

MARKSCHEME

May 2015

MATHEMATICS

Standard level

Paper 2

18 pages



htternational B Baccalauréat ir Bachillerato im

This markscheme is the property of the International Baccalaureate and must **not** be reproduced or distributed to any other person without the authorization of the IB Assessment Centre.

Instructions to Examiners (red changed since M13)

Abbreviations

- *M* Marks awarded for attempting to use a valid **Method**; working must be seen.
- (M) Marks awarded for a valid Method; may be implied by correct subsequent working.
- **A** Marks awarded for an **Answer** or for **Accuracy**; often dependent on preceding **M** marks.
- (A) Marks awarded for an Answer or for Accuracy; may be implied by correct subsequent working.
- *R* Marks awarded for clear **Reasoning**.
- *N* Marks awarded for **correct** answers if **no** working shown.
- **AG** Answer given in the question and so no marks are awarded.

Using the markscheme

1 General

Mark according to RM assessor instructions and the document "Mathematics SL: Guidance for e-marking May 2015". It is essential that you read this document before you start marking. In particular, please note the following. Marks must be recorded using the annotation stamps, using the RM assessor tool. Please check that you are entering marks for the right question. All the marks will be added and recorded by RM assessor.

If a part is **completely correct**, (and gains all the "must be seen" marks), use the ticks with numbers to stamp full marks. Do **not** use the ticks with numbers for anything else.

- If a part is completely wrong, stamp **A0** by the final answer.
- If a part gains anything else, all the working **must** have annotations stamped to show what marks are awarded. This includes any zero marks.

2 Method and Answer/Accuracy marks

- Do **not** automatically award full marks for a correct answer; all working **must** be checked, and marks awarded according to the markscheme.
- It is generally not possible to award *MO* followed by *A1*, as *A* mark(s) depend on the preceding *M* mark(s), if any. An exception to this rule is when work for *M1* is missing, as opposed to incorrect (see point 4).
- Where *M* and *A* marks are noted on the same line, *eg M1A1*, this usually means *M1* for an **attempt** to use an appropriate method (*eg* substitution into a formula) and *A1* for using the **correct** values.
- Where there are two or more **A** marks on the same line, they may be awarded independently; so if the first value is incorrect, but the next two are correct, award **A0A1A1**.
- Where the markscheme specifies (M2), N3, etc., do not split the marks, unless there is a note.
- Most *M* marks are for a valid method, ie a method which can lead to the answer: it must indicate some form of progress towards the answer.
- Once a correct answer to a question or part-question is seen, ignore further correct working. However, if further working indicates a lack of mathematical understanding do not award the final *A1*. An exception to this may be in numerical answers, where a correct exact value is followed by an incorrect decimal (see examples on next page).

Examples

	Correct answer seen	Further working seen	Action
1.	$8\sqrt{2}$	5.65685 (incorrect decimal value)	Award the final A1 (ignore the further working)
2.	$\frac{1}{4}\sin 4x$	sin x	Do not award the final A1
3.	$\log a - \log b$	$\log(a-b)$	Do not award the final A1

3 N marks

If **no** working shown, award **N** marks for **correct** answers – this includes acceptable answers (see accuracy booklet). In this case, ignore mark breakdown (M, A, R). Where a student only shows a final incorrect answer with no working, even if that answer is a correct intermediate answer, award **NO**.

- Do **not** award a mixture of **N** and other marks.
- There may be fewer **N** marks available than the total of **M**, **A** and **R** marks; this is deliberate as it penalizes candidates for not following the instruction to show their working.
- There may not be a direct relationship between the **N** marks and the implied marks. There are times when all the marks are implied, but the **N** marks are not the full marks: this indicates that we want to see some of the working, without specifying what.
- For consistency within the markscheme, **N** marks are noted for every part, even when these match the mark breakdown.
- If a candidate has incorrect working, which somehow results in a correct answer, do **not** award the **N** marks for this correct answer. However, if the candidate has indicated (usually by crossing out) that the working is to be ignored, award the **N** marks for the correct answer.

4 Implied and must be seen marks

Implied marks appear in brackets eg (M1).

- Implied marks can only be awarded if the work is seen or if implied in subsequent working (a correct final answer does not necessarily mean that the implied marks are all awarded). There are questions where some working is required, but as it is accepted that not everyone will write the same steps, all the marks are implied, but the **N** marks are not the full marks for the question.
- Normally the correct work is seen in the next line.
- Where there is an (*M1*) followed by *A1* for each correct answer, if no working shown, one correct answer is sufficient evidence to award the (*M1*).

