1-r^{n}\right)}{1-r} \quad(r \neq 1) \\
& S_{\infty}=\frac{a}{1-r}(|r|<1)
\end{aligned}
$$

## 2. TRIGONOMETRY

Identities

$$
\begin{gathered}
\sin ^{2} A+\cos ^{2} A=1 \\
\sec ^{2} A=1+\tan ^{2} A \\
\operatorname{cosec}^{2} A=1+\cot ^{2} A
\end{gathered}
$$

Formulae for $\triangle A B C$

$$
\begin{gathered}
\frac{a}{\sin A}=\frac{b}{\sin B}=\frac{c}{\sin C} \\
a^{2}=b^{2}+c^{2}-2 b c \cos A \\
\Delta=\frac{1}{2} b c \sin A
\end{gathered}
$$

1 Solve the inequality $(x-8)(x-10)>35$.

2 Find the value of $x$ such that $\frac{4^{x+1}}{2^{x-1}}=32^{\frac{x}{3}} \times 8^{\frac{1}{3}}$.

3 (a) Find the equation of the perpendicular bisector of the line joining the points $(12,1)$ and $(4,3)$, giving your answer in the form $y=m x+c$.
(b) The perpendicular bisector cuts the axes at points $A$ and $B$. Find the length of $A B$.

4 Solve the simultaneous equations.

$$
\begin{align*}
\log _{3}(x+y) & =2 \\
2 \log _{3}(x+1) & =\log _{3}(y+2) \tag{6}
\end{align*}
$$

## 5 DO NOT USE A CALCULATOR IN THIS QUESTION.

(a) Find the equation of the tangent to the curve $y=x^{3}-6 x^{2}+3 x+10$ at the point where $x=1$.
(b) Find the coordinates of the point where this tangent meets the curve again.

6 Find the exact value of $\int_{2}^{4} \frac{(x+1)^{2}}{x^{2}} \mathrm{~d} x$.

7 A geometric progression has a first term of 3 and a second term of 2.4. For this progression, find
(a) the sum of the first 8 terms,
(b) the sum to infinity,
(c) the least number of terms for which the sum is greater than $95 \%$ of the sum to infinity.

## 8 DO NOT USE A CALCULATOR IN THIS QUESTION.

In this question lengths are in centimetres.


You may use the following trigonometric ratios.

$$
\begin{aligned}
& \sin 30^{\circ}=\frac{1}{2} \\
& \cos 30^{\circ}=\frac{\sqrt{3}}{2} \\
& \tan 30^{\circ}=\frac{1}{\sqrt{3}}
\end{aligned}
$$

(a) Given that the area of the triangle $A B C$ is $5.5 \mathrm{~cm}^{2}$, find the exact length of $A C$. Write your answer in the form $a+b \sqrt{3}$, where $a$ and $b$ are integers.
(b) Show that $B C^{2}=c+d \sqrt{3}$, where $c$ and $d$ are integers to be found.


In the diagram $\overrightarrow{O P}=\mathbf{2 b}, \overrightarrow{O S}=3 \mathbf{a}, \overrightarrow{S R}=\mathbf{b}$ and $\overrightarrow{P Q}=\mathbf{a}$. The lines $O R$ and $Q S$ intersect at $X$.
(a) Find $\overrightarrow{O Q}$ in terms of $\mathbf{a}$ and $\mathbf{b}$.
(b) Find $\overrightarrow{Q S}$ in terms of $\mathbf{a}$ and $\mathbf{b}$.
(c) Given that $\overrightarrow{Q X}=\mu \overrightarrow{Q S}$, find $\overrightarrow{O X}$ in terms of $\mathbf{a}, \mathbf{b}$ and $\mu$.
(d) Given that $\overrightarrow{O X}=\lambda \overrightarrow{O R}$, find $\overrightarrow{O X}$ in terms of $\mathbf{a}, \mathbf{b}$ and $\lambda$.
(e) Find the value of $\lambda$ and of $\mu$.
(f) Find the value of $\frac{Q X}{X S}$.
(g) Find the value of $\frac{O R}{O X}$.

10 The number, $b$, of bacteria in a sample is given by $b=P+Q \mathrm{e}^{2 t}$, where $P$ and $Q$ are constants and $t$ is time in weeks. Initially there are 500 bacteria which increase to 600 after 1 week.
(a) Find the value of $P$ and of $Q$.
(b) Find the number of bacteria present after 2 weeks.
(c) Find the first week in which the number of bacteria is greater than 1000000 .

11 (a) Show that $\frac{\sin x \tan x}{1-\cos x}=1+\sec x$.
(b) Solve the equation $5 \tan x-3 \cot x=2 \sec x$ for $0^{\circ} \leqslant x \leqslant 360^{\circ}$.

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