Cambridge IGCSE[™]

CANDIDATE NAME					
CENTRE NUMBER			CANDIDATE NUMBER		

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ADDITIONAL MATHEMATICS

0606/11

Paper 1 October/November 2021

2 hours

You must answer on the question paper.

No additional materials are needed.

INSTRUCTIONS

- Answer all questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do not use an erasable pen or correction fluid.
- Do not write on any bar codes.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

INFORMATION

- The total mark for this paper is 80.
- The number of marks for each question or part question is shown in brackets [].

This document has 16 pages.

Mathematical Formulae

1. ALGEBRA

Quadratic Equation

For the equation $ax^2 + bx + c = 0$,

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Binomial Theorem

$$(a+b)^n = a^n + \binom{n}{1}a^{n-1}b + \binom{n}{2}a^{n-2}b^2 + \dots + \binom{n}{r}a^{n-r}b^r + \dots + b^n$$

where *n* is a positive integer and $\binom{n}{r} = \frac{n!}{(n-r)!r!}$

Arithmetic series $u_n = a + (n-1)d$

$$S_n = \frac{1}{2}n(a+l) = \frac{1}{2}n\left\{2a + (n-1)d\right\}$$

Geometric series $u_n = ar^{n-1}$

$$S_n = \frac{a(1-r^n)}{1-r} \ (r \neq 1)$$

$$S_{\infty} = \frac{a}{1-r} \ (|r| < 1)$$

2. TRIGONOMETRY

Identities

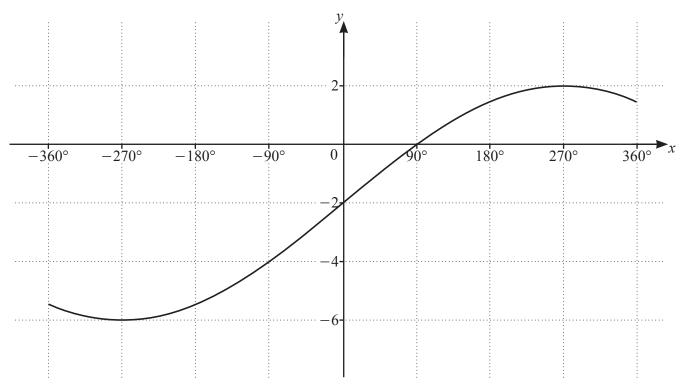
$$\sin^2 A + \cos^2 A = 1$$
$$\sec^2 A = 1 + \tan^2 A$$
$$\csc^2 A = 1 + \cot^2 A$$

Formulae for $\triangle ABC$

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$
$$a^2 = b^2 + c^2 - 2bc \cos A$$
$$\Delta = \frac{1}{2}bc \sin A$$

3

1



The diagram shows the graph of $y = a \sin \frac{x}{b} + c$ for $-360^{\circ} \le x \le 360^{\circ}$, where a, b and c are integers.

(a) Write down the period of $a \sin \frac{x}{b} + c$. [1]

(b) Find the value of a, of b and of c. [3]

2	Points A and C have coordinates $(-4,6)$ and $(2,18)$ respectively. The point B lies on the line AC such
	that $\overrightarrow{AB} = \frac{2}{3} \overrightarrow{AC}$.

(a) Find the coordinates of B.

[2]

(b) Find the equation of the line l, which is perpendicular to AC and passes through B. [2]

(c) Find the area enclosed by the line *l* and the coordinate axes.

[2]

3 (a) Find the vector which has magnitude 39 and is in the same direction as $\begin{pmatrix} 12 \\ -5 \end{pmatrix}$. [2]

(b) Given that $\mathbf{a} = \begin{pmatrix} 2 \\ -1 \end{pmatrix}$ and $\mathbf{b} = \begin{pmatrix} -4 \\ 5 \end{pmatrix}$, find the constants λ and μ such that $5\mathbf{a} + \lambda \begin{pmatrix} 4 \\ 6 \end{pmatrix} = \mu \mathbf{b}$. [4]

4 (a) Given that
$$\frac{q^{-2}\sqrt{pr}}{\sqrt[3]{r}(pq)^{-3}} = p^a q^b r^c$$
, find the value of each of the constants a , b and c . [3]

(b) Solve the equation
$$3x^{\frac{4}{5}} - 8x^{\frac{2}{5}} + 5 = 0$$
. [4]

5	The polynomial	$p(x) = ax^3 + bx^2 + 6x + 4,$	where a and b are integers.	is divisible by $x-2$. When
	p'(x) is divided b	by $x+1$ the remainder is -7 .		

