

Markscheme

May 2015

Mathematical studies

Standard level

Paper 2

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Paper 2 Markscheme
Instructions to Examiners

Notes: If in doubt about these instructions or any other marking issues, contact your team leader for clarification.

1 Abbreviations

M Marks awarded for **Method**

A Marks awarded for an **Answer** or for **Accuracy**

R Marks awarded for clear **Reasoning**

G Marks awarded for correct solutions obtained from a **Graphic Display Calculator**, when no working shown.

AG Answer Given in the question and consequently, marks not awarded.

ft Marks that can be awarded as **follow through** from previous results in the question.

2 Method of Marking

- (a) All marking must be done in RM Assessor using the mathematical studies annotations and in accordance with the current document for guidance in e-marking Mathematical Studies SL. It is essential that you read this document before you start marking.
- (b) If a question part is completely correct use the number tick annotations to award full marks. If a part is completely wrong use the **A0** annotation, otherwise full annotations must be shown.
- (c) Working crossed out by the candidate should not be awarded any marks.
- (d) Where candidates have written two solutions to a question, only the first solution should be marked.
- (e) If correct working results in a correct answer but then further working is developed, indicating a lack of mathematical understanding full marks should **not** be awarded. In most such cases it will be a single final answer mark that is lost. An exception to this may be in numerical answers, where a correct exact value is followed by an incorrect decimal.

Example:

	Correct answer seen	Further working seen	Action
1.	$8\sqrt{2}$	5.65685... (incorrect decimal value)	Award the final (A1) (ignore the further working)
2.	$(x-6)(x+1)$	$x=6$ and -1	Do not award the final (A1)

Example: Calculate the gradient of the line passing through the points (5, 3) and (0, 9).

Markscheme	Candidates' Scripts	Marking
$\frac{9-3}{0-5}$ (M1) Award (M1) for correct substitution in gradient formula $-\frac{6}{5}$ (A1)	(i) $\frac{9-3}{0-5} = -\frac{6}{5}$ Gradient is $= -\frac{6}{5}$ <i>(There is clear understanding of the gradient.)</i>	(M1) (A1)
	(ii) $\frac{9-3}{0-5} = -\frac{6}{5}$ $y = -\frac{6}{5}x + 9$ <i>(There is confusion about what is required.)</i>	(M1) (A0)

3 Follow-through (ft) Marks

Errors made at any step of a solution affect all working that follows. To limit the severity of the penalty, **follow through (ft)** marks can be awarded. Mark schemes will indicate where it is appropriate to apply follow through in a question with **'(ft)'**.

- (a) Follow through applies only from one part of a question to a subsequent part of the question. Follow through does not apply within the same part.
- (b) If an answer resulting from follow through is extremely unrealistic (eg, negative distances or incorrect by large order of magnitude) then the final **A** mark should not be awarded.
- (c) If a question is transformed by an error into a **different, much simpler question** then follow through may not apply.
- (d) To award follow through marks for a question part, **there must be working present for that part**. An isolated follow through answer, without working is regarded as incorrect and receives no marks **even if it is approximately correct**.
- (e) The exception to the above would be in a question which is testing the candidate's use of the GDC, where working will not be expected. **The markscheme will clearly indicate where this applies**.
- (f) Inadvertent use of radians will be penalized the first time it occurs. The markscheme will give clear instructions to ensure that only one mark per paper can be lost for the use of radians.

Example: Finding angles and lengths using trigonometry

Markscheme	Candidates' Scripts	Marking
(a) $\frac{\sin A}{3} = \frac{\sin 30}{4}$ (M1)(A1) <i>Award (M1) for substitution in sine rule formula, (A1) for correct substitutions.</i> $A = 22.0^\circ$ (22.0243...) (A1)(G2)	(a) $\frac{\sin A}{4} = \frac{\sin 30}{3}$ $A = 41.8^\circ$ <i>(Note: the 2nd (A1) here was not marked (ft) and cannot be awarded because there was an earlier error in the same question part.)</i>	(M1)(A0) <i>(use of sine rule but with wrong values)</i> (A0)
(b) $x = 7 \tan (22.0243\dots^\circ)$ (M1) $= 2.83$ (2.83163...) (A1)(ft)	(b) case (i) $x = 7 \tan 41.8^\circ$ $= 6.26$ but case (ii) 6.26	(M1) (A1)(ft) (G0) <i>since no working shown</i>

