



**ADVANCED
General Certificate of Education
2016**

Mathematics
Assessment Unit S4
assessing
Module S2: Statistics 2

[AMS41]

FRIDAY 24 JUNE, MORNING

**MARK
SCHEME**

GCE ADVANCED/ADVANCED SUBSIDIARY (AS) MATHEMATICS

Introduction

The mark scheme normally provides the most popular solution to each question. Other solutions given by candidates are evaluated and credit given as appropriate; these alternative methods are not usually illustrated in the published mark scheme.

The marks awarded for each question are shown in the right-hand column and they are prefixed by the letters **M**, **W** and **MW** as appropriate. The key to the mark scheme is given below:

M indicates marks for correct method.

W indicates marks for working.

MW indicates marks for combined method and working.

The solution to a question gains marks for correct method and marks for an accurate working based on this method. Where the method is not correct no marks can be given.

A later part of a question may require a candidate to use an answer obtained from an earlier part of the same question. A candidate who gets the wrong answer to the earlier part and goes on to the later part is naturally unaware that the wrong data is being used and is actually undertaking the solution of a parallel problem from the point at which the error occurred. If such a candidate continues to apply correct method, then the candidate's individual working must be followed through from the error. If no further errors are made, then the candidate is penalised only for the initial error. Solutions containing two or more working or transcription errors are treated in the same way. This process is usually referred to as "follow-through marking" and allows a candidate to gain credit for that part of a solution which follows a working or transcription error.

Positive marking:

It is our intention to reward candidates for any demonstration of relevant knowledge, skills or understanding. For this reason we adopt a policy of **following through** their answers, that is, having penalised a candidate for an error, we mark the succeeding parts of the question using the candidate's value or answers and award marks accordingly.

Some common examples of this occur in the following cases:

- (a) a numerical error in one entry in a table of values might lead to several answers being incorrect, but these might not be essentially separate errors;
- (b) readings taken from candidates' inaccurate graphs may not agree with the answers expected but might be consistent with the graphs drawn.

When the candidate misreads a question in such a way as to make the question easier only a proportion of the marks will be available (based on the professional judgement of the examining team).

				AVAILABLE MARKS
1	(i)	$r = \frac{\sum xy - \frac{\sum x \cdot \sum y}{n}}{\sqrt{\left(\sum x^2 - \frac{(\sum x)^2}{n}\right)\left(\sum y^2 - \frac{(\sum y)^2}{n}\right)}}$ $= \frac{16725 - \frac{755 \times 233}{10}}{\sqrt{\left(58323 - \frac{755^2}{10}\right)\left(6051 - \frac{233^2}{10}\right)}}$ $= -0.956 \text{ (3 s.f.)}$	M1	
	(ii)	Strong negative correlation between hours of practice and the number of errors	W2	
			W1	
2		$\bar{X}_{15} \sim N\left(155, \frac{12^2}{15}\right)$ $P(154 < \bar{X}_{15} < 156.5) = P(-0.323 < Z < 0.484)$ $= \Phi(0.323) + \Phi(0.484) - 1$ $= 0.6266 + 0.6858 - 1$ $= 0.312 \text{ (3 s.f.)}$	M1	6
			MW1	
			M1	
			MW1	
			W1	5
3		$n = 110$ $\sum fx = 1632$ $\sum fx^2 = 24686$ $\bar{x} = \frac{1632}{110} = 14.836\dots$ $\sigma_{n-1} = 2.08325\dots$ $\text{C. I.} = \bar{x} \pm 1.96 \frac{\hat{\sigma}}{\sqrt{n}}$ $= 14.836\dots \pm 1.96 \times \frac{2.08325\dots}{\sqrt{110}}$ $= (14.45, 15.23) \text{ (4 s.f.)}$	MW1	
			M1 W1	
			M1	
			MW2	
			W2	8
4	(i)	Avoidance of bias		
		Any suitable suggestion	M1	
	(ii)	If using random number tables		
		<ul style="list-style-type: none"> • Assigning values to pupils • Use of table (start, move, etc) • Dealing with duplicates • Dealing with values outside range • Final list 	M5	
	(iii)	<ul style="list-style-type: none"> • Fairness • Wieldy process for large school 	M2	8

