## Cambridge IGCSE ${ }^{\text {TM }}$

CANDIDATE NAME

CENTRE NUMBER


ADDITIONAL MATHEMATICS
0606/11
Paper 1
October/November 2021
2 hours
You must answer on the question paper.
No additional materials are needed.

## INSTRUCTIONS

- Answer all questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do not use an erasable pen or correction fluid.
- Do not write on any bar codes.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.


## INFORMATION

- The total mark for this paper is 80 .
- The number of marks for each question or part question is shown in brackets [ ].


## Mathematical Formulae

## 1. ALGEBRA

Quadratic Equation
For the equation $a x^{2}+b x+c=0$,

$$
x=\frac{-b \pm \sqrt{b^{2}-4 a c}}{2 a}
$$

Binomial Theorem

$$
(a+b)^{n}=a^{n}+\binom{n}{1} a^{n-1} b+\binom{n}{2} a^{n-2} b^{2}+\ldots+\binom{n}{r} a^{n-r} b^{r}+\ldots+b^{n}
$$

where $n$ is a positive integer and $\binom{n}{r}=\frac{n!}{(n-r)!r!}$

Arithmetic series

$$
\begin{aligned}
& u_{n}=a+(n-1) d \\
& S_{n}=\frac{1}{2} n(a+l)=\frac{1}{2} n\{2 a+(n-1) d\}
\end{aligned}
$$

Geometric series

$$
\begin{aligned}
& u_{n}=a r^{n-1} \\
& S_{n}=\frac{a\left(1-r^{n}\right)}{1-r} \quad(r \neq 1) \\
& S_{\infty}=\frac{a}{1-r}(|r|<1)
\end{aligned}
$$

## 2. TRIGONOMETRY

Identities

$$
\begin{gathered}
\sin ^{2} A+\cos ^{2} A=1 \\
\sec ^{2} A=1+\tan ^{2} A \\
\operatorname{cosec}^{2} A=1+\cot ^{2} A
\end{gathered}
$$

Formulae for $\triangle A B C$

$$
\begin{gathered}
\frac{a}{\sin A}=\frac{b}{\sin B}=\frac{c}{\sin C} \\
a^{2}=b^{2}+c^{2}-2 b c \cos A \\
\Delta=\frac{1}{2} b c \sin A
\end{gathered}
$$

1


The diagram shows the graph of $y=a \sin \frac{x}{b}+c$ for $-360^{\circ} \leqslant x \leqslant 360^{\circ}$, where $a, b$ and $c$ are integers.
(a) Write down the period of $a \sin \frac{x}{b}+c$.
(b) Find the value of $a$, of $b$ and of $c$.

2 Points $A$ and $C$ have coordinates $(-4,6)$ and $(2,18)$ respectively. The point $B$ lies on the line $A C$ such that $\overrightarrow{A B}=\frac{2}{3} \overrightarrow{A C}$.
(a) Find the coordinates of $B$.
(b) Find the equation of the line $l$, which is perpendicular to $A C$ and passes through $B$.
(c) Find the area enclosed by the line $l$ and the coordinate axes.

3 (a) Find the vector which has magnitude 39 and is in the same direction as $\binom{12}{-5}$.
(b) Given that $\mathbf{a}=\binom{2}{-1}$ and $\mathbf{b}=\binom{-4}{5}$, find the constants $\lambda$ and $\mu$ such that $5 \mathbf{a}+\lambda\binom{4}{6}=\mu \mathbf{b}$. [4]

4 (a) Given that $\frac{q^{-2} \sqrt{p r}}{\sqrt[3]{r}(p q)^{-3}}=p^{a} q^{b} r^{c}$, find the value of each of the constants $a, b$ and $c$.
(b) Solve the equation $3 x^{\frac{4}{5}}-8 x^{\frac{2}{5}}+5=0$.

5 The polynomial $\mathrm{p}(x)=a x^{3}+b x^{2}+6 x+4$, where $a$ and $b$ are integers, is divisible by $x-2$. When $\mathrm{p}^{\prime}(x)$ is divided by $x+1$ the remainder is -7 .
(a) Find the value of $a$ and of $b$.
(b) Using your answers to part (a), find the remainder when $\mathrm{p}^{\prime \prime}(x)$ is divided by $x$.

6 A curve with equation $y=\mathrm{f}(x)$ is such that $\frac{\mathrm{d}^{2} y}{\mathrm{~d} x^{2}}=6 \mathrm{e}^{3 x}+4 x$. The curve has a gradient of 5 at the point $\left(0, \frac{5}{3}\right)$. Find $\mathrm{f}(x)$.

7 The first three terms, in ascending powers of $x$, in the expansion of $(2+a x)^{n}$ can be written as $64+b x+c x^{2}$, where $n, a, b$ and $c$ are constants.
(a) Find the value of $n$.
(b) Show that $5 b^{2}=768 c$.
(c) Given that $b=12$, find the exact value of $a$ and of $c$.


The diagram shows a circle, centre $O$, radius 5 cm . The lines $A O B$ and $C O D$ are diameters of this circle. The line $A C$ has length 6 cm .
(a) Show that angle $A O C=1.287$ radians, correct to 3 decimal places.
(b) Find the perimeter of the shaded region.
(c) Find the area of the shaded region.

9 (a) Find the coordinates of the stationary points on the curve $y=(2 x+1)(x-3)^{2}$. Give your answers in exact form.
(b) On the axes below, sketch the graph of $y=\left|(2 x+1)(x-3)^{2}\right|$, stating the coordinates of the points where the curve meets the axes.

(c) Hence write down the value of the constant $k$ such that $\left|(2 x+1)(x-3)^{2}\right|=k \quad$ has exactly 3 distinct solutions.

10 (a) Jess runs on 5 days each week to prepare for a race.
In week 1 , every run is 2 km .
In week 2 , every run is 2.5 km .
In week 3 , every run is 3 km .
Jess increases the distance of the run by 0.5 km every week.
(i) Find the week in which Jess runs 16 km on each of the 5 days.
(ii) Find the total distance Jess will have run by the end of week 8 .
(b) Kyle also runs on 5 days each week to prepare for a race.

In week 1 , every run is 2 km .
In week 2, every run is 2.5 km .
In week 3 , every run is 3.125 km .
The distances he runs each week form a geometric progression.
(i) Find the common ratio of the geometric progression.
(ii) Find the first week in which Kyle will run more than 16 km on each of the 5 days.
(iii) Find the total distance Kyle will have run by the end of week 8.

11 (a) Solve the equation $3 \operatorname{cosec}^{2} \theta-5=5 \cot \theta$ for $0^{\circ} \leqslant \theta \leqslant 180^{\circ}$.
(b) Solve the equation $\sin \left(\phi+\frac{\pi}{3}\right)=-\frac{1}{2}$, where $\phi$ is in radians and $-\pi \leqslant \phi \leqslant \pi$. Give your answers in terms of $\pi$.

To avoid the issue of disclosure of answer-related information to candidates, all copyright acknowledgements are reproduced online in the Cambridge Assessment International Education Copyright Acknowledgements Booklet. This is produced for each series of examinations and is freely available to download at www.cambridgeinternational.org after the live examination series.

Cambridge Assessment International Education is part of the Cambridge Assessment Group. Cambridge Assessment is the brand name of the University of Cambridge Local Examinations Syndicate (UCLES), which itself is a department of the University of Cambridge.