4 Using the Markscheme

- (a) **A** marks are **dependent** on the preceding **M** mark being awarded, it is **not** possible to award **(M0)(A1)**. Once an **(M0)** has been awarded, all subsequent **A** marks are lost in that part of the question, even if calculations are performed correctly, until the next **M** mark.
The only exception to this will be for an answer where the accuracy is specified in the question – see section 5.
- (b) **A** marks are **dependent** on the **R** mark being awarded, it is **not** possible to award **(A1)(R0)**. Hence the **(A1)** cannot be awarded for an answer which is correct when no reason or the wrong reason is given.
- (c) In paper 2 candidates are expected to demonstrate their ability to communicate mathematics using appropriate working. Answers which are correct but not supported by adequate working will **not always receive full marks**, these unsupported answers are designated **G** in the mark scheme as an alternative to the full marks. Example **(M1)(A1)(A1)(G2)**.

Example: Using trigonometry to calculate an angle in a triangle.

Markscheme	Candidates' Scripts	Marking
(a) $\frac{\sin A}{3} = \frac{\sin 30}{4}$ (M1)(A1) Award (M1) for substitution in sine rule formula, (A1) for correct substitutions. $A = 22.0^\circ$ (22.0243...) (A1)(G2)	(i) $\frac{\sin A}{3} = \frac{\sin 30}{4}$ $A = 22.0^\circ$ (ii) $A = 22.0^\circ$ Note: G marks are used only if no working has been shown and the answer is correct.	(M1)(A1) (A1) (G2)

- (d) **Alternative methods** may not always be included. Thus, if an answer is wrong then the working must be carefully analysed in order that marks are awarded for a different method consistent with the markscheme.
Where alternative methods for complete questions are included in the markscheme, they are indicated by '**OR**' etc.
- (e) Unless the question specifies otherwise, accept **equivalent forms**. For example: $\frac{\sin \theta}{\cos \theta}$ for $\tan \theta$.
On the markscheme, these equivalent numerical or algebraic forms will sometimes be written in brackets after the required answer.
Where numerical answers are required as the final answer to a part of a question in the markscheme, the scheme will show, in order:
the 3 significant figure answer worked through from full calculator display;
the exact value $\left(\text{for example } \frac{2}{3} \text{ if applicable} \right)$;
the full calculator display in the form 2.83163... as in the example above.
Where answers are given to 3 significant figures and are then used in subsequent parts of the question leading to a **different** 3 significant figure answer, these solutions will also be given.

- (f) As this is an international examination, all valid **alternative forms of notation** should be accepted. Some examples of these are:

Decimal points: 1.7; 1'7; 1·7; 1,7 .

Decimal numbers less than 1 may be written with or without a leading zero: 0.49 or .49 .

Different descriptions of an interval: $3 < x < 5$; $(3, 5)$; $] 3, 5 [$.

Different forms of notation for set properties (eg, complement): A' ; \bar{A} ; A^c ; $U - A$; $(A; U \setminus A$.

Different forms of logic notation: $\neg p$; p' ; \tilde{p} ; \bar{p} ; $\sim p$.

$p \Rightarrow q$; $p \rightarrow q$; $q \Leftarrow p$.

Significance level may be written as α .

- (g) Discretionary marks: There will be very rare occasions where the markscheme does not cover the work seen. In such cases the annotation DM should be used to indicate where an examiner has used discretion. Discretion should be used sparingly and if there is doubt and exception should be raised through RM Assessor to the team leader.

As with previous sessions there will be no whole paper penalty marks for accuracy AP, financial accuracy FP and units UP. Instead these skills will be assessed in particular questions and the marks applied according to the rules given in sections 5, 6 and 7 below.

5 Accuracy of Answers

Incorrect accuracy should be penalized once only in each question according to the rules below.

Unless otherwise stated in the question, all numerical answers should be given exactly or correct to 3 significant figures.

1. If the **candidate's answer** is seen to 4 sf or greater **and** would round to the required 3 sf answer, then award **(A1)** and ignore subsequent rounding.
2. If the candidate's unrounded answer is **not** seen then award **(A1)** if the answer given is **correctly** rounded to 2 or more significant figures, otherwise **(A0)**.

Note: If the candidate's unrounded answer is **not** seen and the answer is given correct to 1 sf (correct or not), the answer will be considered wrong and will not count as incorrect accuracy. If this answer is used in subsequent parts, then working must be shown for further marks to be awarded.

3. If a correct 2 sf answer is used in subsequent parts, then working **must** be shown for further marks to be awarded. (This treatment is the same as for following through from an incorrect answer.)

