



Rewarding Learning

**General Certificate of Secondary Education
2019**

Mathematics

M4

Calculator Paper

Higher Tier

[GMC41]

TUESDAY 21 MAY, 9.15am–11.15am

**MARK
SCHEME**

GCSE MATHEMATICS

Introduction

The mark scheme normally provides the most popular solution to each question. Other solutions given by candidates are evaluated and credit given as appropriate; these alternative methods are not usually illustrated in the published mark scheme.

The marks awarded for each question are shown in the right hand column and they are prefixed by the letters **M**, **A** and **MA** as appropriate. The key to the mark scheme is given below:

M indicates marks for correct method.

A indicates marks for accurate working, whether in calculation, reading from tables, graphs or answers. Accuracy marks may depend on preceding M (method) marks, hence M0 A1 cannot be awarded, i.e. where the method is not correct no marks can be given.

MA indicates marks for combined method and accurate working.

A later part of a question may require a candidate to use an answer obtained from an earlier part of the same question. A candidate who gets the wrong answer to the earlier part and goes on to the later part is naturally unaware that the wrong data is being used and is actually undertaking the solution of a parallel problem from the point at which the error occurred. If such a candidate continues to apply correct method, then the candidate's individual working must be **followed through** from the error. If no further errors are made, then the candidate is penalised only for the initial error. Solutions containing two or more working or transcription errors are treated in the same way. This process is usually referred to as "follow-through marking" and allows a candidate to gain credit for that part of a solution which follows a working or transcription error.

Positive marking:

It is our intention to reward candidates for any demonstration of relevant knowledge, skills or understanding. For this reason we adopt a policy of **following through** their answers, that is, having penalised a candidate for an error, we mark the succeeding parts of the question using the candidate's value or answers and award marks accordingly.

Some common examples of this occur in the following cases:

- (a) a numerical error in one entry in a table of values might lead to several answers being incorrect, but these might not be essentially separate errors;
- (b) readings taken from candidates' inaccurate graphs may not agree with the answers expected but might be consistent with the graphs drawn.

When the candidate misreads a question in such a way as to make the question easier only a proportion of the marks will be available (based on the professional judgement of the examining team).

General Marking Advice

- (i) If the correct answer is seen in the body of the script and the answer given in the answer line is clearly a transcription error, full marks should be awarded.
- (ii) If the answer is missing, but the correct answer is seen in the body of the script, full marks should be awarded.
- (iii) If the correct answer is seen in working but a completely different answer is seen in the answer space, then some marks will be awarded depending on the severity of the error.
- (iv) Work crossed out but not replaced should be marked.
- (v) In general, if two or more methods are offered, mark only the method that leads to the answer on the answer line, if two (or more) answers are offered (with no solution offered on the answer line), mark the poorest answer.
- (vi) For methods not provided for in the mark scheme, give as far as possible equivalent marks for equivalent work.
- (vii) Where a follow through mark is indicated on the mark scheme for a particular part question, the marker must ensure that you refer back to the answer of the previous part of the question.
- (viii) Unless the question asks for an answer to a specific degree of accuracy, always mark at the greatest number of significant figures seen, e.g. the answer in the mark scheme is 4.65 and the candidate then correctly round to 4.7 or 5 on the answer line. Allow full marks for 4.65 seen in the working.
- (ix) Anything in the mark scheme which is in brackets (...) is not required for the mark to be earned, but if present it must be correct.
- (x) For any question, the range of answers given in the mark scheme is inclusive.

			AVAILABLE MARKS
1	$2.5 \times 7 + 7.5 \times 8 + 12.5 \times 5 + 17.5 \times 5 + 22.5 \times 4 + 27.5 \times 1 (= 345)$ $345/30$ $= 11.5$	M1 A1 MA1 A1	4
2	$8x - 12 - 2x + 10$ $= 6x - 2$	MA1 MA1	2
3	$200 = 2 \times 2 \times 2 \times 5 \times 5$ $2^3 \times 5^2$	M1 A1 A1	3
4	$2x + 10 + 2x + x + 20 = 180$ $5x = 150$ $x = 30$ Smallest angle = 50	M1 MA1 MA1 A1	4
5	Diagram correctly set up $4^2 + x^2 = 12^2$ $x^2 = 128$ $x = 11.3$ Perimeter = $4 + 12 + 11.3 = 27.3$	M1 MA1 MA1 MA1 MA1	5
6	(a) 20% increase, e.g. 120% of 150 = 180 20% decrease, e.g. 80% of 180 = 144 – decrease (b) % decrease = 4% (c) (20% decrease) = 0.8×1.2 (20% increase) = same (or similar explanation/calculation to justify answer)	M1 A1 MA1 M1 A1 M1 A1	7
7	SA of sphere = $4 \times \pi \times 6^2 = 452$ SA hemisphere = 226 base = $\pi \times 6^2 = 113$ total = 339 Martha is correct	MA1 MA1 MA1 MA1	4
8	distance travelled in 1 minute = 720m $\sin 20 = x/720$ $x = 720 \sin 20$ $x = 246.25\text{m}$	MA1 MA1 MA1 A1	4
9	$(x - 4)(x + 3) = 0$ $x = 4 \quad x = -3$	M1 A1 A1	3