Must be seen marks appear without brackets eg M1.

- Must be seen marks can only be awarded if the work is seen.
- If a must be seen mark is not awarded because work is missing (as opposed to **MO** or **AO** for incorrect work) all subsequent marks may be awarded if appropriate.

5 Follow through marks (only applied after an error is made)

Follow through (FT) marks are awarded where an incorrect answer (final or intermediate) from one **part** of a question is used correctly in **subsequent** part(s) or subpart(s). Usually, to award FT marks, **there must be working present** and not just a final answer based on an incorrect answer to a previous part. However, if the only marks awarded in a subpart are for the **final** answer, then FT marks should be awarded if appropriate. Examiners are expected to check student work in order to award FT marks where appropriate.

- 4 -

- Within a question part, once an **error** is made, no further **A** marks can be awarded for work which uses the error, but **M** and **R** marks may be awarded if appropriate. (However, as noted above, if an **A** mark is not awarded because work is missing, all subsequent marks may be awarded if appropriate).
- Exceptions to this rule will be explicitly noted on the markscheme.
- If the question becomes much simpler because of an error then use discretion to award fewer *FT* marks.
- If the error leads to an inappropriate value (*eg* probability greater than 1, use of r > 1 for the sum of an infinite GP, $\sin \theta = 1.5$, non integer value where integer required), do not award the mark(s) for the final answer(s).
- The markscheme may use the word "**their**" in a description, to indicate that candidates may be using an incorrect value.
- If a candidate makes an error in one part, but gets the correct answer(s) to subsequent part(s), award marks as appropriate, unless the question says hence. It is often possible to use a different approach in subsequent parts that does not depend on the answer to previous parts.
- In a "show that" question, if an error in a previous subpart leads to not showing the required answer, do not award the final *A1*. Note that if the error occurs within the same subpart, the *FT* rules may result in further loss of marks.
- Where there are anticipated common errors, the *FT* answers are often noted on the markscheme, to help examiners. It should be stressed that these are not the only *FT* answers accepted, neither should *N* marks be awarded for these answers.

6 Mis-read

If a candidate incorrectly copies information from the question, this is a mis-read (**MR**). A candidate should be penalized only once for a particular mis-read. Use the **MR** stamp to indicate that this is a misread. Do not award the first mark in the question, even if this is an **M** mark, but award all others (if appropriate) so that the candidate only loses one mark for the misread.

- If the question becomes much simpler because of the *MR*, then use discretion to award fewer marks.
- If the *MR* leads to an inappropriate value (*eg* probability greater than 1, use of r > 1 for the sum of an infinite GP, $\sin \theta = 1.5$, non integer value where integer required), do not award the mark(s) for the final answer(s).
- Miscopying of candidates' own work does **not** constitute a misread, it is an error.

7 Discretionary marks (d)

An examiner uses discretion to award a mark on the rare occasions when the markscheme does not cover the work seen. In such cases the annotation DM should be used and a brief **note** written next to the mark explaining this decision.

8 Alternative methods

Candidates will sometimes use methods other than those in the markscheme. Unless the question specifies a method, other correct methods should be marked in line with the markscheme. If in doubt, contact your team leader for advice.

- Alternative methods for complete parts are indicated by METHOD 1, METHOD 2, etc.
- Alternative solutions for parts of questions are indicated by **EITHER** . . . **OR**. Where possible, alignment will also be used to assist examiners in identifying where these alternatives start and finish.

9 Alternative forms

Unless the question specifies otherwise, accept equivalent forms.

- As this is an international examination, accept all alternative forms of notation.
- In the markscheme, equivalent **numerical** and **algebraic** forms will generally be written in brackets immediately following the answer.
- In the markscheme, **simplified** answers, (which candidates often do not write in examinations), will generally appear in brackets. Marks should be awarded for either the form preceding the bracket or the form in brackets (if it is seen).

10 Calculators

A GDC is required for paper 2, but calculators with symbolic manipulation features (eg TI-89) are not allowed.

Calculator notation The mathematics SL guide says:

Students must always use correct mathematical notation, not calculator notation. Do **not** accept final answers written using calculator notation. However, do not penalize the use of calculator notation in the working.

11 Style

The markscheme aims to present answers using good communication, eg if the question asks to find the value of k, the markscheme will say k = 3, but the marks will be for the correct value 3 - there is usually no need for the "k =". In these cases, it is also usually acceptable to have another variable, as long as there is no ambiguity in the question, eg if the question asks to find the value of p and of q, then the student answer needs to be clear. Generally, the only situation where the full answer is required is in a question which asks for equations – in this case the markscheme will say "must be an equation". Accept sloppy notation in the working, where this is

followed by correct working eg $-2^2 = 4$ where they should have written $(-2)^2 = 4$.

