

5-Aug-24

Objective: Complete **iGCSE questions** on statistical questions.

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(c) Use your graph to find

(i) the median mass,

(ii) the interquartile range.

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| | | | | |
|----------|----------------|----|----------|--|
| 3 | (a) (i) | 60 | 1 | |
| | (ii) | 8 | 2 | B1 for [lq =] 56 or [uq =] 64 |
| | (iii) | 12 | 2 | M1 for 188 seen |

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| | | | | |
|----------|------------|-----------------------|----------|--|
| 6 | (a) | 166 or 165.6 to 165.7 | 2 | M1 for correct use of mid-pts at least 157.5, 162.5, 167.5, 172.5, 182.5) |
|----------|------------|-----------------------|----------|--|


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- 11** A farmer sorts the grapefruit he grows into sizes, according to their diameter. The diameters, d cm, of 170 grapefruit are shown in the table.

| | | | | | |
|---|-------------------------------------|-----------------|------------------|------------------|-------------------|
|  | Size | Small | Medium | Large | Very Large |
| | Diameter (d cm) | $9 < d \leq 10$ | $10 < d \leq 12$ | $12 < d \leq 14$ | $14 < d \leq 17$ |
| | Frequency | 10 | 50 | 65 | 45 |

- (a)** Calculate an estimate of the mean diameter of the grapefruit.

.....

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| Question | Answer | Marks | Partial Marks |
|----------|------------------------|-------|---|
| 11(a) | 12.9 or 12.86 to 12.87 | 2 | M1 for evidence of at least three mid-inter values 9.5, 11, 13, 15.5 soi by 95, 550, 845, 697.5 or 2187.5 |

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- 3 (a) 12 students take part in a quiz.
The table shows the number of correct answers given by each student.

| Student | A | B | C | D | E | F | G | H | I | J | K | L |
|---------------------------|---|---|---|---|---|---|---|---|---|----|---|---|
| Number of correct answers | 7 | 6 | 9 | 5 | 6 | 4 | 7 | 8 | 4 | 10 | 9 | 3 |

Find

- (i) the median,

.....

- (ii) the lower quartile,

.....

- (iii) the number of students with a smaller number of correct answers than the lower quartile.

.....



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| | | | |
|-----------|-----|---|--|
| 3(a)(i) | 6.5 | 1 | |
| 3(a)(ii) | 4.5 | 1 | |
| 3(a)(iii) | 3 | 1 | |

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- 4 (a) The mass, x grams, of each of 100 oranges is found.
The results are shown in the table.

| Mass (x grams) | Frequency |
|--------------------|-----------|
| $0 < x \leq 100$ | 4 |
| $100 < x \leq 140$ | 14 |
| $140 < x \leq 180$ | 22 |
| $180 < x \leq 250$ | 35 |
| $250 < x \leq 300$ | 25 |

- (i) Calculate an estimate of the mean mass of the oranges.

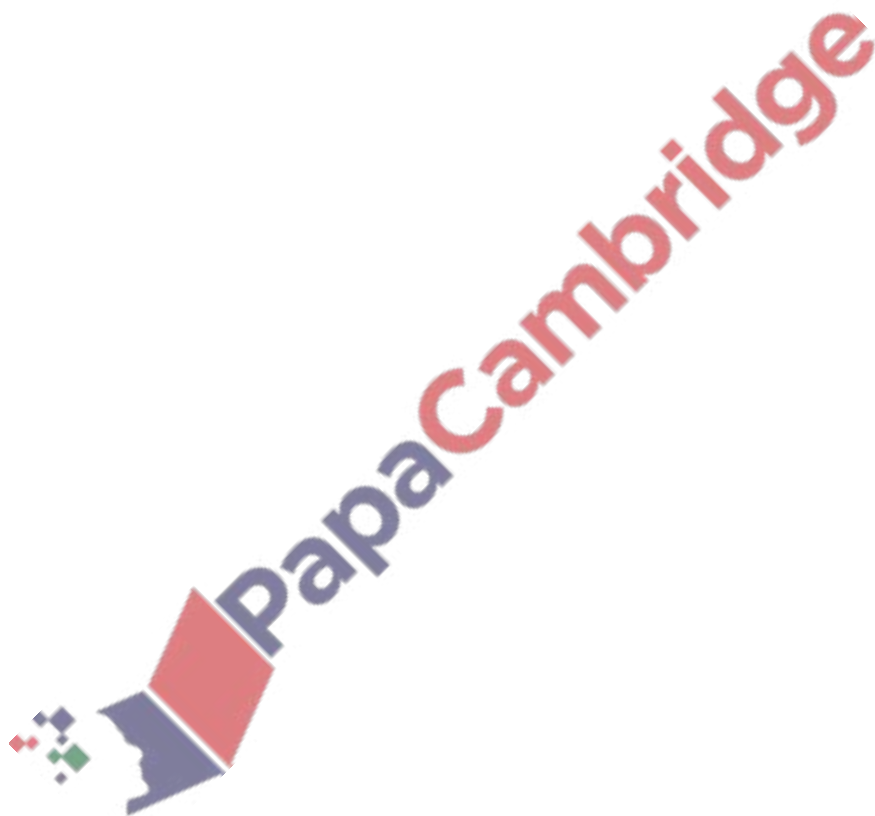
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| | | | |
|---------|-----|---|------------------------------------|
| 4(a)(i) | 198 | 2 | M1 for 3 or more 50, 120, 160, 210 |
|---------|-----|---|------------------------------------|

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| Question | Answer | Marks | Partial Marks |
|----------|------------------------|-------|---|
| 1(a) | 10 | 1 | |
| 1(b) | 6 nfw | 2 | B1 for 17 or 11 seen |
| 1(c) | 10 | 1 | |
| 1(d) | 15 | 1 | |
| 1(e) | 14.5 or 14.51 to 14.52 | 2 | M1 for $\sum xf$ soi by e.g. 450 |
| 1(f) | It is the smallest oe | 1 | |



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| | | | |
|-----------|------------------------|---|--|
| 4(a) | 27.7 or 27.70 to 27.71 | 2 | M1 for at least 3 midpoints soi |
| 4(b) | Correct cf curve | 5 | Curve/polygon through (10, 0), (20, 44), (30, 76), (35, 100), (40, 114), (50, 120) or B4 for curve through 5 or 6 points 7 points with no curve or B3 for 'correct curve' through all consistent points in interval or B2 for all correct cfs or B1 for 4 or 5 correct cfs. If 0 scored SC1 for any cumulative frequency diagram. |
| 4(c)(i) | 26 to 28 | 1 | Dep on increasing curve FT |
| 4(c)(ii) | 9 to 11.5 | 2 | Dep on increasing curve FT B1 for $lq = 22$ to 23.5 or $uq = 32.5$ to |
| 4(c)(iii) | 10 to 15 | 2 | Dep on increasing curve FT B1 for 105 to 110 seen |

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- 9 240 students take part in a charity run.
The table shows information about the times, t minutes, taken to complete the run.

| | | | | |
|---------------------|------------------|------------------|------------------|------------------|
| Time (t minutes) | $20 < t \leq 40$ | $40 < t \leq 50$ | $50 < t \leq 55$ | $55 < t \leq 60$ |
| Number of students | 20 | 70 | 120 | 30 |

- (a) Write down the time interval that contains the median.

