



Centre Number

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| 71 |  |
|----|--|

Candidate Number

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General Certificate of Secondary Education  
January 2015

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## Mathematics

Unit T3  
(With calculator)  
Higher Tier  
[GMT31]



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|------|
| MV18 |
|------|

FRIDAY 9 JANUARY, 9.15am–11.15am

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### TIME

2 hours, plus your additional time allowance.

### INSTRUCTIONS TO CANDIDATES

Write your Centre Number and Candidate Number in the spaces provided at the top of this page.

**You must answer the questions in the spaces provided.**

Complete in blue or black ink only.

Answer **all twenty-seven** questions.

Any working should be clearly shown in the spaces provided since marks may be awarded for partially correct solutions.

You **may** use a calculator for this paper.

## INFORMATION FOR CANDIDATES

The total mark for this paper is 100.

Figures in brackets printed at the end of each question indicate the marks awarded to each question or part question.

Functional Elements will be assessed in this paper.

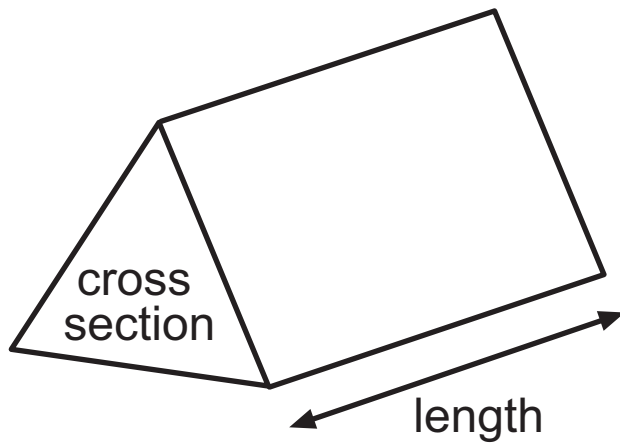
Quality of written communication will be assessed in **Questions 2 and 10**.

You should have a calculator, ruler, compasses and a protractor.  
The Formula Sheet is on pages 4 and 5.

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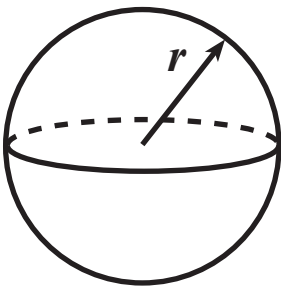
# Formula Sheet

**Volume of prism = area of cross section  $\times$  length**



**Volume of sphere =  $\frac{4}{3} \pi r^3$**

**Surface area of sphere =  $4 \pi r^2$**



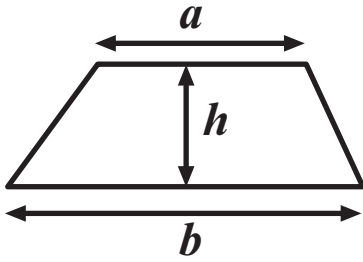
## Quadratic Equation

The solutions of  $ax^2 + bx + c = 0$

where  $a \neq 0$ , are given by

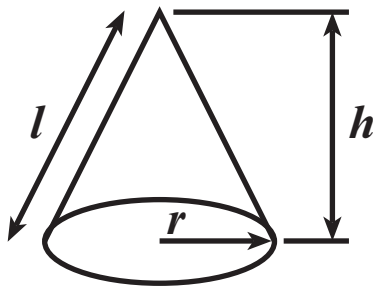
$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Area of trapezium =  $\frac{1}{2} (a + b)h$

