

UNIVERSITY OF CAMBRIDGE INTERNATIONAL EXAMINATIONS
International General Certificate of Secondary Education

MARK SCHEME for the May/June 2012 question paper
for the guidance of teachers

0581 MATHEMATICS	
0581/43	Paper 4 (Extended), maximum raw mark 130

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Abbreviations

cao	correct answer only
cso	correct solution only
dep	dependent
ft	follow through after error
isw	ignore subsequent working
oe	or equivalent
SC	Special Case
www	without wrong working
art	anything rounding to
soi	seen or implied

1	(a) (i)	[0]5 38 oe	1	Allow 5h 38 but not 5h 38mins
	(ii)	92.7 [92.72 to 92.73] oe	2	Allow $92\frac{8}{11}$ or $\frac{1020}{11}$ M1 for $850 \div$ their 9 h 10 min in hours oe Allow $850 \div 9.1$ for M1
	(b) (i)	204 or 203. 9[0] to 203.91	3	M1 for $160 \times 255 + 330 \times 190 + 150 \times 180$ [130 500] M1 dep for $\div 640$
	(ii)	$640 \div (4 + 3 + 1)$ $\times 3 [= 240]$	M1	[Can be in either order or shown together]
	(iii)	150 www 3	M1	Accept $240 \div 3 \times (4 + 3 + 1) = 640$ for M2
	(c)	11 cao www 3	3	M2 for $240 \div 1.6$ oe or M1 for recognition of $240 = 100 + 60 \%$
			3	M1 for figs 340 or figs $550 \div$ speed [e.g. figs 188, figs 306] – can be spoiled by further work and M1 for correct conversion of units to give answer in seconds e.g. speed = 50 m/s M's independent

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<p>2 (a)</p> <p>$[\sin =] \frac{10 \sin 95}{12}$ 56.1 (56.11 to 56.12) www 3</p> <p>(b)</p> <p>$12^2 + 17^2 - 2 \times 12 \times 17 \cos 30$ oe 8.93 [8.925....] www 4</p> <p>(c) (i)</p> <p>126 or 126.1 (126.11 to 126.12)</p> <p>(ii)</p> <p>306 or 306.1 (306.11 to 306.12)</p> <p>(d)</p> <p>$[\sin =] \frac{17 \sin 30}{\text{their}(b)}$ oe or $[\cos =] \frac{12^2 + (\text{their}(b))^2 - 17^2}{2 \times 12 \times \text{their}(b)}$ oe 180 – 95 – their (a)</p> <p>137 [136.5 to 136.9] www 4</p>		<p>M2</p> <p>A1</p> <p>M2</p> <p>A2</p> <p>1ft</p> <p>1ft</p> <p>M2</p> <p>M1</p> <p>A1</p>	<p>M1 for correct implicit equation</p> <p>M1 for correct implicit equation A1 for 79.66 to 79.67 or 79.7</p> <p>ft their (a) + 70 [provided less than 360]</p> <p>ft 180 + their (c)(i) [provided less than 360]</p> <p>M1 for correct implicit equation [107.7 to 107.9 or 108 or 72 or 72.1 to 72.3]</p> <p>e.g. 28.88 to 28.9 seen – may be on diagram <u>Alt methods possible</u> e.g. $[\sin ABC =] \frac{12 \sin 30}{\text{their}(b)}$ [42.2...] gets M1 then 360 – 95 – 30 – their (a) – their 42.2 gets M2 dep on previous M1</p> <p>isw reflex angle 223 or 223.1 to 223.5 after correct answer seen</p>
<p>3 (a)</p> <p>Triangle with vertices (6, 4), (9, 4), (9, 6)</p> <p>(b)</p> <p>Triangle with vertices (11, 1), (8, 1), (8, 3)</p> <p>(c) (i)</p> <p>Rotation 90° [anticlockwise] oe [centre] (0, 0) oe</p> <p>(ii)</p> <p>$\begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}$</p> <p>(d) (i)</p> <p>Triangle with vertices (1, 3), (4, 3), (4, 9)</p> <p>(ii)</p> <p>$\begin{pmatrix} 1 & 0 \\ 0 & 3 \end{pmatrix}$</p>		<p>2</p> <p>2</p> <p>1</p> <p>1</p> <p>1</p> <p>2</p> <p>2</p> <p>2</p>	<p>Ignore labels and condone good freehand in parts (a), (b) and (d)(i)</p> <p>SC1 for translation $\begin{pmatrix} 5 \\ k \end{pmatrix}$ or $\begin{pmatrix} k \\ 3 \end{pmatrix}$</p> <p>SC1 for reflection in $y = 6$</p> <p>If other transformations in addition, then 0, 0, 0 e.g. O, origin</p> <p>B1 each column</p> <p>SC1 for (1, 3) and (4, 3), or (4, 9)</p> <p>B1 right-hand column or $\begin{pmatrix} 3 & 0 \\ 0 & 1 \end{pmatrix}$</p>

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4	(a) (i)	Median = 2 www 2	2	M1 for identifying mid-value [e.g. List with 10 th and 11 th seen in working] or 10.5 soi
		Mode = 3	1	
	(ii)	54 www 2	2	M1 for $3 \div 20 \times 360$ oe
	(b)	184 www 4	4	M1 for 175, 185, 195 soi M1 for $5 \times a + 12 \times b + 3 \times c$ where a, b, c are in correct interval, including boundaries [3680] M1 (dep on 2 nd M) $\div 20$
5	(a) (i)	980 (979.6 to 980.3....) www 4	4	M3 for $(\pi \times 8^2 \times 6) - \left(2 \times \frac{4}{3} \times \pi \times 3^3\right)$ Or M1 for $\pi \times 8^2 \times 6$ and M1 for $\left[2 \times \frac{4}{3} \times \pi \times 3^3\right]$
	(ii)	0.98[0] (0.9796 to 0.9803...)	1ft	ft their (i) $\div 1000$ but not in terms of π
	(b)	1.2[0] (1.195 to 1.196)	2ft	ft their (a)(i) $\times 1.22 \div 1000$ or their (a)(ii) $\times 1.22$ SC1ft for figs 12[0] or 1195 to 1196 Apply ft to SC
	(c)	4.88 or 4.87 (4.871 to 4.878..) www 2	2ft	ft their (a)(i) $\div \pi 8^2$ provided their (a)(i) is not 384π or 1206... M1 for their (a)(i) $\div \pi 8^2$