		AVAILABLE MARKS
5	$\bar{x} = \frac{1972}{50} = 39.44$ $\hat{\sigma}^2 = \frac{1}{49} \left(78210 - \frac{1972^2}{50} \right)$ $= 8.86\dots$ $H_0: \mu = 40$ $H_1: \mu \neq 40$ (1-tail lower also acceptable) 2-tail z -test at 5% $ z_{\text{crit}} = 1.96$ Reject H_0 if $ z_{\text{test}} > 1.96$ $z_{\text{test}} = \frac{\bar{x} - \mu}{\sqrt{\frac{\sigma^2}{n}}} = \frac{39.44 - 40}{\sqrt{8.86/50}}$ $= -1.33$ Since $ z_{\text{test}} < 1.96$ we do not reject H_0 There is insufficient evidence at 5% level to suggest that the mean mass of the crisps is not 40 g.	MW1 M1 W1 M1 M1 M1 M1 MW1 MW1 W1 M1 M1 12
6	(i) $y = a + bx$ $b = \frac{S_{xy}}{S_{xx}} = \frac{\sum xy - \frac{\sum x \sum y}{n}}{\sum x^2 - \frac{(\sum x)^2}{n}}$ $= \frac{48898 - \frac{210 \times 1142.5}{6}}{9100 - \frac{210^2}{6}}$ $= 5.09$ (3 s.f.) $a = \bar{y} - b\bar{x}$ $= \frac{1142.5}{6} - 5.09\dots \times \frac{210}{6}$ $= 12.2$ (3 s.f.) $\therefore y = 12.2 + 5.09x$ (ii) $x = 45 \rightarrow \hat{y} = 12.2 + 5.09 \times 45$ $\hat{y} = 241$ (grammes) (3 s.f.) (iii) Need equation of x on y	M1 W1 W1 M1 W1 W1 M1 M1 M1 M1 8

											AVAILABLE MARKS
7	differences										
	-1.8	1.5	1.1	-4.3	3.5	-2.7	-1.9	-2.7	-3.4	1.2	M1
	$n = 10$				$\sum d = -9.5$			$\sum d^2 = 68.63$			MW1
	$\bar{d} = -0.95$										MW1
	$\hat{\sigma}_d^2 = 6.62\dots$										MW1
	$H_0: \mu_d = 0$										M1
	$H_1: \mu_d < 0$										M1
	One tailed paired t-test at 5% level										M1
	$t_{\text{crit}} = -1.833$	with			degrees of freedom = 9						M1 M1
	Reject H_0 if $t_{\text{test}} < -1.833$										
	$t_{\text{test}} = \frac{\bar{d} - \mu_d}{\sqrt{\hat{\sigma}_d^2/n}} = \frac{-0.95 - 0}{\sqrt{\frac{6.62\dots}{10}}} = -1.17$										MW1
											MW1
											W1
	Since $t_{\text{test}} > -1.833$ we do not reject H_0										M1
	There is insufficient evidence at 5% to suggest that the use of weight loss literature is effective in reducing weight.										M1
											13

8	(i)	$2X + Y \sim N(2 \times 200 + 190, 2^2 \times 25 + 20)$ $2X + Y \sim N(590, 120)$ $P(2X + Y > 600) = P\left(Z > \frac{600 - 590}{\sqrt{120}}\right)$ $= P(Z > 0.9129)$ $= 1 - \Phi(0.9129)$ $= 0.1806$	MW2	AVAILABLE MARKS
			MW1	
	(ii)	$Y - X \sim N(190 - 200, 20 + 25)$ $Y - X \sim N(-10, 45)$ $P(Y - X < 5) = P(-5 < Y - X < 5)$ $= P\left(\frac{-5 - (-10)}{\sqrt{45}} < Z < \frac{5 - (-10)}{\sqrt{45}}\right)$ $= P(0.7454 < Z < 2.236)$ $= \Phi(2.236) - \Phi(0.7454)$ $= 0.9873 - 0.7720$ $= 0.2153$	MW1 M1 MW2 M1 W1	
	(iii)	$X + Y_1 + Y_2 \sim N(200 + 190 + 190, 25 + 20 + 20)$ $\sim N(580, 65)$ $P(X + Y_1 + Y_2 < 590) = P\left(Z < \frac{590 - 580}{\sqrt{65}}\right)$ $= P(Z < 1.240)$ $= \Phi(1.240)$ $= 0.8925$	MW2 MW1 W1	15
		Total	75	