



Mathematical Formulae**1. ALGEBRA***Quadratic Equation*

For the equation $ax^2 + bx + c = 0$,

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} .$$

Binomial Theorem

$$(a + b)^n = a^n + \binom{n}{1} a^{n-1} b + \binom{n}{2} a^{n-2} b^2 + \dots + \binom{n}{r} a^{n-r} b^r + \dots + b^n,$$

where n is a positive integer and $\binom{n}{r} = \frac{n!}{(n-r)!r!} .$

2. TRIGONOMETRY*Identities*

$$\sin^2 A + \cos^2 A = 1$$

$$\sec^2 A = 1 + \tan^2 A$$

$$\operatorname{cosec}^2 A = 1 + \cot^2 A$$

Formulae for ΔABC

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc \cos A$$

$$\Delta = \frac{1}{2} bc \sin A$$

- 1 Show that $\sec x - \cos x = \sin x \tan x$. [3]
- 2 A 4-digit number is formed by using four of the seven digits 2, 3, 4, 5, 6, 7 and 8. No digit can be used more than once in any one number. Find how many different 4-digit numbers can be formed if
- (i) there are no restrictions, [2]
- (ii) the number is even. [2]
- 3 The line $y = mx + 2$ is a tangent to the curve $y = x^2 + 12x + 18$. Find the possible values of m . [4]
- 4 The remainder when the expression $x^3 + kx^2 - 5x - 3$ is divided by $x - 2$ is 5 times the remainder when the expression is divided by $x + 1$. Find the value of k . [4]
- 5 Solve the simultaneous equations
- $$\log_3 a = 2 \log_3 b,$$
- $$\log_3 (2a - b) = 1. \quad [5]$$
- 6 Solve the equation $3x^3 + 7x^2 - 22x - 8 = 0$. [6]
- 7 (i) Sketch the graph of $y = |3x - 5|$, for $-2 \leq x \leq 3$, showing the coordinates of the points where the graph meets the axes. [3]
- (ii) On the same diagram, sketch the graph of $y = 8x$. [1]
- (iii) Solve the equation $8x = |3x - 5|$. [3]
- 8 (a) A function f is defined, for $x \in \mathbb{R}$, by
- $$f(x) = x^2 + 4x - 6.$$
- (i) Find the least value of $f(x)$ and the value of x for which it occurs. [2]
- (ii) Hence write down a suitable domain for $f(x)$ in order that $f^{-1}(x)$ exists. [1]
- (b) Functions g and h are defined, for $x \in \mathbb{R}$, by
- $$g(x) = \frac{x}{2} - 1,$$
- $$h(x) = x^2 - x.$$
- (i) Find $g^{-1}(x)$. [2]
- (ii) Solve $gh(x) = g^{-1}(x)$. [3]

- 9 (a) Find $\int \left(x^{\frac{1}{3}} - 3\right)^2 dx$. [3]
- (b) (i) Given that $y = x \sqrt{x^2 + 6}$, find $\frac{dy}{dx}$. [3]
- (ii) Hence find $\int \frac{x^2 + 3}{\sqrt{x^2 + 6}} dx$. [2]

- 10 A particle travels in a straight line so that, t s after passing through a fixed point O , its displacement s m from O is given by $s = \ln(t^2 + 1)$.

- (i) Find the value of t when $s = 5$. [2]
- (ii) Find the distance travelled by the particle during the third second. [2]
- (iii) Show that, when $t = 2$, the velocity of the particle is 0.8 ms^{-1} . [2]
- (iv) Find the acceleration of the particle when $t = 2$. [3]

- 11 Solve the equation

- (i) $3 \sin x - 4 \cos x = 0$, for $0^\circ \leq x \leq 360^\circ$, [3]
- (ii) $11 \sin y + 1 = 4 \cos^2 y$, for $0^\circ \leq y \leq 360^\circ$, [4]
- (iii) $\sec\left(2z + \frac{\pi}{3}\right) = -2$, for $0 \leq z \leq \pi$ radians. [4]

12 Answer only **one** of the following two alternatives.

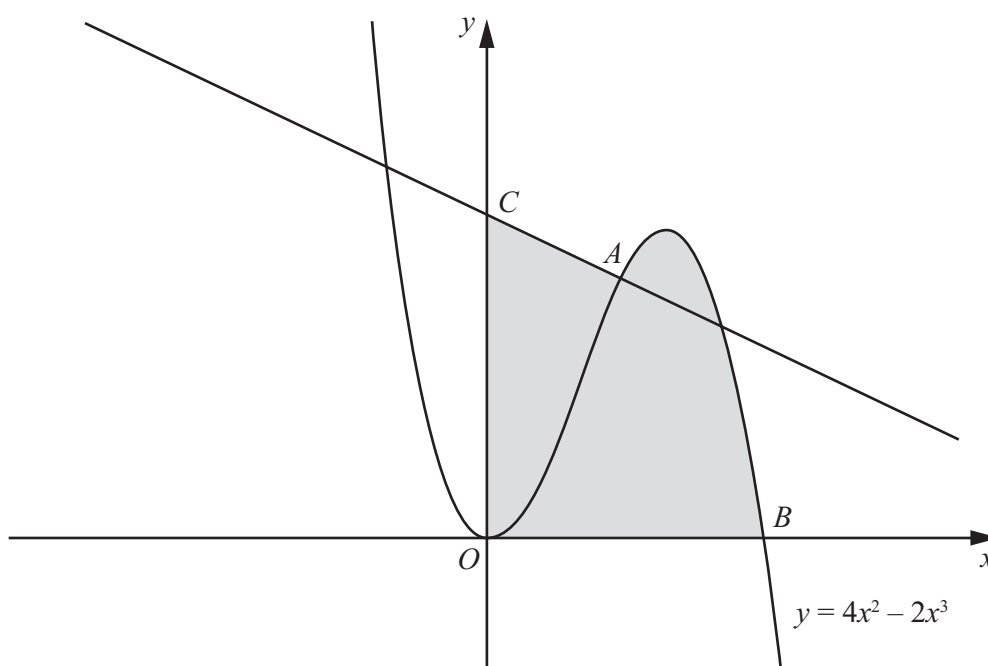
EITHER

A curve has the equation $y = A \sin 2x + B \cos 3x$. The curve passes through the point with coordinates $\left(\frac{\pi}{12}, 3\right)$ and has a gradient of -4 when $x = \frac{\pi}{3}$.

(i) Show that $A = 4$ and find the value of B . [6]

(ii) Given that, for $0 \leq x \leq \frac{\pi}{3}$, the curve lies above the x -axis, find the area of the region enclosed by the curve, the y -axis and the line $x = \frac{\pi}{3}$. [5]

OR



The diagram shows the curve $y = 4x^2 - 2x^3$. The point A lies on the curve and the x -coordinate of A is 1. The curve crosses the x -axis at the point B . The normal to the curve at the point A crosses the y -axis at the point C .

(i) Show that the coordinates of C are $(0, 2.5)$. [5]

(ii) Find the area of the shaded region. [6]

BLANK PAGE

BLANK PAGE

BLANK PAGE

Permission to reproduce items where third-party owned material protected by copyright is included has been sought and cleared where possible. Every reasonable effort has been made by the publisher (UCLES) to trace copyright holders, but if any items requiring clearance have unwittingly been included, the publisher will be pleased to make amends at the earliest possible opportunity.

University of Cambridge International Examinations is part of the Cambridge Assessment Group. Cambridge Assessment is the brand name of University of Cambridge Local Examinations Syndicate (UCLES), which is itself a department of the University of Cambridge.