The markscheme often uses words to describe what the marks are for, followed by examples, using the eg notation. These examples are not exhaustive, and examiners should check what candidates have written, to see if they satisfy the description. Where these marks are **M** marks, the examples may include ones using poor notation, to indicate what is acceptable. A valid method is one which will allow candidate to proceed to the next step eg if a quadratic function is given in factorised form, and the question asks for the zeroes, then multiplying the factors does not necessarily help to find the zeros, and would not on its own count as a valid method.

12 Candidate work

If a candidate has drawn a line through work on their examination script, or in some other way crossed out their work, do not award any marks for that work.

Candidates are meant to write their answers to Section A on the question paper (QP), and Section B on answer booklets. Sometimes, they need more room for Section A, and use the booklet (and often comment to this effect on the QP), or write outside the box. That is fine, and this work should be marked.

The instructions tell candidates not to write on Section B of the QP. Thus they may well have done some rough work here which they assume will be ignored. If they have solutions on the answer booklets, there is no need to look at the QP. However, if there are whole questions or whole part solutions missing on answer booklets, please check to make sure that they are not on the QP, and if they are, mark those whole questions or whole part solutions that have not been written on answer booklets.

-7-

13. Diagrams

The notes on how to allocate marks for sketches usually refer to passing through particular points or having certain features. These marks can only be awarded if the sketch is approximately the correct shape. All values given will be an approximate guide to where these points/features occur. In some questions, the first *A1* is for the shape, in others, the marks are only for the points and/or features. In both cases, unless the shape is approximately correct, no marks can be awarded (unless otherwise stated). However, if the graph is based on previous calculations, *FT* marks should be awarded if appropriate.

14. Accuracy of Answers

If the level of accuracy is specified in the question, a mark will be allocated for giving the final answer to the required accuracy. When this is not specified in the question, all numerical answers should be given exactly or correct to three significant figures.

Do not accept unfinished numerical final answers such as 3/0.1 (unless otherwise stated). As a rule, numerical answers with more than one part (such as fractions) should be given using integers (*eg* 6/8). Calculations which lead to integers should be completed, with the exception of fractions which are not whole numbers.

Intermediate values do not need to be given to the correct three significant figures. But, if candidates work with rounded values, this could lead to an incorrect answer, in which case award *A0* for the final answer.

Where numerical answers are required as the **final** answer to a part of a question in the markscheme, the markscheme will show

a truncated 6 sf value, the exact value if applicable, and the correct 3 sf answer.

Units (which are generally not required) will appear in brackets at the end.

