



General Certificate of Secondary Education
2016

Centre Number

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Candidate Number

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Mathematics

Unit T4
(With calculator)
Higher Tier



[GMT41]

THURSDAY 26 MAY, 9.15am–11.15am

TIME

2 hours, plus your additional time allowance.

INSTRUCTIONS TO CANDIDATES

Write your Centre Number and Candidate Number in the spaces provided at the top of this page.

You must answer the questions in the spaces provided.

Do not write outside the boxed area on each page, on blank pages or tracing paper.

Complete in blue or black ink only.

Answer **all twenty-one** questions.

Any working should be clearly shown in the spaces provided since marks may be awarded for partially correct solutions.

You **may** use a calculator for this paper.

INFORMATION FOR CANDIDATES

The total mark for this paper is 100.

Figures in brackets printed down the right-hand side of pages indicate the marks awarded to each question or part question.

Functional Elements will be assessed in this paper.

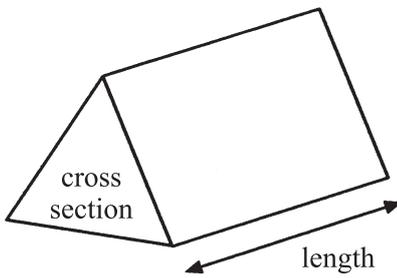
Quality of written communication will be assessed in **Questions 10 and 18**.

You should have a calculator, ruler, compasses and a protractor.

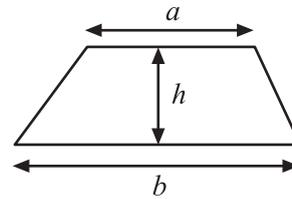
The Formula Sheet is on page 2.

Formula Sheet

Volume of prism = area of cross section \times length

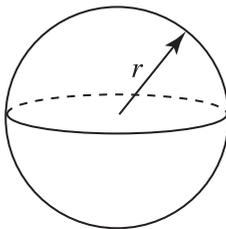


Area of trapezium = $\frac{1}{2}(a+b)h$



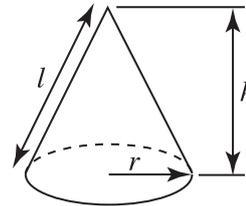
Volume of sphere = $\frac{4}{3}\pi r^3$

Surface area of sphere = $4\pi r^2$

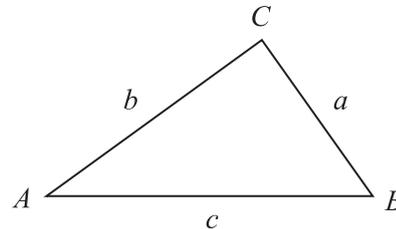


Volume of cone = $\frac{1}{3}\pi r^2 h$

Curved surface area of cone = $\pi r l$



In any triangle ABC



Quadratic Equation

The solutions of $ax^2 + bx + c = 0$
where $a \neq 0$, are given by

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Sine Rule: $\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$