		AVAILABLE MARKS
10	$2(a - 1) + (a + 1) = 12$ $2a - 2 + a + 1 = 12$ $3a = 13$ $a = 4\frac{1}{3}$	MA1 MA1 MA1 MA1 4
11	$y = 3x + c$ ($c =$ any numerical value, $c \neq 5$)	M1 A1 2
12	$107.5\% = 29455$ $100\% = 29455 \div 107.5 \times 100$ $= \text{£}27400$	MA1 MA1 A1
	Alternative Solution	
	$100\% = 29455 \div 1.075$ $= \text{£}27400$	M1 A1 A1 3
13	(a) Cumulative frequency graph and scale	M1 A2
	(b) 160 – (reading from 55 on their graph) (correct reading approx. $160 - 72 = 88$) Allow A1 for reading at 55	A2 5
14	Year 8: $\frac{126}{756} \times 50 = 8$ or 9	M1 A1 2
15	(a) $5.75 - 3.25 = 2.5$	MA1
	(b) $\frac{5.85}{3.15} = 1.\dot{8}5714\dot{2}$	M1 A1 3
16	(a) perimeter of rectangle = $16 + 4x$ Side of square = $4 + x$	MA1 A1
	(b) (i) $(4 + x)^2 = 16x + 4$	MA1
	$16 + 8x + x^2 = 16x + 4$	MA1
	$x^2 - 8x + 12 = 0$	A1
	(ii) $(x - 2)(x - 6) = 0$ $x = 2, 6$	MA1 A1 7

			AVAILABLE MARKS
17	$l_1 : m = \frac{8 - (-4)}{2 - (-1)} = 4$ $l_2 : m = -\frac{1}{4}$ $y = -\frac{1}{4}x + c$ or $y - 1 = -\frac{1}{4}(x - 1)$ $1 = -\frac{1}{4}(1) + c$ $c = \frac{5}{4}$ $y = -\frac{1}{4}x + \frac{5}{4}$	M1 A1 MA1 MA1 A1	5
18	$\cos AOC = \frac{5}{13}$ $AOC = 67.4^\circ$ $\text{Area of sector AOB} = \frac{67.4}{360} \times \pi \times 13^2 = 99.4$ $AC^2 = 13^2 - 5^2$ $AC = 12$ $\text{Area of triangle OAC} = \frac{1}{2} \times 5 \times 12 = 30$ $\text{Shaded Area} = 99.4 - 30 = 69.4\text{cm}^2$	M1 A1 M1 A1 M1 A1 MA1 MA1	8
19	$\frac{4(x+4) - 3(x+3)}{(x+3)(x+4)} = 1$ $\frac{x+7}{x^2+7x+12} = 1$ $x+7 = x^2+7x+12$ $x^2+6x+5=0$ $(x+1)(x+5)=0$ $x=-1, -5$	M1 MA1 MA1 MA1 MA1 A1	6
20	<p>(a) 30, 15</p> <p>0–10 bar, freq. density of 1.0 10–20 bar, freq. density of 2.5 90–100 bar, freq. density of 1.5 100–120 bar, freq. density of 0.5</p> <p>(b) Median = $40 + \frac{50}{80} \times 20$ = 52.5 minutes</p>	A1 A1 MA1 MA1 MA1 MA1 MA1 A1	8
21	<p>Angle PSQ = 41° (alternate segment theorem) Angle SPQ = 82° (180 – 57 – 41 triangle) (or Angle SPT = 57° (alternate segment theorem) and Angle SPQ = 82° (straight line) Angle SRQ = 98° (opposite angle in cyclic quadrilateral) Angle SQR = 41° (isosceles triangle) So SP parallel to RQ as alternate angles PSQ and SQR are equal</p>	MA1 MA1 MA1 MA1 MA1 MA1 MA1	5

22 (a) $(2a - b)(a + 4b)$

(b)
$$\frac{(x+1)(x-4) + (3x-4)(2x-1)}{(2x-1)(x-4)} \times \frac{2x-1}{x}$$

$$\frac{x^2 - 3x - 4 + 6x^2 - 11x + 4}{(2x-1)(x-4)} \times \frac{(2x-1)}{x}$$

$$\frac{7x^2 - 14x}{(x-4)} \times \frac{1}{x}$$

$$\frac{7(x-2)}{x-4} \text{ or } \frac{7x-14}{x-4}$$

M1 A1

AVAILABLE
MARKS

MA1

MA1

MA1

A1

6

Total**100**