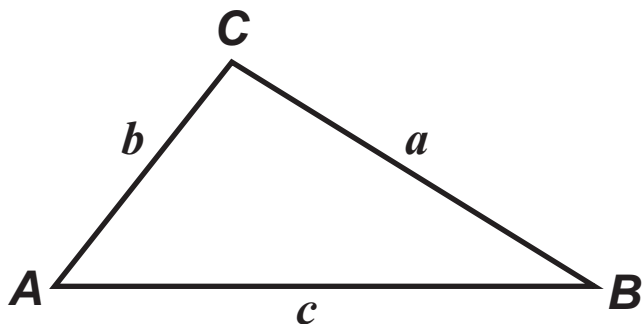


Volume of cone =  $\frac{1}{3} \pi r^2 h$

Curved surface area of cone =  $\pi r l$



In any triangle  $ABC$



Sine Rule:  $\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$

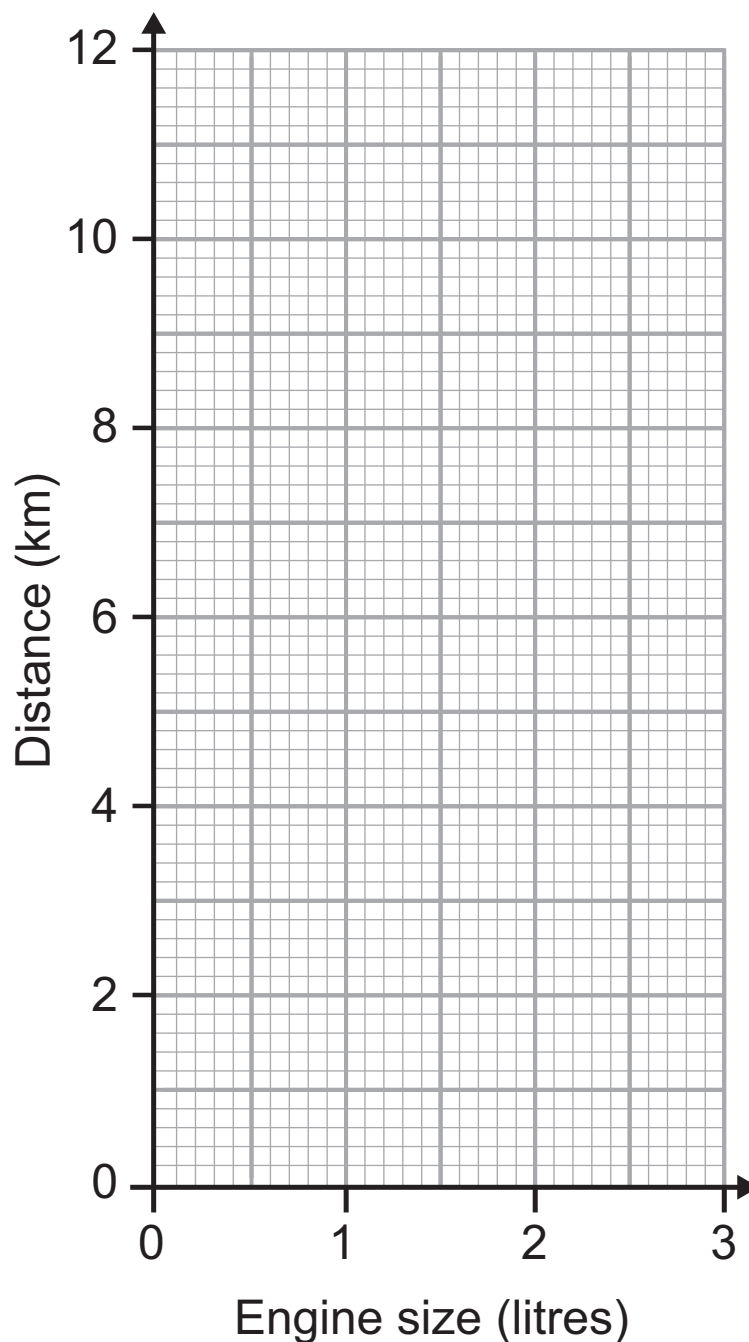
Cosine Rule:  $a^2 = b^2 + c^2 - 2bc \cos A$

Area of triangle =  $\frac{1}{2} ab \sin C$

- 1 The table shows the engine size (litres) of different cars and the distance (km) that the cars can travel on one litre of petrol.

|             |     |     |     |     |     |      |     |
|-------------|-----|-----|-----|-----|-----|------|-----|
| Engine size | 1.0 | 1.8 | 2.4 | 1.2 | 2.1 | 1.5  | 2.7 |
| Distance    | 12  | 8.6 | 5   | 9.4 | 5.9 | 10.2 | 3.8 |

- (a) Draw a scatter graph. [2 marks]



**(b)** Draw a line of best fit. [1 mark]

**(c)** Another car travels 7 km on one litre of petrol. Use your line of best fit to estimate the engine size of this car.  
[1 mark]

Answer \_\_\_\_\_ litres

**Quality of written communication will be assessed in this question.**

- 2** Joanne is having a party. She needs forty packets of crisps. A single packet of crisps costs 30 pence in each of two local stores.  
Each store has a special offer on packets of crisps.

|  |   |
|--|---|
| <p>Bargain Store</p> <p>20% off</p> <p>every ten packets</p> | <p>Discount Store</p> <p>buy 3 and get</p> <p>one more free</p> |
|--|---|

Which is better value? [4 marks]

**Show your working clearly.**

Answer \_\_\_\_\_



- 3** Complete the spaces **(a)**, **(b)**, **(c)** and **(d)** on the electricity bill. [5 marks]

| Northern Electricity |               |                |            |                |              |
|----------------------|---------------|----------------|------------|----------------|--------------|
|                      | Meter Reading |                |            |                |              |
| Date                 | Current units | Previous units | Units used | Price per unit | Total (£)    |
| 30 June              | 43458         | 42763          | <b>(a)</b> | 15 pence       | <b>(b) £</b> |
|                      |               |                |            | VAT @ 5%       | <b>(c) £</b> |
|                      |               |                |            | Total Charge   | <b>(d) £</b> |

- 4 (a) Write the recurring decimal  $0.375375375\dots$  using dot notation. [1 mark]

Answer \_\_\_\_\_

- (b) Write  $0.\dot{2}\dot{8}$  correct to 4 decimal places. [1 mark]

Answer \_\_\_\_\_

- (c) Fill in the box to make the statement correct.