..... $< t \leq$

- (b) Calculate an estimate of the mean.

.....

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| | | | |
|------|------------------|---|--|
| 9(a) | $50 < t \leq 55$ | 1 | Allow e.g. 50 to 55 |
| 9(b) | 50 | 2 | M1 for at least three of 30, 45, 52.. |

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| Question | Answer | Marks | Partial Marks |
|----------|--------|-------|---|
| 1(a) | 6 | 1 | |
| 1(b) | 10 | 1 | |
| 1(c) | 6 | 1 | |
| 1(d) | 4 | 2 | B1 for LQ = 4 or UQ = 8 |
| 1(e) | 5.55 | 2 | M1 for attempt at $\sum fx$ (3 or terms correct) |

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| | | | |
|---------|----|---|------------------------|
| 6a(i) | 74 | 1 | |
| 6a(ii) | 18 | 2 | B1 for 64 or 82 |
| 6a(iii) | 38 | 2 | B1 for 82 |

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| | | | |
|-----------|--------------------------|---|---|
| 6(b)(i) | Correct graph | 3 | B1 for minimum at (10, h) where $h < 30$, lq and median correct B1 for uq correct B1 for maximum correct |
| 6(b)(ii) | Answer in range 50 to 60 | 2 | B1 for 74 or 14 to 24 |
| 6(b)(iii) | [A is] steeper oe | 1 | |

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| | | | |
|------|--|---|---|
| 4(a) | 39.8 or 39.81 to 39.82 | 2 | M1 for at least 5 correct mid-points |
| 4(b) | [41], 73, 117, 167, 232, 280, [300] | 1 | |
| | In parts (c), (d) and (e), marks can only be earned with an increasing curve | | |
| 4(c) | Correct curve (10, 41) (20, 73) (30, 117) (40, 167) (60, 232) (80, 280) (100, 300) | 3 | M1 for horizontal plot correct M1 for at least 6 vertical plots from table correct |

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| | | | |
|----------|----------|---|---|
| 4(d)(i) | 35 to 38 | 1 | |
| 4(d)(ii) | 35 to 39 | 2 | B1 for [UQ =] 56 to 59 or [LQ =] 20 to 21 |
| 4(e) | 46 to 50 | 2 | B1 for 195 or 105 seen |

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3 The table shows the masses of 30 sheep.

| | | | | |
|--------------|------------------|-------------------|--------------------|--------------------|
| Mass, m kg | $60 < m \leq 80$ | $80 < m \leq 100$ | $100 < m \leq 120$ | $120 < m \leq 140$ |
| Frequency | 8 | 3 | 12 | 7 |

(a) Write down the modal group.

.....

(b) Write down the class which contains the lower quartile.

.....

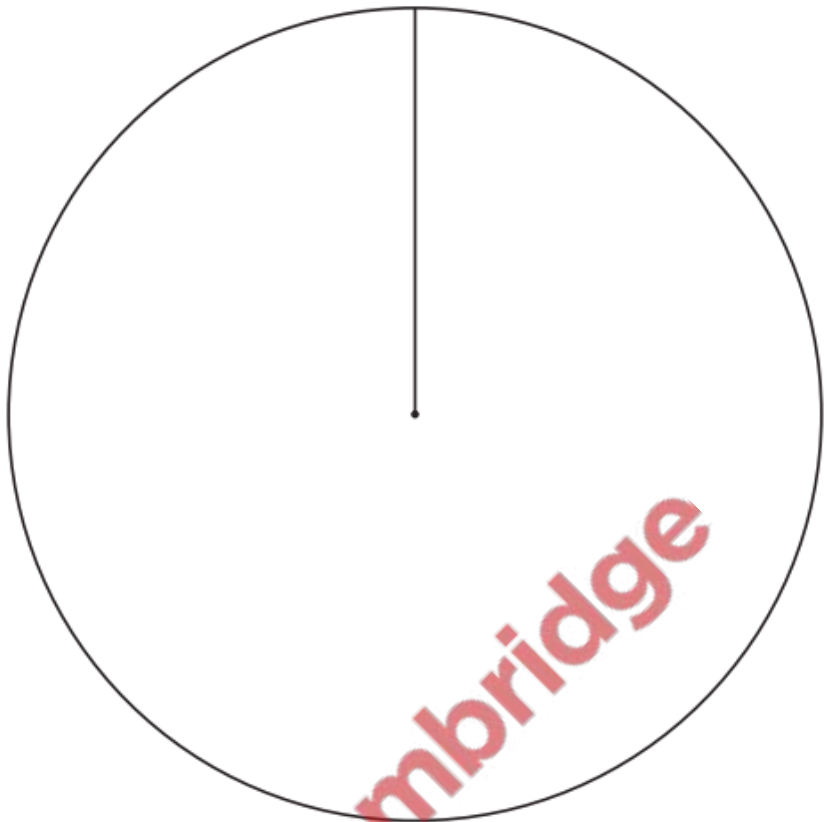
(c) Maria says that the range of masses is 80 kg.

Explain why she is incorrect.

.....

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(d) Draw an accurate pie chart to show this information.



| | | | |
|------|-----------------------|---|--|
| 3(a) | $100 < m \leq 120$ | 1 | |
| 3(b) | $60 < m \leq 80$ | 1 | |
| 3(c) | Any correct statement | 1 | |

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| | | | |
|------|---|---|--|
| 3(d) | Correct labelled pie chart (labels indicating masses) | 4 | B3 for pie chart with all angles correct or B2 for pie chart with two angles correct or B1 for 2 correct angles calculated B1 for correct labels on sectors |
|------|---|---|--|

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| | | | |
|------|-------------------------|---|--|
| 5(a) | 178 or 178.4 to 178.5 | 2 | M1 for evidence of mid-values |
| 5(b) | $[x =] 7$ $[y =] 18$ | 3 | B2 for $y = 18$ or M1 for $([x \times 0] + y [\times 1] + 30 \times 2 + 45 \times 3) \div 100$ If 0 scored SC1 for <i>their</i> $x + \text{their } y = 25$ |

- 5 (a) There are 200 students in a school.
The table shows information about their heights, h cm.

| | | | | | | |
|----------------|--------------------|--------------------|--------------------|--------------------|--------------------|--------------------|
| Height, h cm | $150 < h \leq 165$ | $165 < h \leq 170$ | $170 < h \leq 175$ | $175 < h \leq 180$ | $180 < h \leq 190$ | $190 < h \leq 200$ |
| Frequency | 7 | 17 | 43 | 64 | 49 | 20 |

Calculate an estimate of the mean height.

