



**ADVANCED
General Certificate of Education
January 2014**

Mathematics
Assessment Unit C3
assessing
Module C3: Core Mathematics 3

[AMC31]



MONDAY 20 JANUARY, MORNING

TIME

1 hour 30 minutes.

INSTRUCTIONS TO CANDIDATES

Write your Centre Number and Candidate Number on the Answer Booklet provided.
Answer **all eight** questions.

Show clearly the full development of your answers.

Answers should be given to three significant figures unless otherwise stated.

You are permitted to use a graphic or scientific calculator in this paper.

INFORMATION FOR CANDIDATES

The total mark for this paper is 75

Figures in brackets printed down the right-hand side of pages indicate the marks awarded to each question or part question.

A copy of the **Mathematical Formulae and Tables booklet** is provided.

Throughout the paper the logarithmic notation used is $\ln z$ where it is noted that $\ln z \equiv \log_e z$

Answer all eight questions.

Show clearly the full development of your answers.

Answers should be given to three significant figures unless otherwise stated.

1 Solve $|3x + 7| \geq 2$ [4]

2 (i) By completing the square, write $x^2 - 4x + 12$ in the form

$$(x + a)^2 + b \quad [2]$$

(ii) Hence describe two successive transformations which map the graph of the function $y = x^2$ to the graph of the function $y = x^2 - 4x + 12$ [2]

3 Expand

$$\frac{1}{(4-x)^2}$$

in a binomial series up to and including the term in x^3 [7]

4 Express

$$\frac{4x^2 - x + 7}{(2x-1)(x+2)}$$

in partial fractions. [8]

5 (a) A curve is described by the parametric equations

$$x = 2 \cot \theta \quad y = 3 - \sin \theta$$

(i) Find a Cartesian equation connecting x and y . [5]

(ii) Find the points where the curve crosses the y -axis. [2]

(b) (i) Differentiate

$$\frac{\ln x - 1}{3x^2}$$

simplifying your answer. [4]

(ii) Find

$$\int \frac{(e^{2x} - e^{-x})^2}{e^x} dx \quad [6]$$

6 (a) Evaluate

$$\sec^2 x + \sin^2 x + \operatorname{cosec}^2 x + \cos^2 x - \tan^2 x - \cot^2 x \quad [2]$$

(b) Solve

$$7 \sec \theta - 8 = \frac{2}{\cot^2 \theta} \quad -\pi \leq \theta \leq \pi \quad [8]$$

7 A flower bed is modelled as the area bounded by the curve $y = 1 + \sin x$, the axes and the line $x = p$ as shown shaded in **Fig. 1** below:

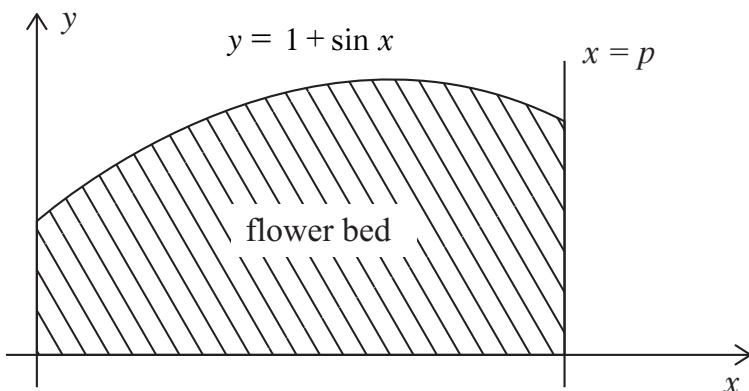


Fig. 1

(i) Show that the area of this flower bed is

$$p - \cos p + 1$$

[6]

(ii) The flower bed is to have an area of 4 units²

Using the Newton–Raphson method, taking the starting value of $p_0 = 2$, find an improved value for p after two applications of the method.

[6]

8 Consider the function $y = \operatorname{cosec}^2 x$.

(i) Find $\frac{d^2y}{dx^2}$, giving your answer in terms of $\operatorname{cosec} x$.

[8]

(ii) Hence find the turning points of the curve

$$y = \operatorname{cosec}^2 x \quad 0 \leq x \leq 2\pi$$

and determine their nature.

[5]

THIS IS THE END OF THE QUESTION PAPER