These 3 points (see numbers in superscript) have been summarized in the table below and illustrated in the examples following.

	If candidates final answer is given ...					
	Exact or to 4 or more sf (and would round to the correct 3 sf)	Correct to 3 sf	Incorrect to 3 sf	Correct to 2 sf ³	Incorrect to 2 sf	Correct or incorrect to 1 sf
Unrounded answer seen ¹	Award the final (A1) irrespective of correct or incorrect rounding					
Unrounded answer not seen ²	(A1)	(A1)	(A0)	(A1)	(A0)	(A0)
Treatment of subsequent parts	As per MS		Treat as follow through, only if working is seen. ³			

Examples:

Markscheme	Candidates' Scripts	Marking
9.43 (9.43398...) (A1)	(i) 9.43398... is seen followed by 9; 9.4; 9.43; 9.434 <i>etc.</i> (correctly rounded)	(A1)
	(ii) 9.43398... is seen followed by 9.433; 9.44 <i>etc.</i> (incorrectly rounded)	(A1)
	(iii) 9.4	
	(iv) 9	
	(v) 9.3	<i>(incorrectly rounded to 2 sf)</i>
	(vi) 9.44	<i>(incorrectly rounded to 3 sf)</i>

Markscheme	Candidates' Scripts	Marking
7.44 (7.43798...) (A1)	(i) 7.43798... is seen followed by 7; 7.4; 7.44; 7.438 <i>etc.</i> (correctly rounded)	(A1)
	(ii) 7.43798... is seen followed by 7.437; 7.43 <i>etc.</i> (incorrectly rounded)	(A1)
	(iii) 7.4	
	(iv) 7	
	(v) 7.5	<i>(incorrectly rounded to 2 sf)</i>
	(vi) 7.43	<i>(incorrectly rounded to 3 sf)</i>

Example: ABC is a right angled triangle with angle $ABC = 90^\circ$, $AC = 32$ cm and $AB = 30$ cm. Find (a) the length of BC, (b) The area of triangle ABC.

Markscheme	Candidates' Scripts	Marking
(a) $BC = \sqrt{32^2 - 30^2}$ (M1) Award (M1) for correct substitution in Pythagoras' formula $= 11.1 (\sqrt{124}, 11.1355...)$ (cm) (A1)	(a) $BC = \sqrt{32^2 - 30^2}$ 11 (cm) <i>(2 sf answer only seen, but correct)</i>	(M1) (A1)
(b) $\text{Area} = \frac{1}{2} \times 30 \times 11.1355...$ (M1) Award (M1) for correct substitution in area of triangle formula $= 167(167.032...)$ (cm ²) (A1)(ft)	(b) case (i) $\text{Area} = \frac{1}{2} \times 30 \times 11$ $= 165$ (cm ²) case (ii) $= 165$ (cm ²) <i>(No working shown, the answer 11 is treated as a ft, so no marks awarded here)</i>	(M1) <i>(working shown)</i> (A1)(ft) (M0)(A0)(ft)

Certain answers obtained from the GDC are worth 2 marks and working will not be seen. In these cases only one mark should be lost for accuracy.

eg, Chi-squared, correlation coefficient, mean

Markscheme	Candidates' Scripts	Marking
Chi-squared	(a) 7.7	(G2)
7.68 (7.67543...) (A2)	(b) 7.67	(G1)
	(c) 7.6	(G1)
	(d) 8	(G0)
	(e) 7	(G0)
	(e) 7.66	(G0)

Regression line

Markscheme	Candidates' Scripts	Marking
$y = 0.888x + 13.5$ (A2) ($y = 0.887686\dots x + 13.4895\dots$) If an answer is not in the form of an equation award at most (A1)(A0) .	(a) $y = 0.89x + 13$	(G2) (both accepted)
	(b) $y = 0.88x + 13$	(G1) (one rounding error)
	(c) $y = 0.88x + 14$	(G1) (rounding error repeated)
	(d) (i) $y = 0.9x + 13$	(G1) (1 sf not accepted)
	(ii) $y = 0.8x + 13$	
(e) $0.88x + 13$	(one rounding error and not an equation)	

Maximum/minimum/points of intersection

Markscheme	Candidates' Scripts	Marking
(2.06, 4.49) (A1)(A1) (2.06020..., 4.49253...)	(a) (2.1, 4.5)	(A1)(A1) (both accepted)
	(b) (2.0, 4.4)	(A1) (same rounding error twice)
	(c) (2.06, 4.4)	(A1) (one rounding error)
	(d) (2, 4.4)	(A0) (1sf not accepted, one rounding error)

Rounding of an exact answer to 3 significant figures **should be accepted if performed correctly**.