..... cm [2]

- (b) A biased die in the shape of a cube is numbered 0, 1, 1, 2, 3 and 3.
It is rolled 100 times.
The table shows the results.

| | | | | |
|-----------|-----|-----|----|----|
| Score | 0 | 1 | 2 | 3 |
| Frequency | x | y | 30 | 45 |

The mean score is 2.13 .

Find the value of x and the value of y .

$x =$

$y =$ [3]



(d) Use your curve in **part (c)** to find an estimate for

(i) the median mark,

.....

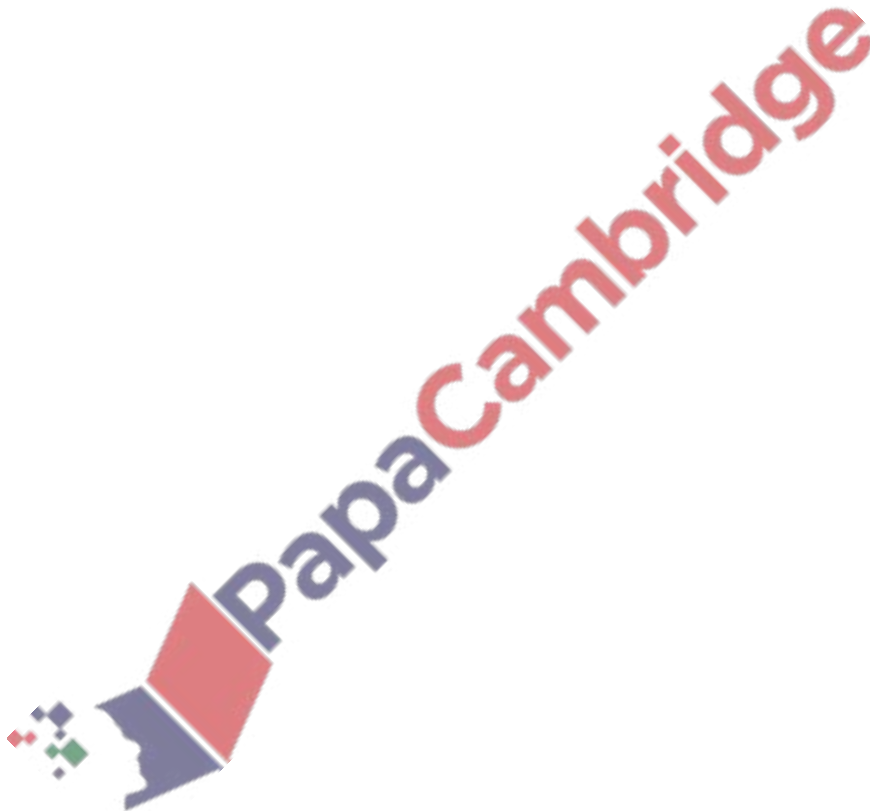
(ii) the interquartile range.

.....

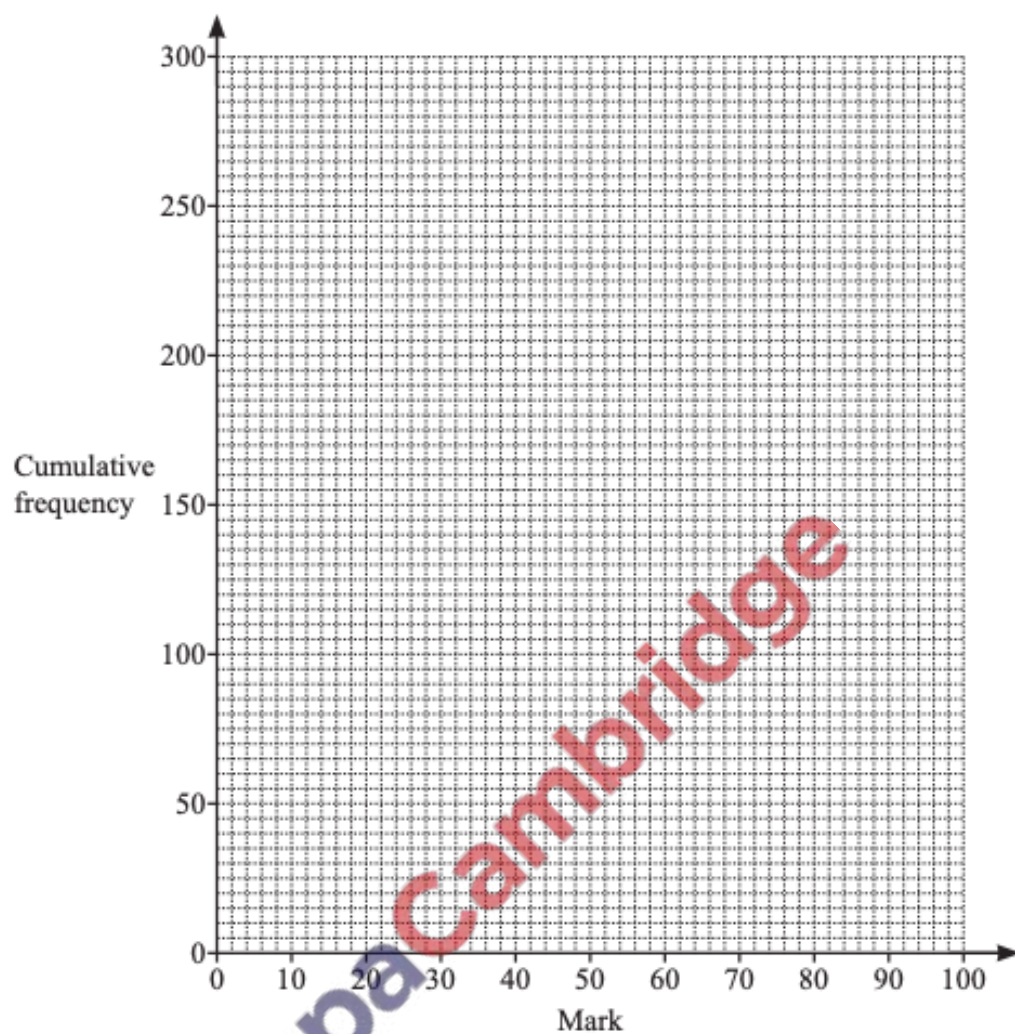
(e) 35% of the students pass the test.