Cosine Rule: $a^2 = b^2 + c^2 - 2bc \cos A$

Area of triangle = $\frac{1}{2} ab \sin C$

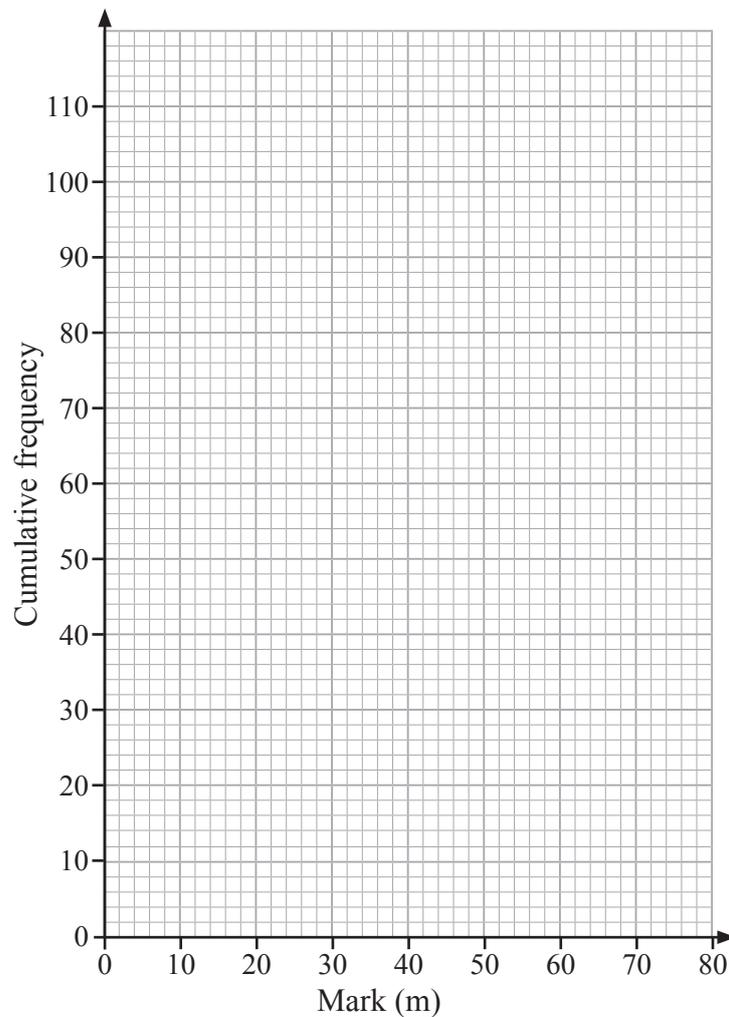


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(Questions start overleaf)

- 1 (a) The marks in an examination are recorded. Write the missing answers in the cumulative frequency column in the table below. [1]

Mark (m)	Frequency	Cumulative Frequency
$0 < m \leq 10$	4	
$10 < m \leq 20$	6	
$20 < m \leq 30$	16	
$30 < m \leq 40$	24	
$40 < m \leq 50$	30	
$50 < m \leq 60$	16	
$60 < m \leq 70$	12	
$70 < m \leq 80$	4	

- (b) Draw a cumulative frequency graph.
Do this on the graph below.



(c) (i) Use the cumulative frequency graph to estimate the median.

Answer _____ [1]

(ii) Use the cumulative frequency graph to estimate the interquartile range.

Answer _____ [2]

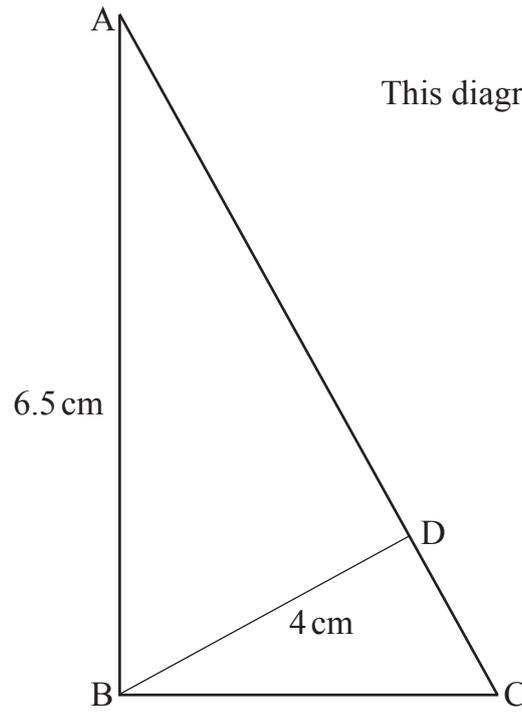
(d) The pass mark is 36

Use the cumulative frequency graph to estimate the percentage of the candidates who pass.