Exact answers such as $\frac{1}{4}$ can be written as decimals to fewer than 3 significant figures if the result is still exact. Reduction of a fraction to its lowest terms is **not** essential, however where an answer simplifies to an integer this is expected.

Ratios of π and answers taking the form of square roots of integers or any rational power of an integer (eg, $\sqrt{13}$, $2^{\frac{2}{3}}$, $\sqrt[4]{5}$, ...) may be accepted as exact answers. All other powers (eg, of non-integers) and values of transcendental functions such as sine and cosine must be evaluated.

If the level of accuracy is specified in the question, a mark will be allocated for giving the answer to the required accuracy. In all such cases the final mark is not awarded if the rounding does not follow the instructions given in the question. A mark for specified accuracy can be regarded as a **(ft)** mark regardless of an immediately preceding **(M0)**.

6 Level of accuracy in finance questions

The accuracy level required for answers will be specified in all questions involving money. This will usually be either whole units or two decimal places. The first answer not given to the specified level of accuracy will not be awarded the final **A** mark. The markscheme will give clear instructions to ensure that only one mark per paper can be lost for incorrect accuracy in a financial question.

Example: A financial question demands accuracy correct to 2 dp.

Markscheme	Candidates' Scripts	Marking
\$231.62 (231.6189) (A1)	(i) 231.6	(A0)
	(ii) 232	(A0) <i>(Correct rounding to incorrect level)</i>
	(iii) 231.61	(A0)
	(iv) 232.00	(A0) <i>(Parts (iii) and (iv) are both incorrect rounding to correct level)</i>

7 Units in answers

There will be specific questions for which the units are required and this will be indicated clearly in the markscheme. The first correct answer with no units or incorrect units will not be awarded the final **A** mark. The markscheme will give clear instructions to ensure that only one or two mark per paper can be lost for lack of units or incorrect units.

The units are considered only when the numerical answer is awarded **(A1)** under the accuracy rules given in Section 5.

Example:

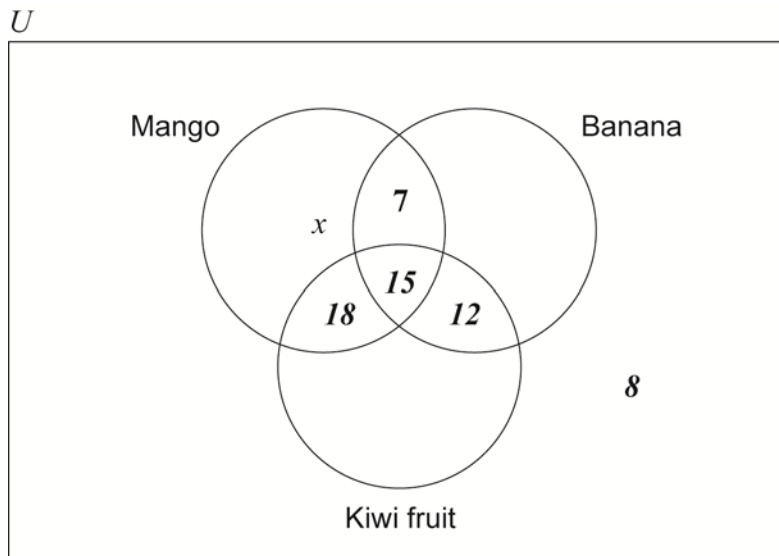
Markscheme	Candidates' Scripts	Marking
(a) 37000 m ² (A1)	(a) 36000 m ²	(A0) <i>(Incorrect answer so units not considered)</i>
(b) 3200 m ³ (A1)	(b) 3200 m ²	(A0) <i>(Incorrect units)</i>

If no method is shown and the answer is correct but with incorrect or missing units award G marks with a one mark penalty.