Use your curve in **part (c)** to find an estimate of the minimum mark needed to pass.

.....



(c) On the grid, draw a cumulative frequency curve.



[3]

- 4 The marks, x , of 300 students in a chemistry test are shown in the table.

| Mark (x) | Frequency |
|-------------------|-----------|
| $0 < x \leq 10$ | 41 |
| $10 < x \leq 20$ | 32 |
| $20 < x \leq 30$ | 44 |
| $30 < x \leq 40$ | 50 |
| $40 < x \leq 60$ | 65 |
| $60 < x \leq 80$ | 48 |
| $80 < x \leq 100$ | 20 |

- (a) Calculate an estimate of the mean mark.

..... [2]

- (b) Complete the cumulative frequency table.

| Mark (x) | Cumulative frequency |
|--------------|----------------------|
| $x \leq 10$ | 41 |
| $x \leq 20$ | |
| $x \leq 30$ | |
| $x \leq 40$ | |
| $x \leq 60$ | |
| $x \leq 80$ | |
| $x \leq 100$ | 300 |

[1]

(b) The table gives some information about 120 similar plants in location B.

| Minimum height (cm) | Lower quartile (cm) | Median (cm) | Interquartile range (cm) | Range (cm) |
|------------------------|------------------------|----------------|-----------------------------|---------------|
| 10 | 34 | 50 | 28 | 90 |

- (i) On the grid opposite, draw the cumulative frequency curve for the heights of the plants in location B.
- (ii) Use the curves to estimate how many **more** plants had heights of over 70 cm in location B than in location A.

- (iii) The heights of the plants in location A are more consistent than the heights of the plants in location B.

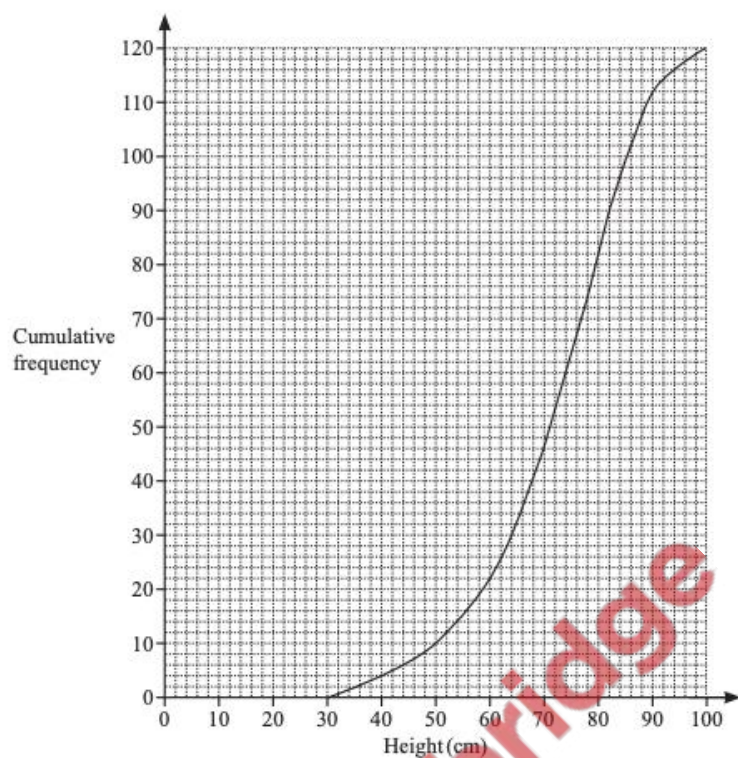
By comparing the **shapes** of the curves, explain how you know this is true.

.....

.....



- 6 The cumulative frequency graph shows the heights, in centimetres, of 120 plants in location A.



- (a) Use the graph to estimate

(i) the median,

..... cm [1]

(ii) the interquartile range,

..... cm [2]

(iii) the number of plants over 80 cm in height.

..... [2]



- 1 A class of 40 students complete a science test.
The table shows the marks of the 40 students.

| | | | | | | | | | | | |
|--------------------|---|---|---|---|---|---|---|---|---|---|----|
| Mark | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| Number of students | 1 | 1 | 2 | 5 | 5 | 5 | 6 | 3 | 9 | 2 | 1 |

- (a) Write down the mode.

..... [1]

- (b) Work out the range.

..... [1]

- (c) Find the median.

..... [1]

- (d) Find the interquartile range.

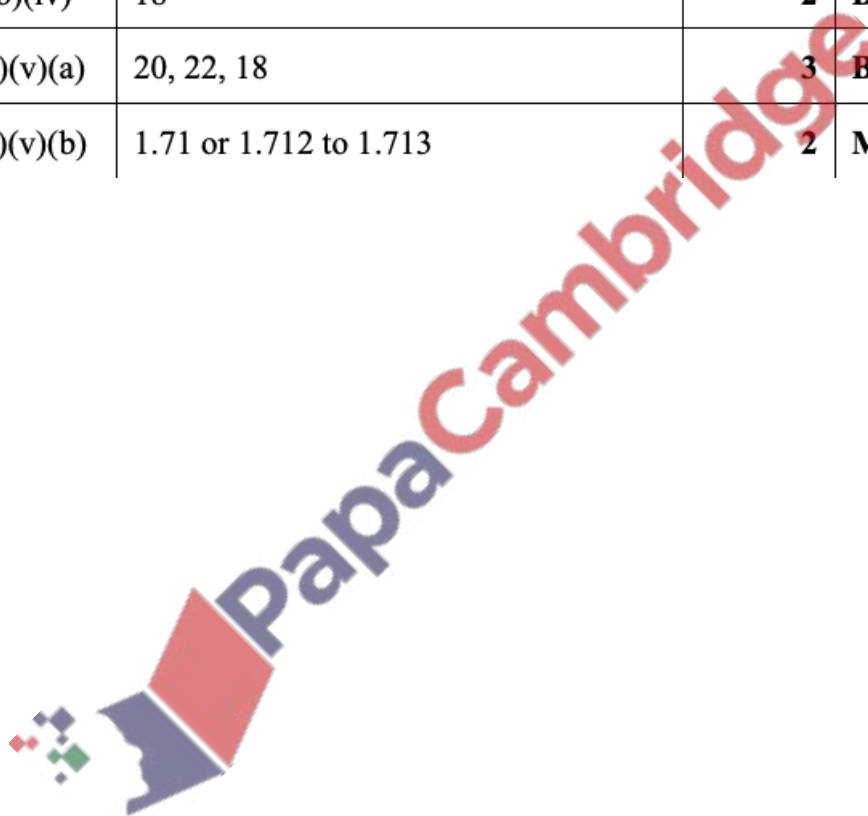
..... [2]

- (e) Calculate the mean.