Explain how you get the missing number. [2 marks]

$$\frac{1}{\square} + \frac{2}{9} = \frac{5}{9}$$

- 5 (a) A toy lorry has 6 wheels and a toy car has 4 wheels.

Write down an expression for the **total** number of wheels on  $x$  lorries and  $y$  cars. [2 marks]

Answer \_\_\_\_\_

- (b) Write down the first 3 terms of the sequence whose  $n^{\text{th}}$  term is  $n^2 + 3$  [2 marks]

Answer \_\_\_\_\_,

\_\_\_\_\_,

\_\_\_\_\_

- 6 The diagram shows a regular pentagon placed on top of a regular hexagon.

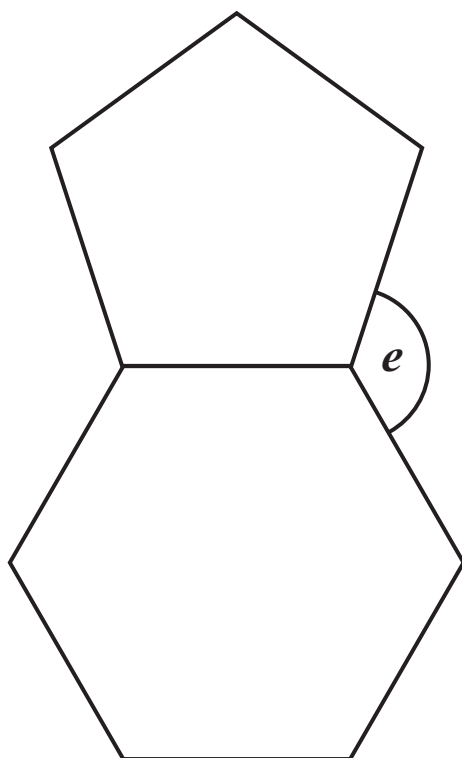


diagram not  
drawn accurately

Calculate the size of the angle marked  $e$ . [4 marks]

**Show all your working.**

Answer  $e =$  \_\_\_\_\_ $^{\circ}$

7 ABCD is a parallelogram.

$$\text{Angle DAB} = 125^\circ$$

$$\text{Angle ADB} = 37^\circ$$

$$\text{Angle CEB} = 51^\circ$$

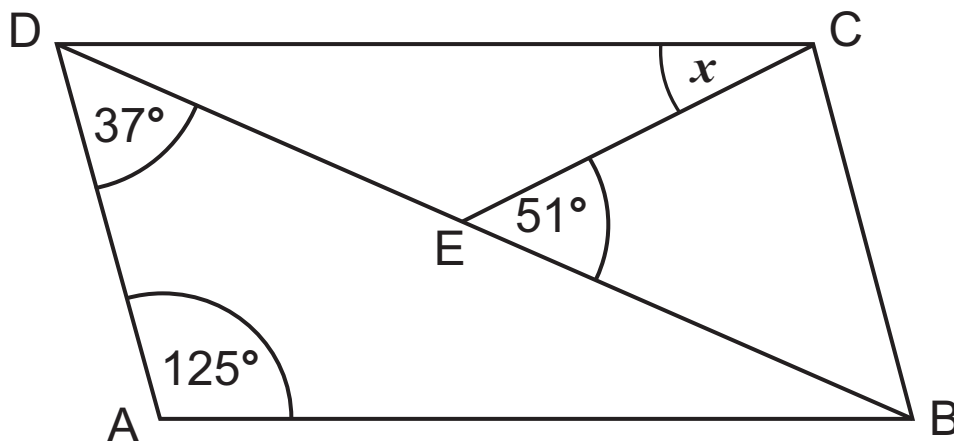


diagram not  
drawn accurately

Calculate the size of the angle  $x$ . [4 marks]

Answer  $x =$  \_\_\_\_\_ °

- 8 The bearing of a fishing boat from a lighthouse is  $118^\circ$ .

Work out the bearing of the lighthouse from the fishing boat.  
[2 marks]

Answer \_\_\_\_\_ $^\circ$

**9** The marks for pupils in a test are shown.

|    |    |    |    |    |    |    |
|----|----|----|----|----|----|----|
| 12 | 58 | 39 | 40 | 52 | 59 | 43 |
| 59 | 26 | 39 | 44 | 42 | 56 | 54 |
| 58 | 43 | 47 | 24 | 27 | 26 | 30 |
| 26 | 38 | 56 | 36 | 36 | 35 | 12 |

Construct a stem and leaf diagram for these marks.  
[3 marks]

**Quality of written communication will be assessed in this question.**

- 10** A questionnaire about their use of a mobile phone was given out to a sample of 20 people who left a supermarket between 10am and 11 am on a Monday morning.  
[2 marks]

Give two reasons why this sample may not be very suitable.