8 Graphic Display Calculators

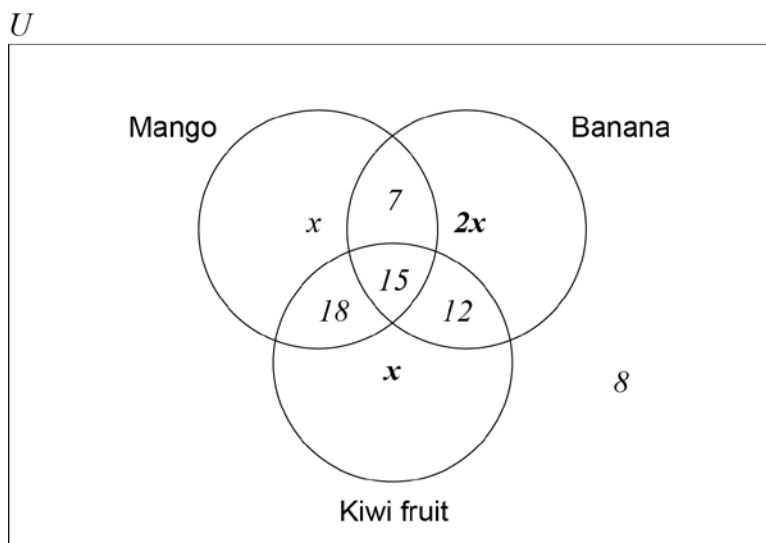
Candidates will often be obtaining solutions directly from their calculators. They must use mathematical notation, not calculator notation. No method marks can be awarded for incorrect answers supported only by calculator notation. The comment 'I used my GDC' cannot receive a method mark.

1. (a)

**(A1)(A1)(A1) [3 marks]**

Notes: Award **(A1)** for 15 in the correct place.
 Award **(A1)** for 7, 18 and 12 seen in the correct places.
 Award **(A1)** for 8 in the correct place.
 Award at most **(A0)(A1)(A1)** if diagram is missing the rectangle.

(b)

**(A1)(A1) [2 marks]**

Notes: Award **(A1)** for x seen in the correct places.
 Award **(A1)** for $2x$ seen in the correct place.
 Award **(A0)(A1)(ft)** if x and $2x$ are replaced by 10 and 20 respectively.

continued...

Question 1 continued

(c) $2x + x + x + 15 + 8 + 7 + 18 + 12 = 100$ ($4x + 60 = 100$ or equivalent) **(M1)**

Note: Award **(M1)** for equating the sum of the elements of their Venn diagram to 100. Equating to 100 may be implied.

$(x =) 10$ **(A1)(ft)(G2)** [2 marks]

Note: Follow through from their Venn diagram. The answer must be a positive integer.

(d) (i) 50 **(A1)(ft)**

(ii) 82 **(A1)(ft)** [2 marks]

Note: Follow through from their answer to part (c) and their Venn diagram.
Award **(A0)(ft)(A1)(ft)** if answer is $\frac{50}{100}$ and $\frac{82}{100}$.

(e) (i) $\frac{8}{100} \left(\frac{2}{25}; 0.08; 8\% \right)$ **(A1)**

Note: Correct answer only. There is no follow through.

(ii) $\frac{37}{100}$ (0.37, 37%) **(A1)(ft)**

Note: Follow through from their Venn diagram.

(iii) $\frac{15}{22}$ (0.681; 0.682; 68.2%) (0.681818...) **(A1)(A1)(ft)(G2)** [4 marks]

Notes: Award **(A1)** for numerator, **(A1)(ft)** for denominator, follow through from their Venn diagram. Award **(A0)(A0)** if answer is given as incorrect reduced fraction without working.

(f) $\frac{8}{100} \times \frac{7}{99}$ **(A1)(ft)(M1)**

Note: Award **(A1)(ft)** for correct fractions, follow through from their answer to part (e)(i), **(M1)** for multiplying their fractions.

$= \frac{56}{9900} \left(\frac{14}{2475}, 0.00565656\dots, 0.00566, 0.0056, 0.566\% \right)$ **(A1)(ft)(G2)** [3 marks]

Total [16 marks]

2. (a) (i) $x^2 + 3^2 = 4^2$ (M1)

Note: Award (M1) for correct substitution into Pythagoras' formula.
Accept correct alternative method using trigonometric ratios.

$$x = 2.64575\dots$$

$$x = 2.65 \text{ (cm)}$$

(A1)
(AG)

Note: The unrounded and rounded answer must be seen for the (A1) to be awarded.

OR

$$\sqrt{4^2 - 3^2}$$

(M1)

Note: Award (M1) for correct substitution into Pythagoras' formula.

$$= \sqrt{7}$$

$$= 2.65 \text{ (cm)}$$

(A1)
(AG)

Note: The exact answer must be seen for the final (A1) to be awarded.

- (ii) $\pi \times 3^2 \times 4.5 + \frac{1}{3} \pi \times 3^2 \times 2.65$ (M1)(M1)(M1)

Note: Award (M1) for correct substitution into the volume of a cylinder formula,
(M1) for correct substitution into the volume of a cone formula,
(M1) for adding both of their volumes.

$$= 152 \text{ cm}^3 \left(152.210\dots \text{ cm}^3, 48.45\pi \text{ cm}^3 \right)$$

(A1)(G3) [6 marks]

continued...