Answer _____ % [2]

[Turn over

2



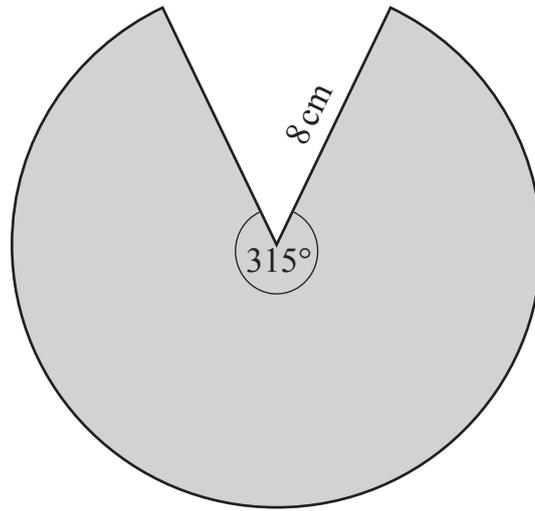
ABC and BDA are right-angled triangles.

$AB = 6.5$ cm and $BD = 4$ cm.

Calculate the length of CD.

Answer _____ cm [6]

3



This diagram is not drawn accurately.

Calculate the area of the shaded sector.

Answer _____ cm² [3]
[Turn over

4 A special offer shampoo bottle has 20% extra.

It has 900 ml of shampoo.

How much shampoo was in the ordinary bottle that was **not** on special offer?

Answer _____ ml [3]

5 A full jar of coffee weighs 670 g. An empty coffee jar weighs 450 g.

Both are measured to the nearest 5 g.

Calculate the maximum weight of coffee in the jar.

Answer _____ g [3]

6 Solve the simultaneous equations

$$3x - y = 7 \text{ and } 5x - 2y = 10$$

A solution by trial and improvement will not be accepted.

Answer $x =$ _____ $y =$ _____ [3]

7 (a) Expand and simplify $(2x - 3)(3x + 4)$

Answer _____ [2]

(b) Factorise $p^2 - 64$

Answer _____ [1]

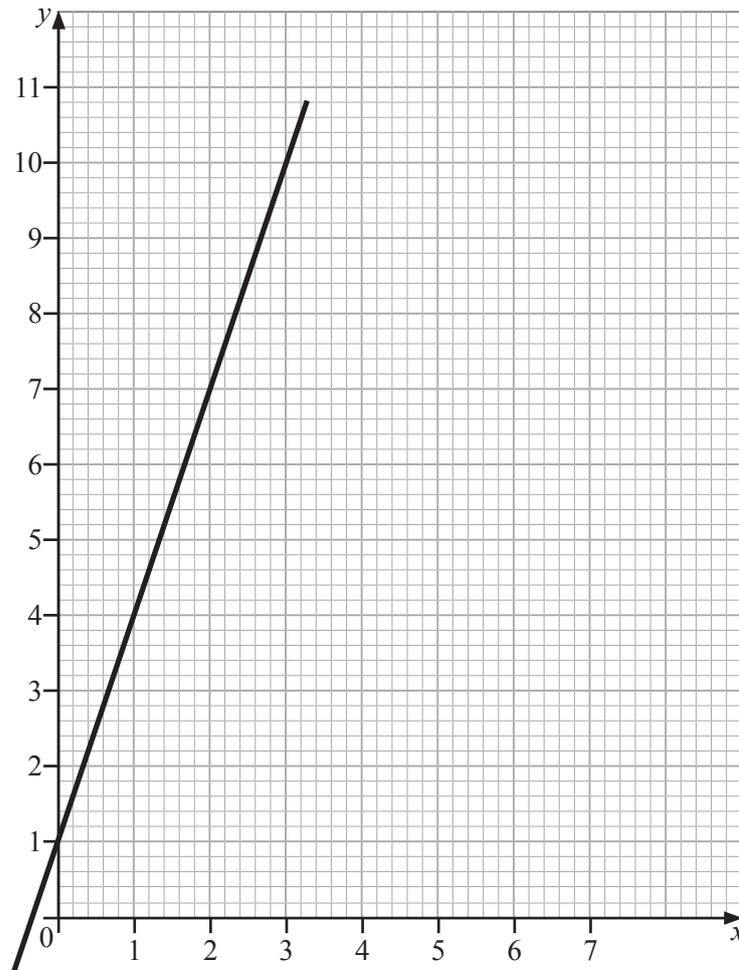
(c) Simplify $\frac{4x^3h}{12x^2h^3}$

Answer _____ [2]



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8



(a) Find the gradient of the line shown.