Reason 1 \_\_\_\_\_

\_\_\_\_\_

Reason 2 \_\_\_\_\_

\_\_\_\_\_



**11 Factorise**

**(a)  $8x + 12$  [1 mark]**

Answer \_\_\_\_\_

**(b)  $x^2 + 7x$  [1 mark]**

Answer \_\_\_\_\_

**12 P is the point (2, 3) and Q is the point (−4, −1).**

Work out the coordinates of the midpoint of the line PQ.  
[2 marks]

Answer (\_\_\_\_\_, \_\_\_\_\_)

- 13** The volume of oil in a tank **decreases** by 5% every hour.  
At 11 am there are 9000 litres of oil in the tank.  
What will the volume of oil be at 2 pm? [3 marks]

Answer \_\_\_\_\_ litres

- 14** In a group of golfers there are 37 males and 23 females.  
19 of the males are wearing glasses and 14 of the females  
are wearing glasses.  
What percentage of the group are wearing glasses?  
[3 marks]

Answer \_\_\_\_\_%

- 15** The masses of 300 stones found on a beach are shown in the table.

| Mass (g)         | Number of stones |  |  |
|------------------|------------------|--|--|
| $10 < m \leq 20$ | 33               |  |  |
| $20 < m \leq 30$ | 88               |  |  |
| $30 < m \leq 40$ | 57               |  |  |
| $40 < m \leq 50$ | 52               |  |  |
| $50 < m \leq 60$ | 43               |  |  |
| $60 < m \leq 70$ | 17               |  |  |
| $70 < m \leq 80$ | 10               |  |  |

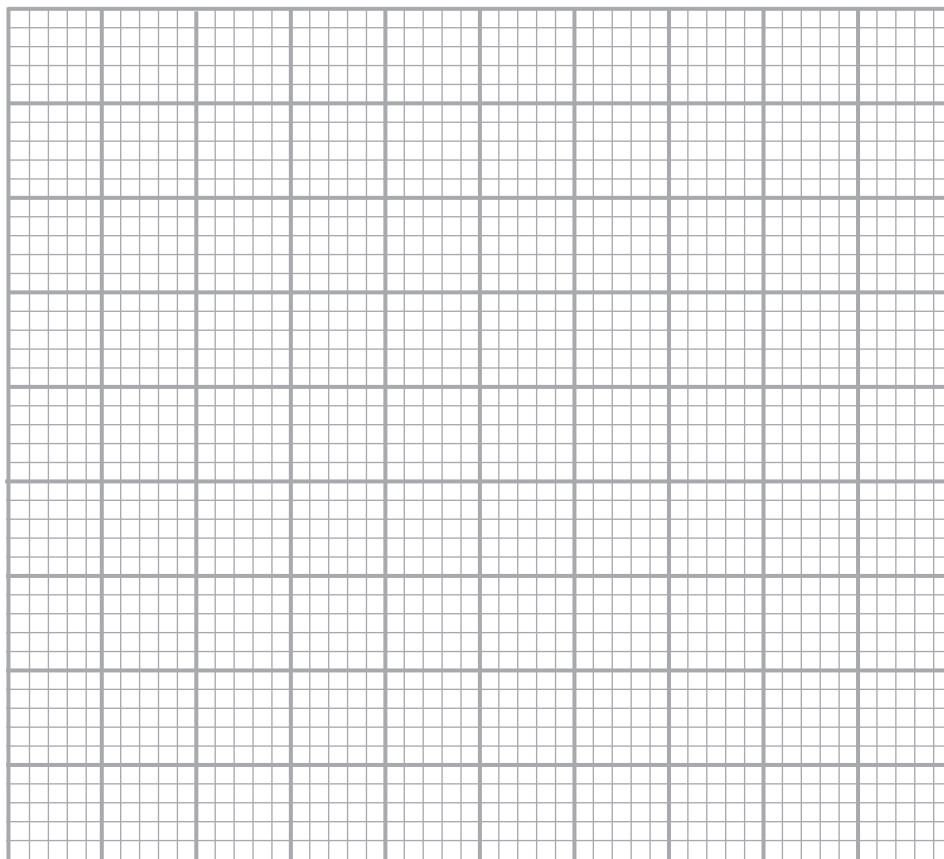
- (a)** Which interval contains the median mass? [1 mark]

Answer \_\_\_\_\_

- (b)** Calculate an estimate of the mean mass of the stones.  
[3 marks]

Answer \_\_\_\_\_ g

- (c) Draw a frequency polygon to represent the data.  
[4 marks]