Question 2 continued

$$(b) \quad \pi 3^2 h = 125 \quad (M1)$$

Note: Award **(M1)** for correct substitution into the volume of a cylinder formula. Accept alternative methods. Accept 4.43 (4.42913...) from using rounded answers in $h = \frac{125 \times 4.5}{127}$.

$$h = 4.42 \text{ (cm)} \text{ (4.42097... (cm))} \quad (A1)(G2) \quad [2 \text{ marks}]$$

$$(c) \quad 2\pi \times 3 \times 4.5 + \pi \times 3 \times 4 + \pi \times 3^2 \quad (M1)(M1)(M1)$$

Note: Award **(M1)** for correct substitution into curved surface area of a cylinder formula, **(M1)** for correct substitution into the curved surface area of a cone formula, **(M1)** for adding the area of the base of the cylinder to the other two areas.

$$= 151 \text{ cm}^2 (150.796... \text{ cm}^2, 48\pi \text{ cm}^2) \quad (A1)(G3) \quad [4 \text{ marks}]$$

$$(d) \quad \frac{150.796...}{7} \times 3 \quad (M1)(M1)$$

Notes: Award **(M1)** for dividing their answer to (c) by 7, **(M1)** for multiplying by 3. Accept equivalent methods.

$$= 64.63 \text{ (ZAR)} \quad (A1)(ft)(G2) \quad [3 \text{ marks}]$$

Notes: The **(A1)** is awarded for their correct answer, correctly rounded to 2 decimal places. Follow through from their answer to part (c). If rounded answer to part (c) is used the answer is 64.71 (ZAR).

$$(e) \quad \frac{325}{13.03} \quad (M1)$$

Note: Award **(M1)** for dividing 325 by 13.03.

$$= 24.94 \text{ (EUR)} \quad (A1)(G2) \quad [2 \text{ marks}]$$

Note: The **(A1)** is awarded for the correct answer rounded to 2 decimal places, unless already penalized in part (d).

Total [17 marks]

3. (a) (i) $S_1 = 7$ (A1)
- (ii) $S_2 = 16$ (A1) [2 marks]
- (b) ($u_2 =$) $16 - 7 = 9$ (M1)(AG)

Note: Award (M1) for subtracting 7 from 16. The 9 must be seen.

OR

$$16 - 7 - 7 = 2$$

$$(u_2 =) 7 + (2 - 1)(2) = 9$$

(M1)(AG)

Note: Award (M1) for subtracting twice 7 from 16 and for correct substitution in correct arithmetic sequence formula. The 9 must be seen. Do not accept: $9 - 7 = 2$, $u_2 = 7 + (2 - 1)(2) = 9$.

[1 mark]

- (c) $u_1 = 7$ (A1)(ft)
- $d = 2 (= 9 - 7)$ (A1)(ft)(G2) [2 marks]

Notes: Follow through from their S_1 in part (a)(i).

- (d) $7 + 2 \times (10 - 1)$ (M1)

Note: Award (M1) for correct substitution in the correct arithmetic sequence formula. Follow through from **their** parts (a)(i) and (c).

$$= 25$$

(A1)(ft)(G2) [2 marks]

Note: Award (A1)(ft) for their correct tenth term.

continued...

Question 3 continued

(e) $7 + 2 \times (n - 1) > 1000$

(A1)(ft)(M1)

Note: Award **(A1)(ft)** for their correct expression for the n th term, **(M1)** for comparing their expression to 1000. Accept an equation. Follow through from their parts (a)(i) and (c).

$n = 498$

(A1)(ft)(G2) [3 marks]

Notes: Answer must be a natural number.

(f) $6n + n^2 = 1512$ OR $\frac{n}{2}(14 + 2(n - 1)) = 1512$ OR

$S_n = 1512$ OR $7 + 9 + \dots + u_n = 1512$

(M1)

Notes: Award **(M1)** for equating the sum of the first n terms to 1512. Accept a sum of at least the first 7 correct terms.

$n = 36$

(A1)(G2) [2 marks]

Note: If $n = 36$ is seen without working, award **(G2)**. Award a maximum of **(M1)(A0)** if -42 is also given as a solution.

Total [12 marks]

4. (a) (i) 6.76(cm) (G2)

Notes: Award (M1) for an attempt to use the formula for the mean with a least two rows from the table.