Answer _____ [1]

(b) Hence write down the equation of the line in the form $y = mx + c$

Answer _____ [1]

- (c) Write down the equation of the line which is parallel to the line shown and which passes through the point $(0, -1)$.

Answer _____ [2]

- (d) Explain why the straight lines $y = 3x - 2$ and $3y + x = 5$ are perpendicular.

[2]

- 9 Jenna runs one lap of a cross-country circuit in 9 minutes.

Her younger brother Luke runs the same circuit in 15 minutes.

They start together. They run in the same direction and have the same lap times.

How many **more** laps will Jenna have done than Luke when they next meet on the starting line together?

Answer _____ [3]

[Turn over

Quality of written communication will be assessed in this question.

10 The grouped frequency table below shows the performance of 22 pupils in a test.

Test Result (marks)	Frequency
$0 \leq x < 20$	7
$20 \leq x < 40$	4
$40 \leq x < 60$	4
$60 \leq x < 80$	3
$80 \leq x < 100$	4

The teacher has worked out the mean, the range, the modal class and the class interval that has the median.

Later, the teacher finds out he has forgotten to record the results for two pupils. These pupils scored 21 and 39 so he changes the data in the table.

(a) How will the range be affected when he puts in the data for these two pupils?

Explain your answer clearly.

[2]

(b) How will the mean be affected when he puts in the data for these two students?

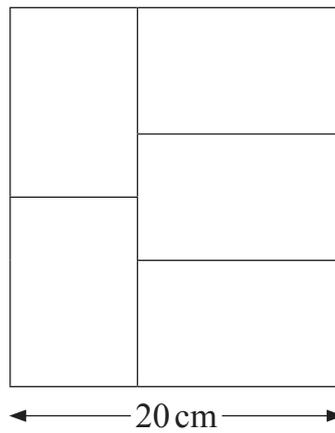
Explain your answer clearly.

[2]

(c) What class interval will have the median when he includes these two students?

Answer _____ [1]

11 Five identical rectangles fit together as shown.



What is the total area covered by the rectangles?

A solution by trial and improvement will not be accepted.

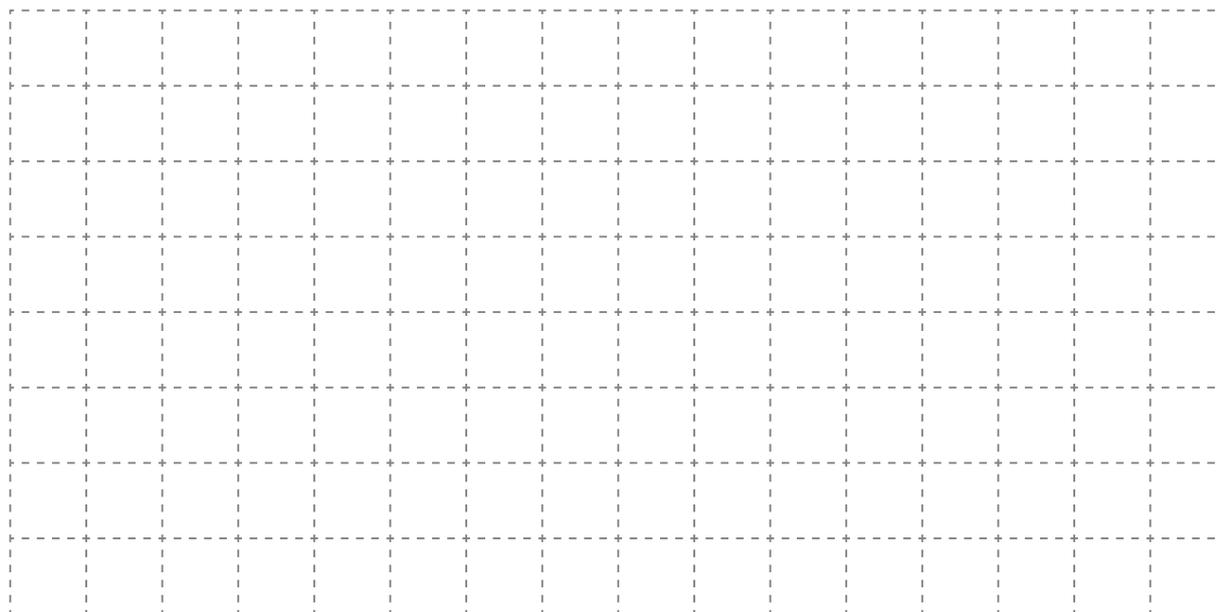
Show your working out.

