



Rewarding Learning

ADVANCED  
General Certificate of Education  
2018

Centre Number

--	--	--	--	--

Candidate Number

--	--	--	--

# Mathematics

## Assessment Unit C4

*assessing*

Module C4:

Core Mathematics 4



[AMC41]

\*AMC41\*

WEDNESDAY 6 JUNE, MORNING

### TIME

1 hour 30 minutes.

### INSTRUCTIONS TO CANDIDATES

Write your Centre Number and Candidate Number in the spaces provided at the top of this page.

You must answer **all eight** questions in the spaces provided.

Do not write outside the boxed area on each page or on blank pages.

Complete in black ink only. **Do not write with a gel pen.**

Questions which require drawing or sketching should be completed using an H.B. pencil.

All working should be clearly shown in the spaces provided. Marks may be awarded for partially correct solutions. **Answers without working may not gain full credit.**

Answers should be given to three significant figures unless otherwise stated.

You are permitted to use a graphic or scientific calculator in this paper.

### INFORMATION FOR CANDIDATES

The total mark for this paper is 75

Figures in brackets printed down the right-hand side of pages indicate the marks awarded to each question or part question.

A copy of the **Mathematical Formulae and Tables booklet** is provided.

Throughout the paper the logarithmic notation used is  $\ln z$  where it is noted that  $\ln z \equiv \log_e z$

11211



\*24AMC4101\*

**BLANK PAGE**  
**DO NOT WRITE ON THIS PAGE**



**1** A curve is defined by the parametric equations

$$x = 2t \qquad y = 4t^2 + t$$

Find the gradient of the curve when  $t = 4$  [5]

[5]

This image shows a full page of white paper with horizontal dotted lines. The lines are evenly spaced and run across the width of the page, providing a guide for handwriting or typing. There are no margins, text, or other markings on the page.

**[Turn over**



**2** The line  $L_1$  has vector equation

$$\mathbf{r}_1 = \begin{pmatrix} 6 \\ 1 \\ -1 \end{pmatrix} + \lambda \begin{pmatrix} 2 \\ 1 \\ 0 \end{pmatrix}$$

The line  $L_2$  passes through the points  $(2, 3, -1)$  and  $(4, -1, 1)$ .

(i) Find the vector equation of  $L_2$

[3]

[illegible]

[4]

11211



\*24AMC4105\*

**3** The functions  $f$  and  $g$  are defined by

$$f(x) = \sqrt{2x + 5} \quad \text{for } x \in \mathbb{R}, x \geq -2.5$$

$$g(x) = \frac{1}{4x + 1} \quad \text{for } x \in \mathbb{R}, x \neq -0.25$$

(i) State the range of  $f$ .

[1]

**(ii)** Find the inverse function  $f^{-1}(x)$  stating the domain of this function.

[4]

[4]

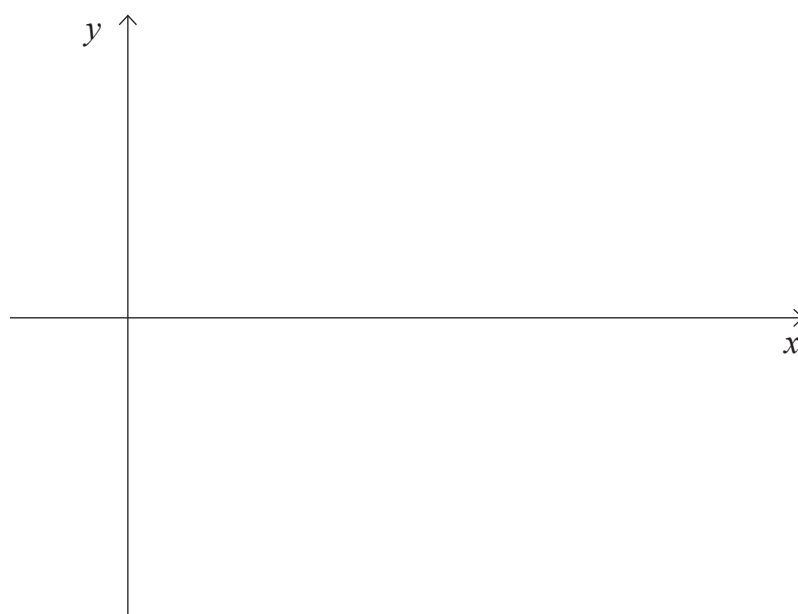
11211



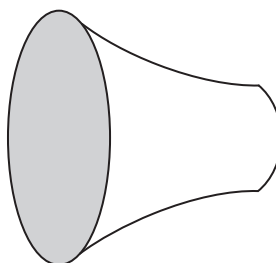
\*24AMC4107\*

- 4 (i) On the axes below sketch the graph of  $y = \sec x$  for  $0 \leq x \leq 2\pi$

[3]



**Fig. 1** below shows a cable reel.



**Fig. 1**

The volume of this reel can be modelled by rotating the area bounded by the graph of  $y = \sec x$ , the  $x$ -axis and the ordinates  $x = 2$  and  $x = 3$  through  $2\pi$  radians about the  $x$ -axis.





[5]

11211



\*24AMC4109\*

**5** Solve the equation

$$\sin 2x = \tan x$$

for  $0^\circ \leq x \leq 360^\circ$

[9]





Handwriting practice lines consisting of 24 horizontal dotted lines.

[Turn over]



**6** A curve has the equation

$$ye^{-2x} = 2x + y^2$$

**(i)** Show that the gradient function of this curve is given by

$$\frac{2 + 2ye^{-2x}}{e^{-2x} - 2y} \quad [7]$$

[illegible]

The point P (0,1) lies on this curve.

- [illegible]

11211



- After  $t$  minutes the coffee has cooled to  $\theta^{\circ}\text{C}$ .

The rate at which the coffee is cooling can be modelled by the differential equation

where  $k$  is a constant.

At  $t = 5$ , the coffee has a temperature of  $68^{\circ}\text{C}$ .

- (i) Show that

$$\theta = 20 + 80e^{-\left(\frac{1}{5}\ln\frac{5}{3}\right)t} \quad [9]$$

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

This image shows a full page of white paper with horizontal dotted lines. The lines are evenly spaced and run across the width of the page, providing a guide for handwriting practice. There are no margins, text, or other markings on the page.

[1]

[illegible]

11211



**8 (a)** Find

$$\int x \cot^2 x \, dx \quad [6]$$

11211



**\*24AMC4116\***



11211



\*24AMC4117\*

**(b) (i)** Write in partial fractions

$$\frac{2}{x(2x-1)}$$

[2]

This image shows a full page of white paper with horizontal dashed lines, typical of primary-ruled notebook paper. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

This image shows a full page of white paper with horizontal blue or grey ruling lines. The lines are evenly spaced and run across the width of the page, providing a template for handwriting practice. There are no margins, text, or other markings on the page.

11211





**THIS IS THE END OF THE QUESTION PAPER**



\*24AMC4121\*

**BLANK PAGE**  
**DO NOT WRITE ON THIS PAGE**



**BLANK PAGE**

**DO NOT WRITE ON THIS PAGE**

11211



\*24AMC4123\*

**DO NOT WRITE ON THIS PAGE**

For Examiner's use only	
Question Number	Marks
1	
2	
3	
4	
5	
6	
7	
8	

<b>Total Marks</b>	
------------------------	--

Examiner Number

Permission to reproduce all copyright material has been applied for.  
In some cases, efforts to contact copyright holders may have been unsuccessful and CCEA  
will be happy to rectify any omissions of acknowledgement in future if notified.

11211/4



\*24AMC4124\*