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6	(a) (i)	180	1	
	(ii)	20	1	
	(b)	220	1	
	(c) (i)	$\frac{170}{240}$ oe isw	1	Allow 0.708, 0.7083... or % equivalents
	(ii)	$\frac{150}{240}$ oe isw	1	Allow 0.625 or % equivalents
	(d)			Penalise once for first correct none 4 dp dec answer to at least 3sf or correct fraction answer in parts (d) and (e)
	(i)	0.5617	2	Accept 56.1715% , do not accept 0.562 ww M1 for $\frac{180}{240} \times \frac{179}{239}$ [0.56171 to 0.56172], $\frac{537}{956}$ oe
	(ii)	0.3766	3	Accept 37.6569% M2 for $2 \times \frac{180}{240} \times \frac{60}{239}$ oe [0.37656 to 0.37657] $\frac{90}{239}$ oe Or M1 for one correct product seen, implied by 0.18828... or 0.1883
	(e)	0.6937	3	Accept 69.3669%, do not accept 0.694 ww M2 for $\frac{150}{180} \times \frac{149}{179}$ [0.69366 to 0.69367] $\frac{745}{1074}$ oe or M1 for $\frac{150}{180}$ oe soi

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7 (a)	1,, 11.3[1..], 16	3	B1 each
(b)	9 points plotted Smooth curve through at least 8 points and exponential shape	P3ft C1ft	P2ft for 7 or 8, P1ft for 5 or 6. ft only if correct shape and covers the domain $0 < x < 4$
(c)	$2.3 < x < 2.35$	1	
(d)	$0.4 < x < 0.5$, $3.25 < x < 3.35$	M1 A1 A1	$y = 3x$ ruled to cut curve at all possible points.
(e)	Reasonable tangent with gradient 3 (their x , their y)	M2 A1	Or M1 for any tangent Dep on M2 . Their point of contact
8 (a)	$u = 24$ $v = 92$ $w = 184$	2 1 1ft	SC1 for angle $DBA = 88$ or $u = \text{angle } CDY$ ft $2 \times$ their v Allow all seen in diagram
(b)	10.8	2	M1 for area factor of 3^2 soi e.g. dividing by 9
(c) (i)	18	2	M1 for $4x + x = 90$ or better
(ii)	72	2ft	ft $90 - \text{their } x$ or $4 \times \text{their } x$
(iii)	54	1	M1 for angle K or $I = 90 - \text{their } x$ or $4 \times \text{their } x$ Allow all seen in diagram

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9	(a) (i)	$-\frac{1}{3}$ oe	2	B1 for $f(2) = -3$ soi
	(ii)	-7	1	
	(b)	$\frac{x-2}{x}$ final answer www	2	M1 for $1 - \frac{2}{x}$ seen
	(c)	$y-1 = x^3$ or $x = y^3 + 1$ $x = \sqrt[3]{y-1}$ or $x-1 = y^3$ $\sqrt[3]{x-1}$ oe final answer www2	M1	i.e. two correct steps For M1, accept a correct reverse flowchart
	(d)	A, F, D	3	B1 each
	(e)	29	2	M1 for $x = k(2)$ or $\sqrt[5]{x+3} = 2$ (Variable can be y in second method)
10	(a)	1.3[0]	3	M2 for $(31.7[0] - 7) \div (12 + 7)$ or better Or M1 for $12x + 7(x + 1) = 31.7[0]$ or better or $31.7[0] - 7$ or better
	(b) (i)	$\frac{36}{y} - \frac{36}{y+1} = 25$ oe	M2	SC1 for $\frac{36}{y}$ oe or $\frac{36}{y+1}$ oe seen Accept both all over $y(y+1)$ Must see at least one of these lines before E mark
		$36(y+1) - 36y = 25y(y+1)$ oe		
		$36y + 36 - 36y = 25y^2 + 25y$ oe		
		$25y^2 + 25y - 36 = 0$	E1	Final line reached without any errors or omissions
(ii)	$(5y+9)(5y-4)$	2	Accept $(25y-20)(y+1.8)$ oe SC1 for $(5y+m)(5y+n)$ where $mn = -36$ or $m+n = 5$	
(iii)	-1.8 oe, 0.8 oe	1ft	ft only SC1 from (b)(ii)	
(iv)	2.6[0]	1ft	ft $2 \times$ positive root from (b)(iii) +1 Dep on pos and neg root in (b)(iii)	

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11 (a)	33, 41 16 π , 25 π 20 π , 30 π	1 1 2	
(b) (i)	8n + 1 oe final answer	2	B1 each e.g. 9 + 8(n - 1), condone n = 8n + 1 SC1 for 8n + k
(ii)	137 www2	2	M1 for their (b)(i) = 1097
(c) (i)	n ² π oe final answer	1	
(ii)	9n ² π oe final answer	1	Allow (3n) ² π
(d)	n(n + 1) π oe final answer	2	SC1 for a quadratic expression e.g. n(n + 1), n ² + 5, n ² + n π