- (ii) 1.14(cm)(1.14122...(cm)) (G1) [3 marks]

- (b) $P(\text{diameter} < 6.5) = 0.338$ (0.338461) (M1)(A1)

Notes: Award (M1) for attempting to use the normal distribution to find the probability **or** for correct region indicated on labelled diagram. Award (A1) for correct probability.

- 33.8(%) (A1)(ft)(G3) [3 marks]

Notes: Award (A1)(ft) for converting their probability into a percentage.

- (c) $P(\text{diameter} \geq a) = 0.05$ (M1)

Note: Award (M1) for attempting to use the normal distribution to find the probability **or** for correct region indicated on labelled diagram.

- $a = 8.97$ (cm) (8.97382...) (A1)(G2) [2 marks]

- (d) $100 - (5 + 33.8461\dots)$ (M1)

Note: Award (M1) for subtracting “5 + their part (b)” from 100 **or** (M1) for attempting to use the normal distribution to find the probability $P(6.5 \leq \text{diameter} < \text{their part (c)})$ **or** for correct region indicated on labelled diagram.

- $= 61.2(\%)$ (61.1538... (%)) (A1)(ft)(G2) [2 marks]

Notes: Follow through from their answer to part (b). Percentage symbol is not required. Accept 61.1(%) (61.1209...(%)) if 8.97 used.

- (e) 100000×0.05 (M1)

Note: Award (M1) for multiplying by 0.05 (or 5%).

- $= 5000$ (A1)(G2) [2 marks]

Total [12 marks]

5. (a) $0.5 \times (-2)^2 - \frac{8}{-2}$ (M1)

Note: Award (M1) for substitution of $x = -2$ into the formula of the function.

6 (A1)(G2) [2 marks]

(b) $f'(x) = x + 8x^{-2}$ (A1)(A1)(A1) [3 marks]

Notes: Award (A1) for x , (A1) for 8, (A1) for x^{-2} or $\frac{1}{x^2}$ (each term must have correct sign). Award at most (A1)(A1)(A0) if there are additional terms present or further incorrect simplifications are seen.

(c) $f'(-2) = -2 + 8(-2)^{-2}$ (M1)

Note: Award (M1) for $x = -2$ substituted into their $f'(x)$ from part (b).

= 0 (A1)(ft)(G2) [2 marks]

Note: Follow through from their derivative function.

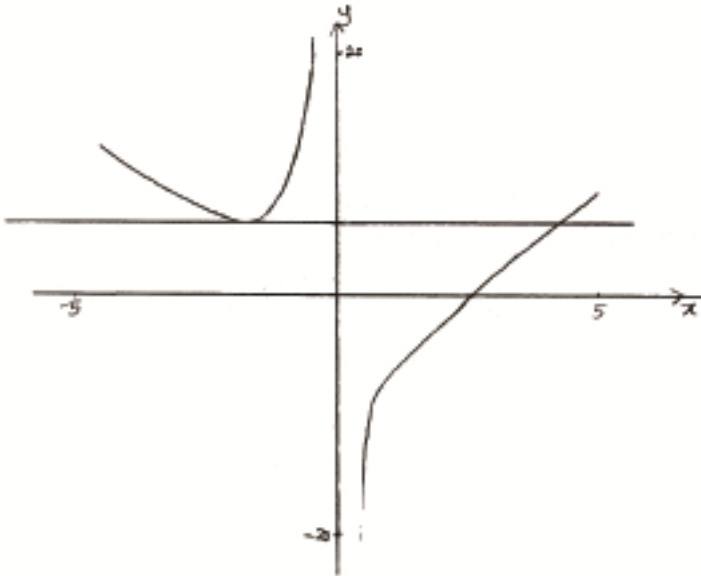
(d) $y = 6$ OR $y = 0x + 6$ OR $y - 6 = 0(x + 2)$ (A1)(ft)(A1)(ft)(G2) [2 marks]

Notes: Award (A1)(ft) for their gradient from part (c), (A1)(ft) for their answer from part (a). Answer must be an equation.
Award (A0)(A0) for $x = 6$.

continued...

Question 5 continued

(e)



(A1)(A1)(A1)(A1) [4 marks]

Notes: Award **(A1)** for labels and some indication of scales in the stated window. The point $(-2, 6)$ correctly labelled, or an x -value and a y -value on their axes in approximately the correct position, are acceptable indication of scales.

Award **(A1)** for correct general shape (curve must be smooth and must not cross the y -axis).