..... [2]



| | | | |
|------------|------------------------|---|------------------------------|
| 2(a)(i) | 5 | 1 | |
| 2(a)(ii) | 7.9 | 1 | |
| 2(a)(iii) | 8 | 1 | |
| 2(a)(iv) | 9 | 1 | |
| 2(b)(i) | 1.5 | 1 | |
| 2(b)(ii) | 1 | 1 | |
| 2(b)(iii) | 1.4 | 1 | |
| 2(b)(iv) | 18 | 2 | B1 for 102 stated |
| 2(b)(v)(a) | 20, 22, 18 | 3 | B1 for each |
| 2(b)(v)(b) | 1.71 or 1.712 to 1.713 | 2 | M1 for mid-values soi |



(i) Find the median.

..... kg [1]

(ii) Find the lower quartile.

..... kg [1]

(iii) Find the interquartile range.

..... kg [1]

(iv) Find the number of parcels with a mass of more than 3 kg.

..... [2]

(v) (a) Use the cumulative frequency curve to complete the frequency table.

| Mass (m kg) | $0 < m \leq 1$ | $1 < m \leq 1.5$ | $1.5 < m \leq 2$ | $2 < m \leq 3$ | $3 < m \leq 4$ |
|----------------|----------------|------------------|------------------|----------------|----------------|
| Frequency | 30 | 30 | | | |

[3]

(b) Use the frequency table to calculate an estimate of the mean.

..... kg [2]



- 2 (a) These are Tom's ten homework marks.

8 7 10 8 9 5 8 10 6 8

Find

- (i) the range,

..... [1]

- (ii) the mean,

..... [1]

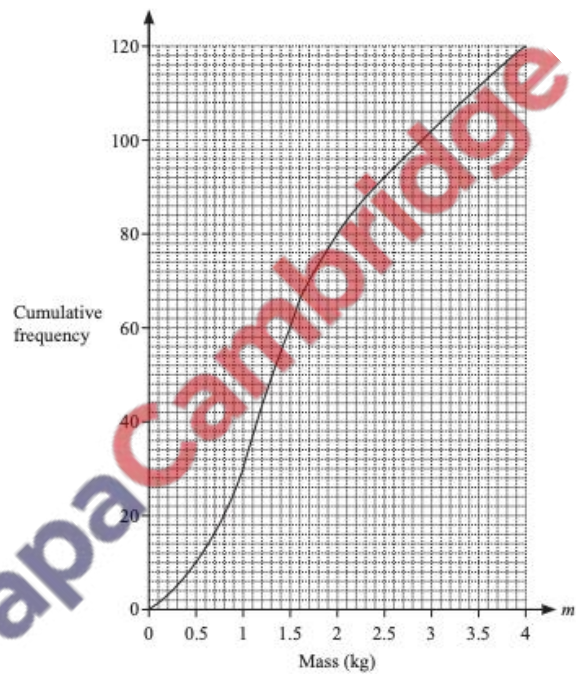
- (iii) the median,

..... [1]

- (iv) the upper quartile.

..... [1]

- (b) The mass, m kg, of each of 120 parcels is recorded.
The cumulative frequency curve shows the results.



(c) Use your cumulative frequency curve to estimate

(i) the median height,

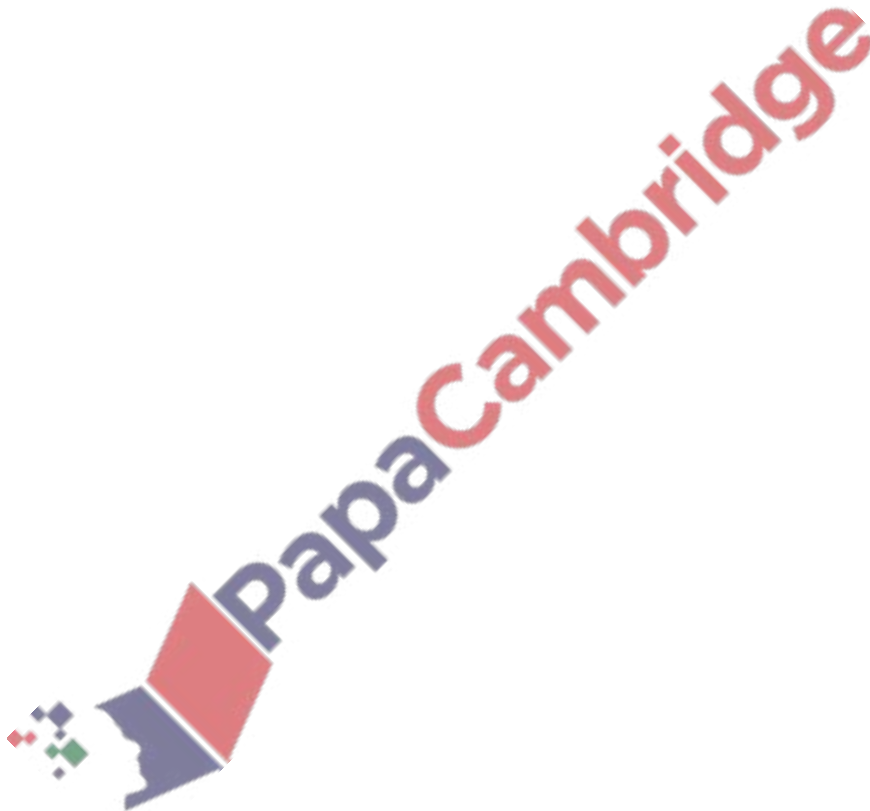
.....

(ii) the interquartile range,

.....

(iii) the number of plants with a height of more than 37 cm.

.....



- 4 Rani planted some seeds in her garden.
After two months she measured the heights, h cm, of each of 120 plants.