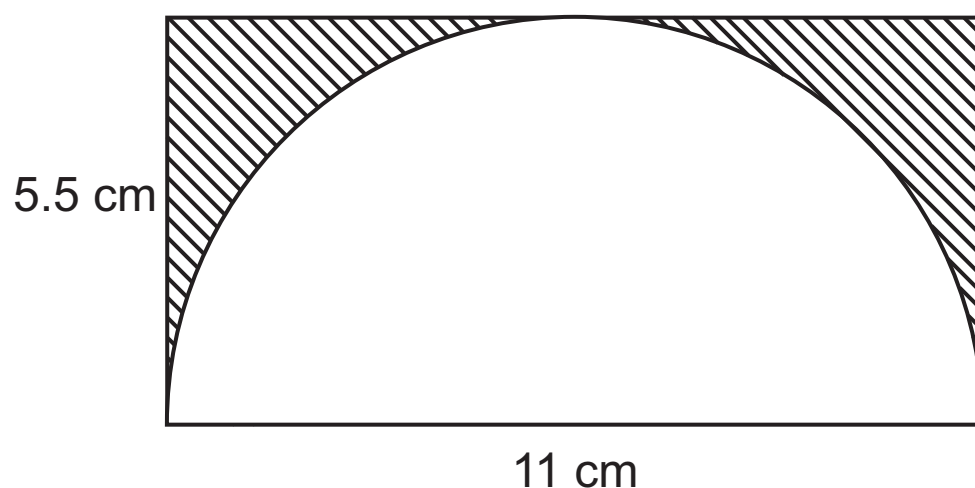


**16** Write 600 as a product of prime factors.

Express your answer in index notation. [3 marks]

Answer \_\_\_\_\_

**17** The diagram shows a semicircle inside a rectangle.



Work out the area of the shaded region. [3 marks]

Answer \_\_\_\_\_  $\text{cm}^2$

- 18** A sheet of A4 paper measures 297 mm by 210 mm.  
Work out the length between diagonally opposite corners.  
[3 marks]

Answer \_\_\_\_\_ mm

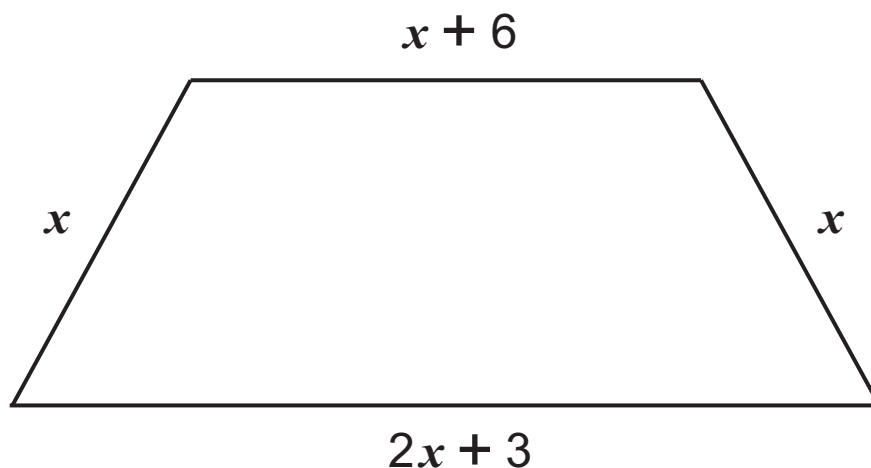


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**(Questions continue overleaf)**

- 19 (a)** Write an expression, in terms of  $x$ , for the perimeter of the trapezium shown.

Give your answer in its simplest form. [2 marks]



Answer \_\_\_\_\_

**(b)** The perimeter of this trapezium is 34 cm.

- (i)** Using the perimeter, write down an equation in terms of  $x$ . [1 mark]

Equation \_\_\_\_\_

- (ii)** Solve the equation to find  $x$ . [1 mark]

Answer  $x =$  \_\_\_\_\_

**20** A solution to the equation  $x^3 - 4x = 26$  lies between 3 and 4

Use trial and improvement to solve this equation.

Give your answer correct to 1 decimal place.

Show each stage of your working. [3 marks]