Award **(A1)** for x -intercept in approximately the correct position.

Award **(A1)** for local minimum in the second quadrant.

(f) Tangent to graph drawn approximately at $x = -2$

(A1)(ft)(A1)(ft) [2 marks]

Notes: Award **(A1)(ft)** for straight line tangent to curve at approximately $x = -2$, with approximately correct gradient. Tangent must be straight for the **(A1)(ft)** to be awarded.

Award **(A1)(ft)** for (extended) line passing through approximately their y -intercept from (d). Follow through from their gradient in part (c) and their equation in part (d).

(g) $(4, 6)$ OR $x = 4, y = 6$

(G1)(ft)(G1)(ft) [2 marks]

Notes: Follow through from their tangent from part (d). If brackets are missing then award **(G0)(G1)(ft)**.

If line intersects their graph at more than one point (apart from $(-2, 6)$), follow through from the first point of intersection (to the right of -2).

Award **(G0)(G0)** for $(-2, 6)$.

Total [17 marks]

6. (a) (i) $r = 0.985$ (0.984905...) (G2)

Notes: If unrounded answer is not seen, award (G1)(G0) for 0.99 or 0.984. Award (G2) for 0.98.

- (ii) strong, positive (A1)(A1) [4 marks]

- (b) $y = 259.909\dots x + 698.648\dots$ ($y = 260x + 699$) (G1)(G1) [2 marks]

Notes: Award (G1) for $260x$ and (G1) for 699. If the answer is not an equation award a maximum of (G1)(G0).

- (c) $y = 259.909\dots \times 13 + 698.648\dots$ (M1)

Note: Award (M1) for substitution of 13 into their regression line equation from part (b).

$y = 4077.47\dots$ (A1)(ft)(G2)

$y = 4077$ (USD) (A1)(ft) [3 marks]

Notes: Follow through from their answer to part (b). If rounded values from part (b) used, answer is 4079. Award the final (A1)(ft) for a correct rounding to the nearest USD of their answer. The unrounded answer may not be seen. If answer is 4077 and no working is seen, award (G2).

continued...

Question 6 continued

$$(d) \quad 13 \times 304 - (4077.47) = -125.477 \dots (-125) \quad \text{OR} \\ 4077.47 - (13 \times 304) = 125.477 \dots (125) \quad \text{(M1)}$$

Notes: Award **(M1)** for calculating the difference between 13×304 and their answer to part (c).
If rounded values are used in equation, answer is -127 .

profit is negative **OR** cost > sales **(A1)**

OR

$$13 \times 304 = 3952 \quad \text{(M1)}$$

Note: Award **(M1)** for calculating the price of 13 bikes.

$$3952 < 4077.47 \quad \text{(A1)(ft)} \quad \text{[2 marks]}$$

Note: Award **(A1)** for showing 3952 is less than their part (c). This may be communicated in words. Follow through from part (c), but only if value is greater than 3952.

OR

$$\frac{4077}{13} = 313.62 \quad \text{(M1)}$$

Note: Award **(M1)** for calculating the cost of 1 bicycle.

$$313.62 > 304 \quad \text{(A1)(ft)}$$

Note: Award **(A1)** for showing 313.62 is greater than 304. This may be communicated in words. Follow through from part (c), but only if value is greater than 304.

OR

$$\frac{4077}{304} = 13.41 \quad \text{(M1)}$$

Note: Award **(M1)** for calculating the number of bicycles that should have been be sold to cover total cost.

$$13.41 > 13 \quad \text{(A1)(ft)}$$

Note: Award **(A1)** for showing 13.41 is greater than 13. This may be communicated in words. Follow through from part (c), but only if value is greater than 13.

[2 marks]

continued...

Question 6 continued

(e) (i) $304x$ (A1)

(ii) $304x - (259.909\dots x + 698.648\dots)$ (A1)(ft)(A1)(ft)

Note: Award (A1)(ft) for difference between their answers to parts (b) and (e)(i), (A1)(ft) for correct expression.

(iii) $304x - (259.909\dots x + 698.648\dots) > 0$ (M1)

Notes: Award (M1) for comparing their expression in part (e)(ii) to 0. Accept an equation. Accept $304x - y > 0$ or equivalent.

$x = 16$ bicycles (A1)(ft)(G2) [5 marks]

Notes: Follow through from their answer to part (b). Answer must be a positive integer greater than 13 for the (A1)(ft) to be awarded. Award (G1) for an answer of 15.84.

Total [16 marks]