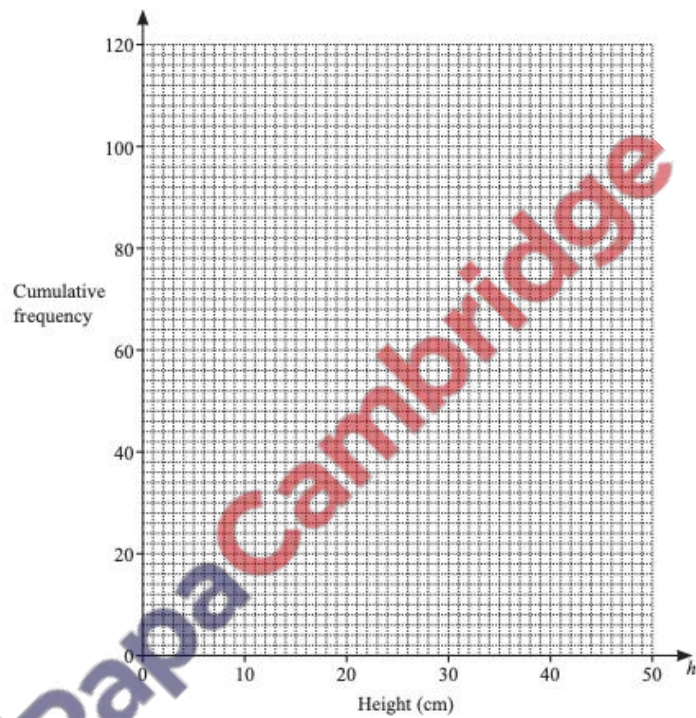
The results are shown in the table.

| Height (h cm) | $0 < h \leq 10$ | $10 < h \leq 20$ | $20 < h \leq 25$ | $25 < h \leq 30$ | $30 < h \leq 35$ | $35 < h \leq 40$ | $40 < h \leq 50$ |
|------------------|-----------------|------------------|------------------|------------------|------------------|------------------|------------------|
| Frequency | 0 | 16 | 28 | 32 | 24 | 14 | 6 |

- (a) Calculate an estimate of the mean height.

..... cm [2]

- (b) Draw a cumulative frequency curve for this information.



[5]

- 1 Gunter keeps chickens.
He records the number of eggs he collects each day for 31 days.
These are the results.

| | | | | | | | | | | | |
|----------------|----|----|----|----|----|----|----|----|----|----|----|
| Number of eggs | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
| Number of days | 5 | 3 | 2 | 3 | 2 | 3 | 2 | 4 | 4 | 1 | 2 |

- (a) Write down the range of the numbers of eggs.

..... [1]

- (b) Find the inter-quartile range.

..... [2]

- (c) Write down the mode.

..... [1]

- (d) Find the median.

..... [1]

- (e) Find the mean.

..... [2]

- (f) Explain why the mode is not the best measure of average to represent these results.

..... [1]



| Question | Answer | Marks | Partial Marks |
|-----------|---|-------|--|
| 4(a)(i) | $\begin{array}{r l} 1 & 7\ 8\ 9\ 9 \\ \hline 2 & 0\ 1\ 1\ 1\ 1\ 2\ 2\ 3\ 4\ 5 \\ & \text{e.g. } 2 3 = 23 \end{array}$ | 3 | B1 for each row B1 for key |
| 4(a)(ii) | 21 19 | 2 | B1 for each |
| 4(a)(iii) | 102.8 to 102.9 | 2 | M1 for $\frac{4}{14}$ oe or $\frac{360}{14}$ oe |
| 4(b)(i) | 2.4 | 1 | |
| 4(b)(ii) | 0.9 | 2 | B1 for 3 or 2.1 seen |
| 4(b)(iii) | 20 | 2 | M1 for 180 seen |
| 4(c)(i) | 253.125 or 253.13 or 253.1 or 253 | 2 | M1 for evidence of at least two mi 150, 225, 325 soi by e.g. 50625 |



Find

(i) the median, litres

(ii) the inter-quartile range, litres

(iii) the number of students who estimated more than 3.5 litres.
.....

- (c) 200 students estimated the area, $y\text{m}^2$, of a field.
The table shows the results.

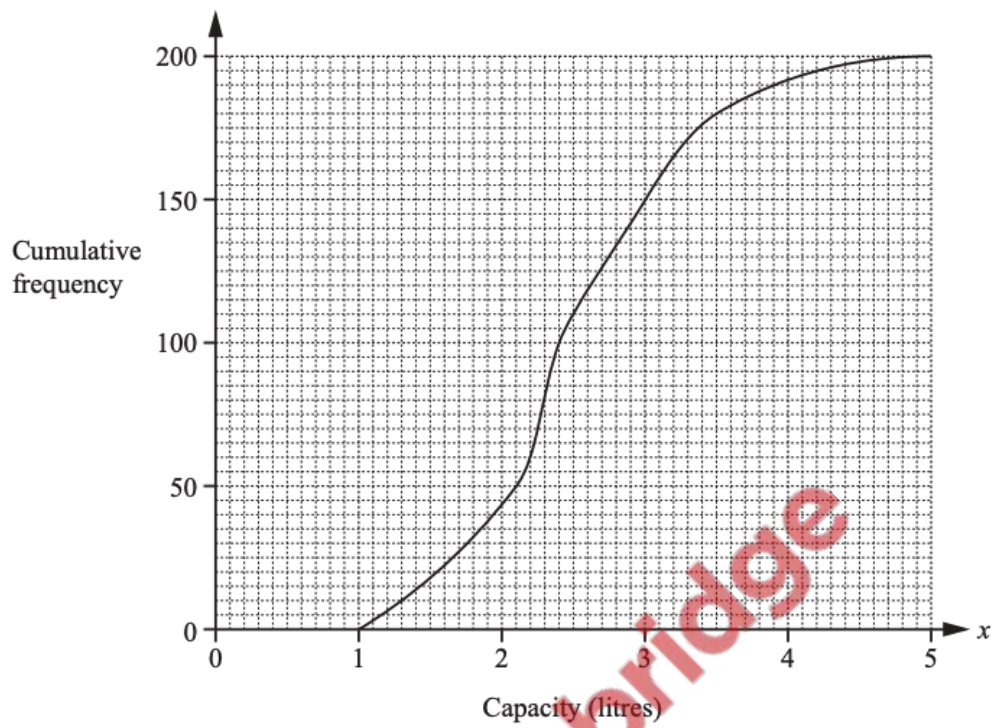
| Area ($y\text{m}^2$) | $100 < y \leq 200$ | $200 < y \leq 250$ | $250 < y \leq 400$ |
|------------------------|--------------------|--------------------|--------------------|
| Frequency | 25 | 100 | 75 |

- (i) Calculate an estimate of the mean.

..... m



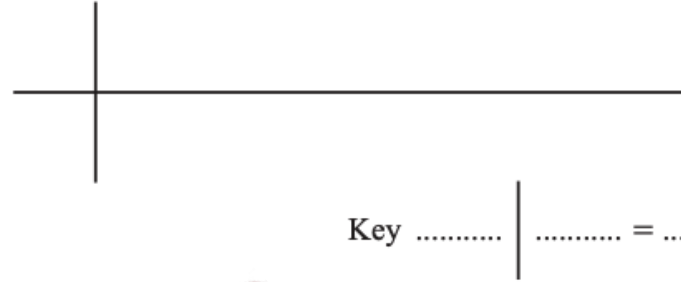
- (b) 200 students estimated the capacity, x litres, of a container. The results are shown in the cumulative frequency curve.