| $x$ | $x^3 - 4x$ |  |
|-----|------------|--|
|     |            |  |

Answer  $x =$  \_\_\_\_\_

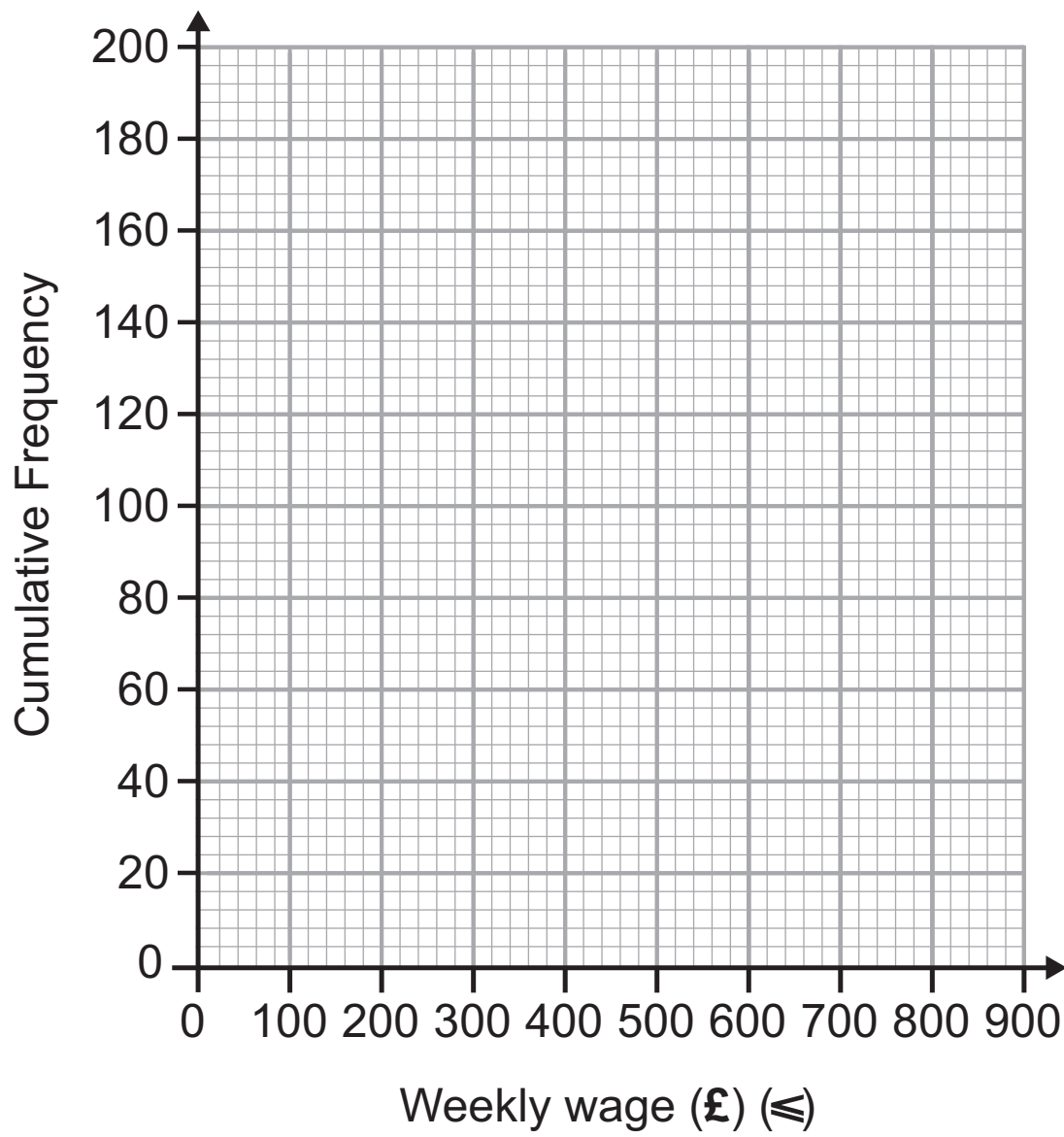
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**(Questions continue overleaf)**

**21** In a survey, a group of people were asked to state their weekly wage. The results are shown.

| Weekly wage (£)    | Frequency | $\leq$ (£) | Cumulative frequency |
|--------------------|-----------|------------|----------------------|
| $0 < w \leq 100$   | 4         | 100        | 4                    |
| $100 < w \leq 200$ | 16        | 200        | 20                   |
| $200 < w \leq 300$ | 25        | 300        |                      |
| $300 < w \leq 400$ | 32        | 400        |                      |
| $400 < w \leq 500$ | 54        | 500        |                      |
| $500 < w \leq 600$ | 25        | 600        |                      |
| $600 < w \leq 700$ | 20        | 700        |                      |
| $700 < w \leq 800$ | 6         | 800        |                      |
| $800 < w \leq 900$ | 2         | 900        |                      |

**(a)** Complete the cumulative frequency column. [1 mark]

**(b)** Draw the cumulative frequency graph on the axes provided opposite. [3 marks]



**(c) Use your graph on page 31 to estimate**

**(i) the median, [1 mark]**

Answer £ \_\_\_\_\_

**(ii) the percentage of people who earn more than  
£640 per week. [2 marks]**

Answer \_\_\_\_\_ %



- 22** A bed has a sale price of £257.40  
This is a saving of 22% on the original price.