Answer _____ cm^2 [5]

- 12 The lengths of times, in minutes, for a group of people to do a questionnaire online are recorded below.

Length of time	Number of people	
$0 < t \leq 5$	10	
$5 < t \leq 8$	36	
$8 < t \leq 11$	24	
$11 < t \leq 16$	10	
$16 < t \leq 32$	4	

- (a) Draw a histogram on the grid below to show this data. [3]



A stratified sample of 20 people is to be chosen from those who took less than or equal to 16 minutes to do the questionnaire.

- (b) Estimate how many of this sample would have taken more than 8 minutes.

Answer _____ [2]

[Turn over

13 A rectangular garden has a length that is 3 metres longer than its width.

Its length is made bigger by adding 3 metres. The width is made smaller by 2 metres.

The area of the newly made garden is exactly the same as the area of the original garden.

Find the new length and width.

New length = _____ m

New width = _____ m [4]

14 (a) Y is directly proportional to the cube of X.

$$Y = 960 \text{ when } X = 4$$

Express Y in terms of X.

Answer _____ [2]

(b) Calculate the value of X when Y = 405

Answer _____ [2]

15 (a) Given $(2^n)^{\frac{2}{3}} = 16$, find the value of n .

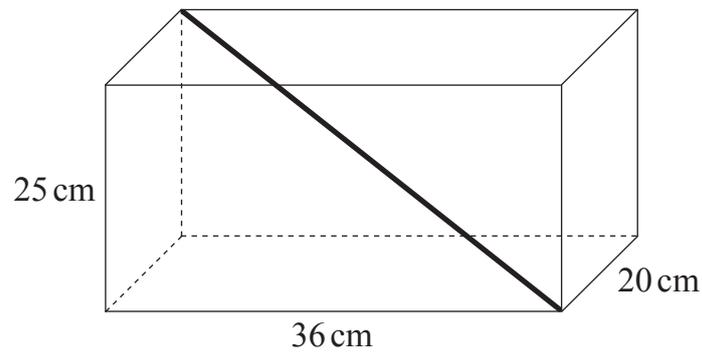
Answer $n =$ _____ [2]

(b) The value of $P = 81$ and the value of $Q = 32$

Find the value of m given that $(P^{\frac{1}{2}} + Q^{\frac{4}{5}})^{-m} = \frac{1}{5}$

Answer $m =$ _____ [3]

16 The diagram below shows the position of the longest rod that can fit inside a box.



(a) Calculate the length of the rod.