(a) Find the value of a and of b.

[5]

[2]

(b) Using your answers to **part** (a), find the remainder when p''(x) is divided by x.

8

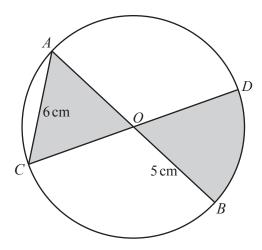
A curve with equation y = f(x) is such that $\frac{d^2y}{dx^2} = 6e^{3x} + 4x$. The curve has a gradient of 5 at the point $\left(0, \frac{5}{3}\right)$. Find f(x).

- 7 The first three terms, in ascending powers of x, in the expansion of $(2+ax)^n$ can be written as $64+bx+cx^2$, where n, a, b and c are constants.
 - (a) Find the value of n. [1]
 - **(b)** Show that $5b^2 = 768c$. [4]

(c) Given that b = 12, find the exact value of a and of c. [2]

[2]

8



The diagram shows a circle, centre O, radius 5 cm. The lines AOB and COD are diameters of this circle. The line AC has length 6 cm.

(a) Show that angle AOC = 1.287 radians, correct to 3 decimal places. [2]

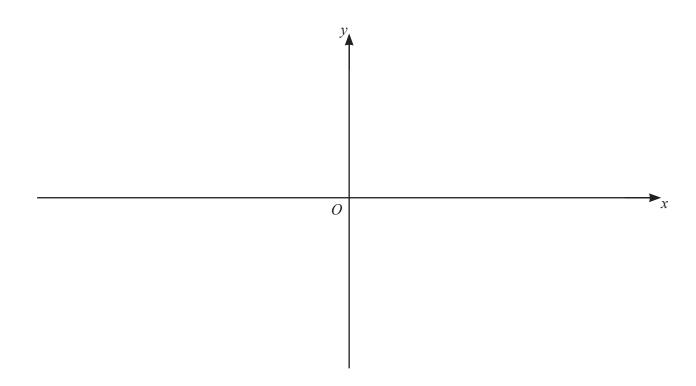
(b) Find the perimeter of the shaded region.

11

(c) Find the area of the shaded region. [3]

9 (a) Find the coordinates of the stationary points on the curve $y = (2x+1)(x-3)^2$. Give your answers in exact form. [4]

(b) On the axes below, sketch the graph of $y = |(2x+1)(x-3)^2|$, stating the coordinates of the points where the curve meets the axes. [4]



(c) Hence write down the value of the constant k such that $\left| (2x+1)(x-3)^2 \right| = k$ has exactly 3 distinct solutions. [1]

10	(a)	In v In v In v	s runs on 5 days each week to prepare for a race. week 1, every run is 2 km. week 2, every run is 2.5 km. week 3, every run is 3 km. s increases the distance of the run by 0.5 km every week.			
		(i)	Find the week in which Jess runs 16km on each of the 5 days.	[2]		

(ii) Find the total distance Jess will have run by the end of week 8. [3]

(b)	Kyle also runs on 5 days each week to prepare for a race. In week 1, every run is 2 km. In week 2, every run is 2.5 km. In week 3, every run is 3.125 km. The distances he runs each week form a geometric progression.						
	(i)	Find the common ratio of the geometric progression.	[1]				
	(ii)	Find the first week in which Kyle will run more than 16 km on each of the 5 days.	[3]				
	(iii)	Find the total distance Kyle will have run by the end of week 8.	[3]				

11 (a) Solve the equation
$$3\csc^2\theta - 5 = 5\cot\theta$$
 for $0^\circ \le \theta \le 180^\circ$. [4]

(b) Solve the equation $\sin\left(\phi + \frac{\pi}{3}\right) = -\frac{1}{2}$, where ϕ is in radians and $-\pi \le \phi \le \pi$. Give your answers in terms of π .

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