- 4 (a) The list shows the temperature, in degrees Celsius, at noon in Paris on each of 14 days.

| | | | | | | |
|----|----|----|----|----|----|----|
| 19 | 18 | 21 | 21 | 23 | 21 | 22 |
| 20 | 24 | 25 | 22 | 21 | 19 | 17 |

- (i) Construct an ordered stem and leaf diagram to show this information, including the key.



- (ii) Find the median and the lower quartile.

median =

lower quartile =

- (iii) Find the angle on a pie chart that represents the number of days the temperature was less than 20°C .

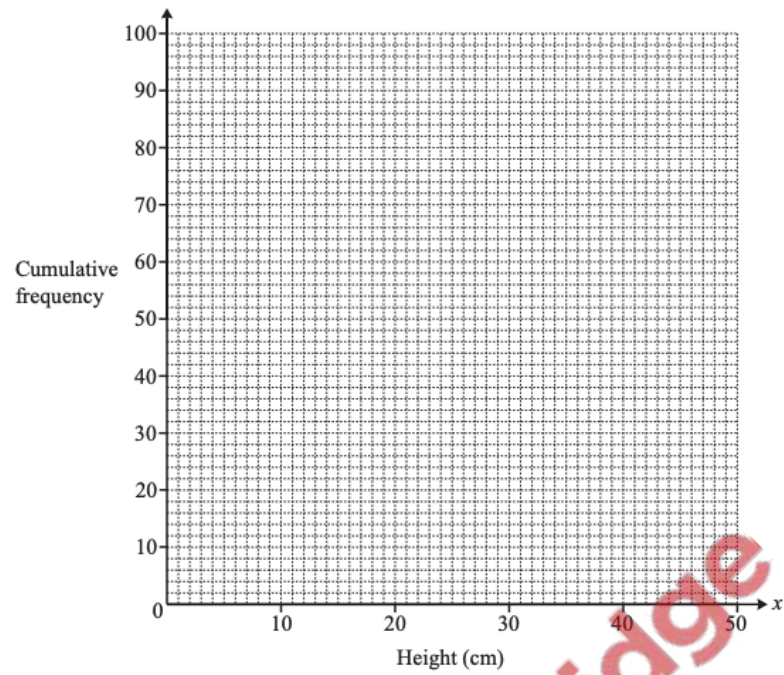
.....



| | | | |
|-----------|----------------------|---|---|
| 2(a) | 31.1 | 2 | M1 for evidence of at least 3 correct mid |
| 2(b)(i) | [7], 20, 40, 72, 100 | 1 | |
| 2(b)(ii) | Correct Graph | 3 | B1 for plotting <i>their</i> points at upper group points must be increasing vertically) B1 for 4 or 5 correct FT vertical plots (m increasing) |
| 2(c)(i) | 32.5 to 34.5 | 1 | FT <i>their</i> graph, dependent on increasing |
| 2(c)(ii) | 16.5 to 20 | 2 | FT <i>their</i> graph, dependent on increasing B1 for UQ = 40.5 to 42 or LQ = 22 to 24 or M1 for <i>their</i> UQ – <i>their</i> LQ |
| 2(c)(iii) | 3 to 4 | 3 | FT <i>their</i> graph, dependent on increasing M2 for <i>their</i> 55 th percentile (34 to 36) and 45 th percentile (31 to 33) or M1 for <i>their</i> 45th percentile (31 to 33) 55th percentile (34 to 36) or SC3 for e.g. 32 to 35 |



(ii) On the grid below, draw the cumulative frequency curve.



[3]

(c) Use your graph in **part (b)(ii)** to find estimates for

(i) the median height,

..... cm [1]

(ii) the interquartile range,

..... cm [2]

(iii) the range of heights of plants that are between the 45th and the 55th percentile.

..... cm [3]



- 2 (a) The heights, x cm, of some plants are shown in the table.

| Height (x cm) | Frequency |
|------------------|-----------|
| $0 < x \leq 10$ | 7 |
| $10 < x \leq 20$ | 13 |
| $20 < x \leq 30$ | 20 |
| $30 < x \leq 40$ | 32 |
| $40 < x \leq 50$ | 28 |

Calculate an estimate of the mean height of the plants.

..... cm [2]

- (b) (i) Complete the cumulative frequency table for the plants.

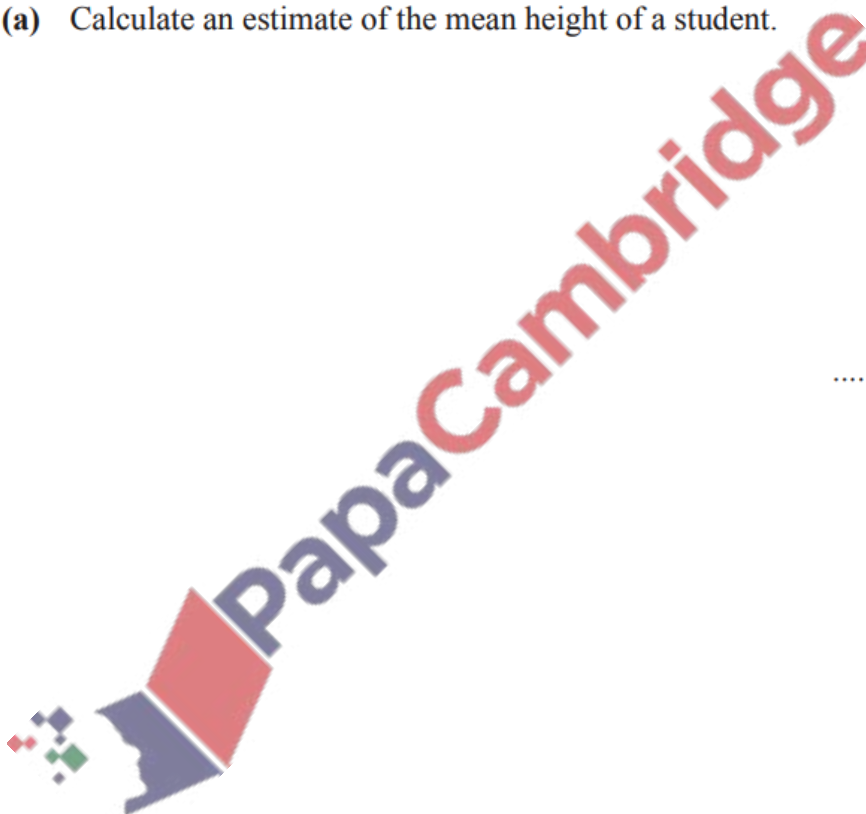
| Height (x cm) | Cumulative Frequency |
|------------------|----------------------|
| $0 < x \leq 10$ | 7 |
| $0 < x \leq 20$ | |
| $0 < x \leq 30$ | |
| $0 < x \leq 40$ | |
| $0 < x \leq 50$ | |