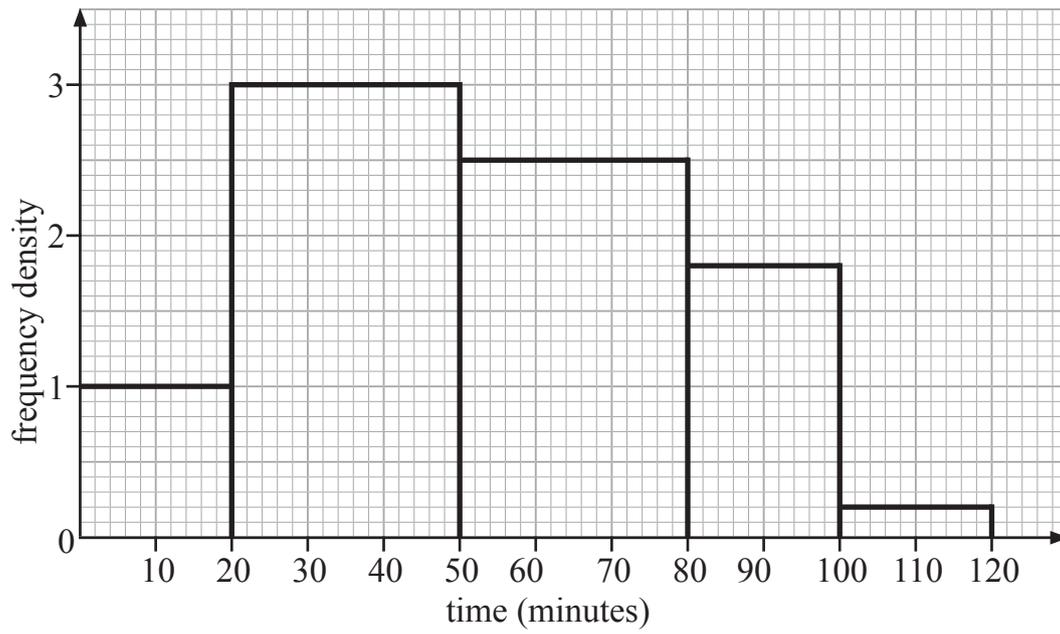
Answer _____ cm [2]

(b) Calculate the angle that the rod makes with the base of the box.

Answer _____ ° [3]

[Turn over

17 The histogram below shows how much time drivers took on a particular journey.



(a) Calculate an estimate for the mean time.

Answer _____ minutes [4]

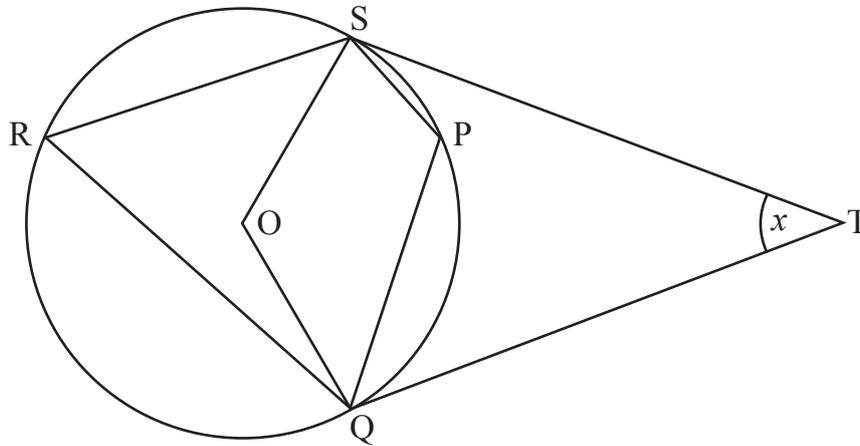
(b) Two-thirds of the drivers took more than M minutes.

Calculate an estimate for the value of M.

Answer _____ minutes [3]

Quality of written communication will be assessed in this question.

- 18 In the diagram, O is the centre of the circle.
 P, Q, R and S are points on the circumference of the circle.
 ST and QT are tangents to the circle.
 Angle $STQ = x$.



Work out the size of angle SPQ in terms of x .

Explain each stage of your working clearly.

Answer $SPQ =$ _____ [5]

19 Simplify $\frac{6a^2 + 4a - 16}{8 - 2a^2}$

Answer _____ [3]

20 Solve the simultaneous equations

$$2x^2 + 3y^2 = 2 \text{ and } x - y + 1 = 0$$

Answer _____ [7]

21 Given $\frac{y+z}{y-z} = 3$ find the value of $\frac{y+3z}{y-3z}$

Answer _____ [5]

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For Examiner's use only	
Question Number	Marks
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Total Marks	
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Examiner Number

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