What was the original price of the bed? [3 marks]

Answer £ \_\_\_\_\_

- 23** Find the lowest common multiple (LCM) of 54 and 90  
[2 marks]

Answer \_\_\_\_\_

**24 (a)** Solve the simultaneous equations  $9x + 4y = 51$   
 $5x + 4y = 23$

[2 marks]

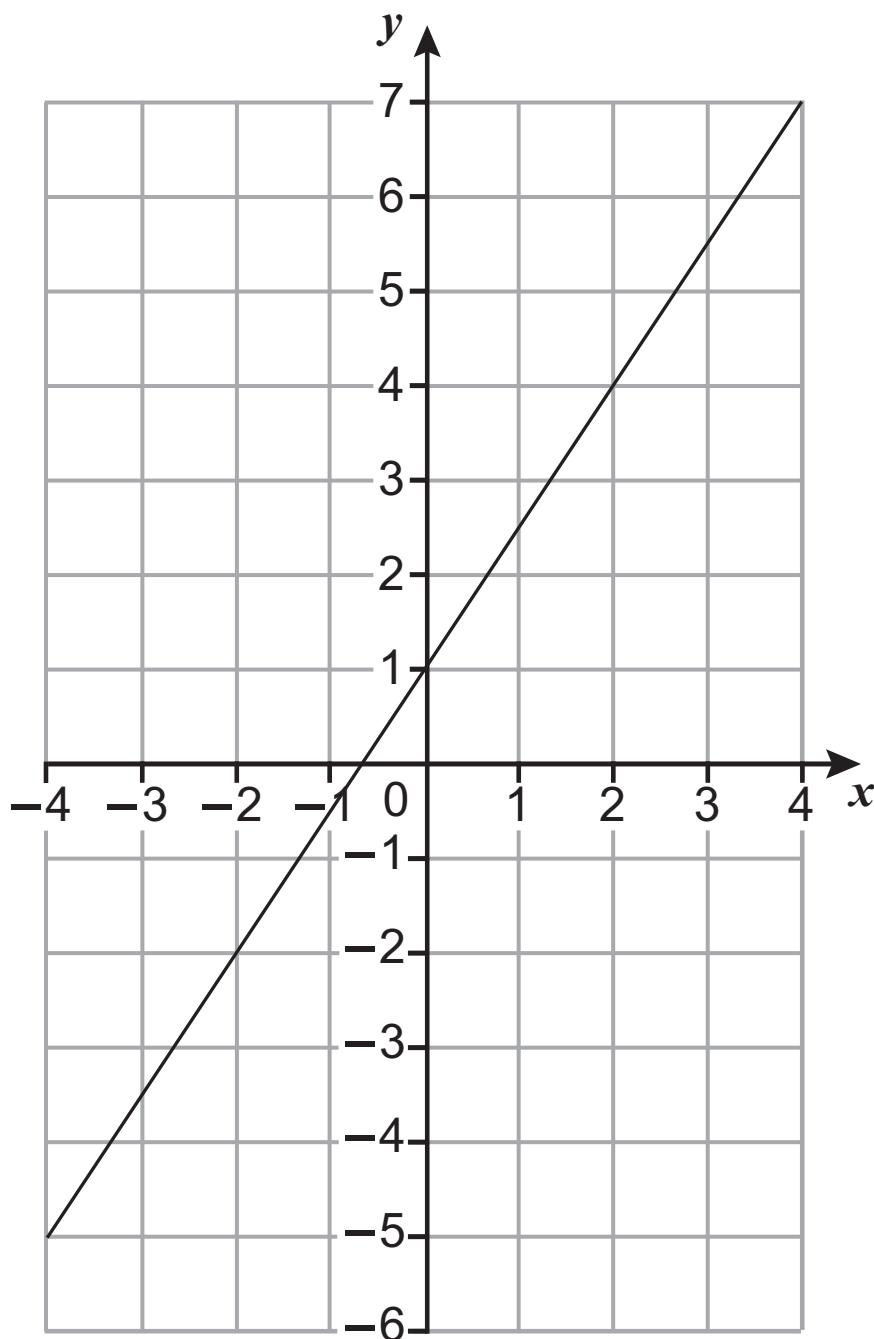
**Show all working. A solution by trial and improvement will not be accepted.**