[1]

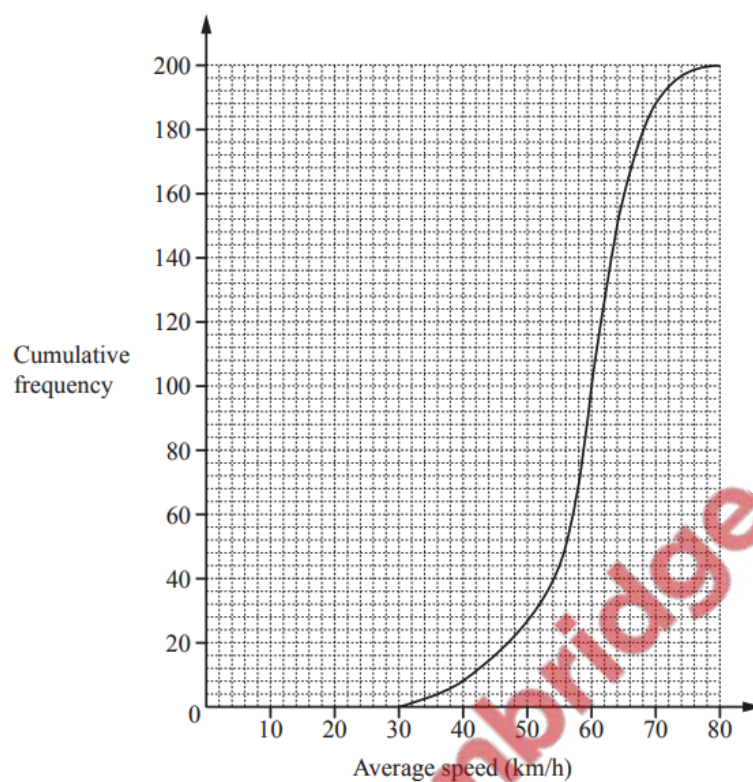
- 6 The heights of 400 students are given in the table.

| Height (h cm) | Frequency |
|--------------------|-----------|
| $145 < h \leq 155$ | 26 |
| $155 < h \leq 160$ | 66 |
| $160 < h \leq 165$ | 82 |
| $165 < h \leq 170$ | 118 |
| $170 < h \leq 175$ | 82 |
| $175 < h \leq 190$ | 26 |

- (a) Calculate an estimate of the mean height of a student.



- 3 (a) The cumulative frequency curve shows information about the average speeds of 200 cars on the same journey.



- (i) Find the median. km/h [1]
- (ii) Find the inter-quartile range. km/h [2]
- (iii) Find the number of cars with an average speed of more than 70 km/h. [2]

| Question | Answer | Mark | Part Marks |
|----------|---------------|------|---|
| 12 (a) | 63.6 | 2 | M1 for midpoints (47.5, 52.5, 57.5, 62.5, 67.5, 72.5, 77.5) so i |
| (b) | Correct Curve | 5 | B4 for 5 points correct and joined or f correct or B3 for at least 3 correct points or B2 for all correct cfs 5, 24, 58, 11 200 seen or B1 for at least 3 correct cfs or for in curve with 6 points plotted at upper bo If 0 or 1 or 2 scored, SC3 for all point but consistently translated to mid-inter lower bound. |
| (c) (i) | 63 to 64 | 1 | Dependent on increasing curve |
| (ii) | 8.5 to 10.5 | 2 | B1 for [l.qtile. =] 58.5 to 59.5 or [u.q to 69 Dependent on increasing curve |



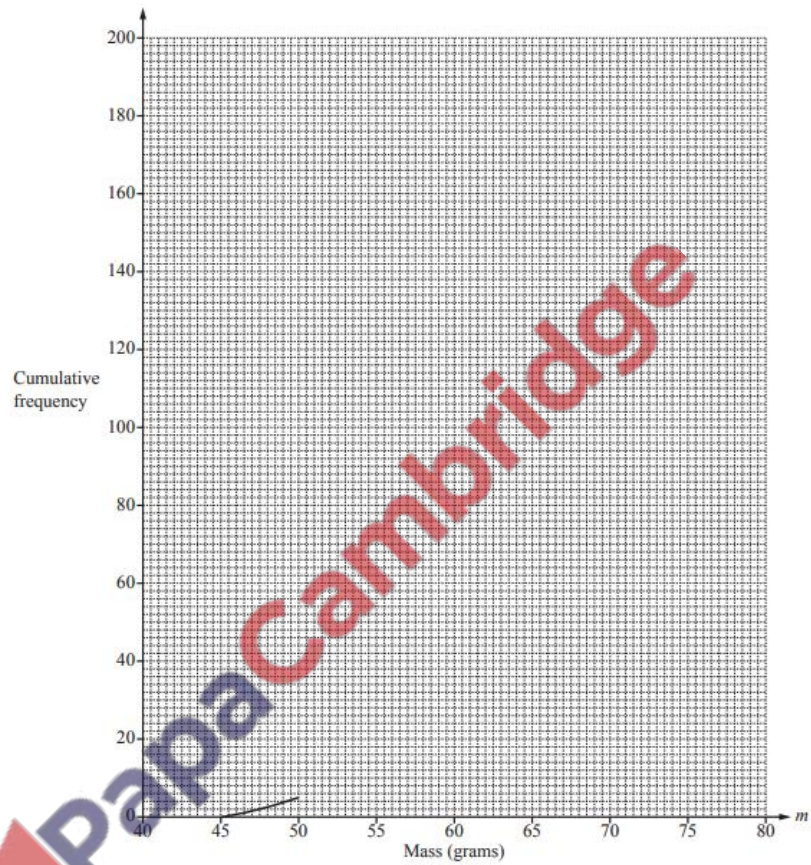
12 The table shows the masses in grams of 200 eggs.

| Mass (m grams) | $45 < m \leq 50$ | $50 < m \leq 55$ | $55 < m \leq 60$ | $60 < m \leq 65$ | $65 < m \leq 70$ | $70 < m \leq 75$ | $75 < m \leq 80$ |
|----------------------|------------------|------------------|------------------|------------------|------------------|------------------|------------------|
| Frequency | 5 | 19 | 34 | 58 | 46 | 29 | 9 |

(a) Calculate an estimate of the mean mass.

..... g [2]

(b) On the grid, complete the cumulative frequency curve for the information in the table.



[5]