Answer  $x =$  \_\_\_\_\_,  $y =$  \_\_\_\_\_

**(b)** Solve the equation  $\frac{2x-1}{5} + \frac{4x+5}{10} = \frac{5}{2}$  [4 marks]

Answer  $x =$  \_\_\_\_\_

25



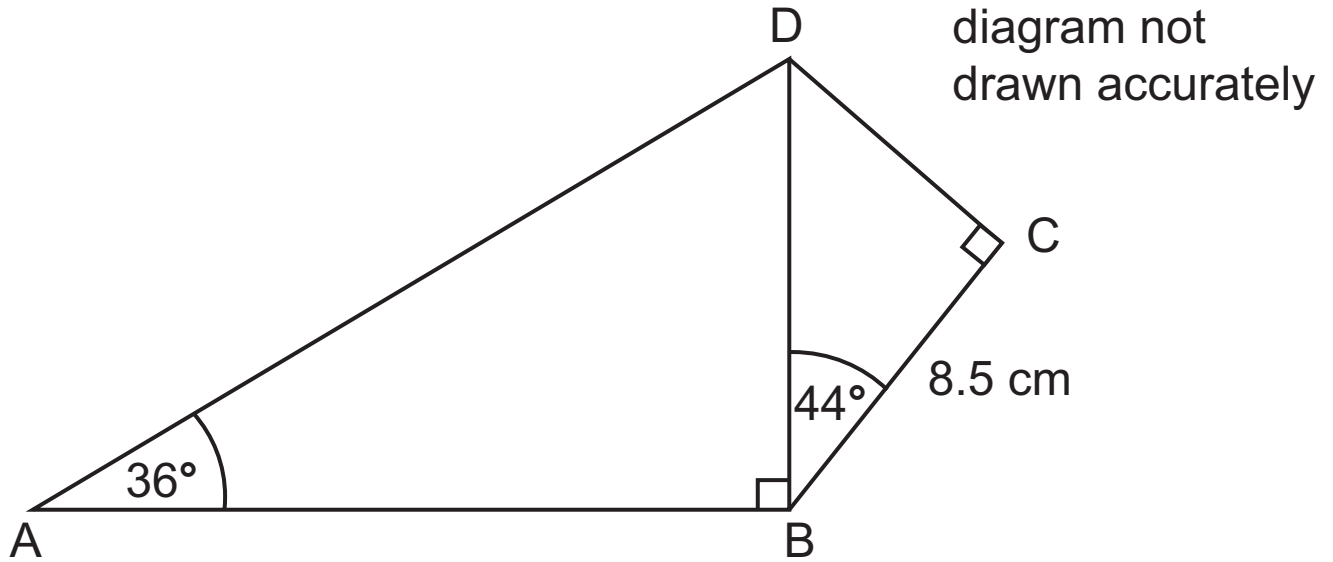
- (a) Write down the gradient of the line drawn above.  
[1 mark]

Answer \_\_\_\_\_

- (b) Hence write down the equation of this line. [2 marks]

Answer \_\_\_\_\_

26



ABCD is a quadrilateral. Angles ABD and BCD are both right angles.

Angle DBC =  $44^\circ$    Angle DAB =  $36^\circ$

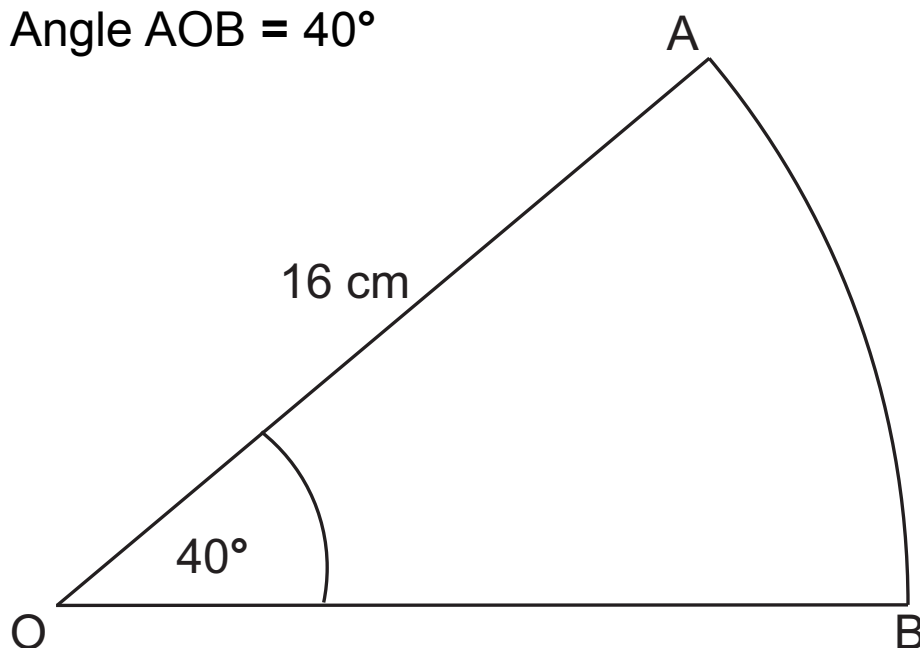
BC = 8.5 cm.

Calculate the length of AD.   [6 marks]

Answer \_\_\_\_\_ cm

**27** AOB is a sector of a circle, radius 16 cm.

Angle AOB =  $40^\circ$



Work out the perimeter of the sector AOB. [3 marks]

Answer \_\_\_\_\_ cm

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**THIS IS THE END OF THE QUESTION PAPER**

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| For Examiner's use only |       |
|-------------------------|-------|
| Question Number         | Marks |
| 1                       |       |
| 2                       |       |
| 3                       |       |
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|                    |  |
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| <b>Total Marks</b> |  |
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Examiner Number

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