-8- M15/5/MATME/SP2/ENG/TZ2/XX/M

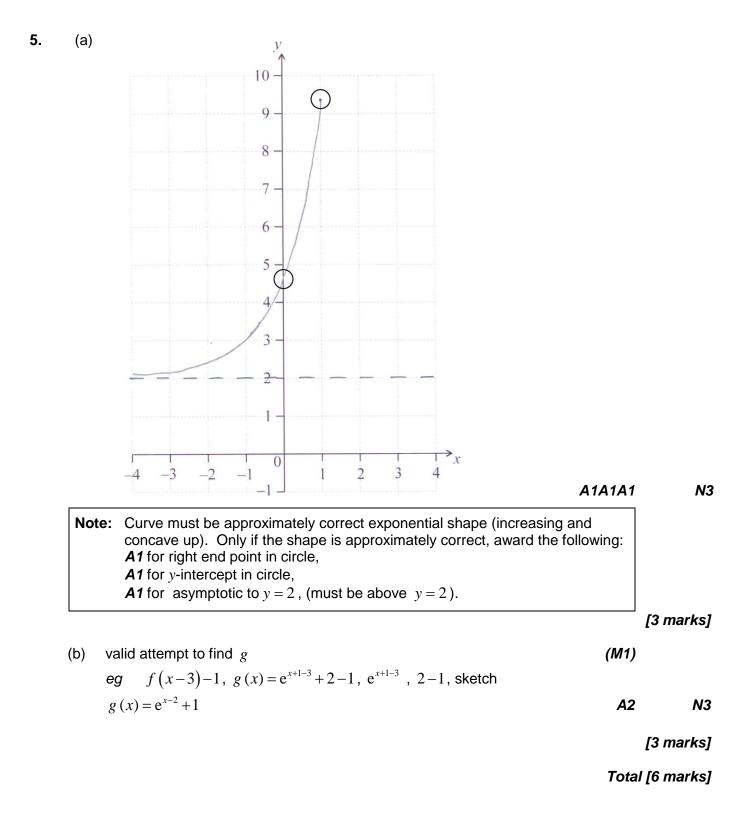
Section A

1.	(a)	evidence of choosing sine rule	(M1)	
		$eg \qquad \frac{AC}{\sin(A\hat{B}C)} = \frac{BC}{\sin(B\hat{A}C)}$		
		correct substitution $eg = \frac{AC}{\sin 80^{\circ}} = \frac{10}{\sin 35^{\circ}}$	(A1)	
		AC = 17.1695 AC = 17.2 (cm)	A1 [3 mar	N2 ks]
	(b)	$\hat{ACB} = 65^{\circ}$ (seen anywhere)	(A1)	
		correct substitution	(A1)	
		$eg = \frac{1}{2} \times 10 \times 17.1695 \times \sin 65^{\circ}$		
		area = 77.8047		
		area = $77.8 \ (cm^2)$	A1 [3 mar	N2 ks]
			Total [6 mar	ks]
2.	(a)	(i) correct substitution eg $6 \times 2 + 3 \times 2 + 6 \times 1$	(A1)	
		$eg 0 \times 2 + 3 \times 2 + 0 \times 1$		
		$u \cdot v = 24$		N2
		-		N2
		$u \cdot v = 24$ (ii) correct substitution into magnitude formula for u or v	A1 (A1)	N2 N2
		(ii) correct substitution into magnitude formula for u or v eg $\sqrt{6^2 + 3^2 + 6^2}$, $\sqrt{2^2 + 2^2 + 1^2}$, correct value for $ v $	A1 (A1) A1	N2 N1
	(b)	$u \cdot v = 24$ (ii) correct substitution into magnitude formula for <i>u</i> or <i>v</i> <i>eg</i> $\sqrt{6^2 + 3^2 + 6^2}$, $\sqrt{2^2 + 2^2 + 1^2}$, correct value for $ v $ u = 9 (iii) $ v = 3$ correct substitution into angle formula	A1 (A1) A1 A1	N2 N1
	(b)	(ii) correct substitution into magnitude formula for u or v eg $\sqrt{6^2 + 3^2 + 6^2}$, $\sqrt{2^2 + 2^2 + 1^2}$, correct value for $ v $ u = 9 (iii) $ v = 3$	A1 (A1) A1 A1 [5 mar	N2 N1
	(b)	$u \cdot v = 24$ (ii) correct substitution into magnitude formula for u or v $eg \sqrt{6^2 + 3^2 + 6^2}, \sqrt{2^2 + 2^2 + 1^2}$, correct value for $ v $ u = 9 (iii) $ v = 3$ correct substitution into angle formula $eg \frac{24}{9 \times 3}, 0.\overline{8}$ $0.475882, 27.26604^{\circ}$	A1 (A1) A1 [5 mar. (A1)	N2 N1
	(b)	$u \cdot v = 24$ (ii) correct substitution into magnitude formula for <i>u</i> or <i>v</i> <i>eg</i> $\sqrt{6^2 + 3^2 + 6^2}$, $\sqrt{2^2 + 2^2 + 1^2}$, correct value for $ v $ u = 9 (iii) $ v = 3$ correct substitution into angle formula <i>eg</i> $\frac{24}{9 \times 3}$, $0.\overline{8}$	A1 (A1) A1 [5 mar. (A1)	N2 N1 ks] N2

-9- M15/5/MATME/SP2/ENG/TZ2/XX/M

3.	(a) (i	i) evidence of set up eg correct value for a , b or r	(M1)	
		a = 4.8, $b = 1.2$	A1A1	N3
		(ii) $r = 0.988064$ r = 0.988	A1	N1 [4 marks]
	(b)	correct substitution into their regression equation $eg = 4.8 \times 7 + 1.2$	(A1)	
		34.8 (millions of dollars) (accept 35 and 34800000)	A1	N2 [2 marks]
			Total	[6 marks]
4.		approach to find the required term	(M1)	
	eg	$\binom{8}{r}x^{8-r}k^r$, Pascal's triangle to 8^{th} row, $x^8 + 8x^7k + 28x^6k^2 +$		
		tifying correct term (may be indicated in expansion) $\begin{pmatrix} 8 \\ 9 \end{pmatrix}$	(A1)	
		$\binom{8}{2}x^6k^2, \binom{8}{6}x^6k^2, r = 2$	<i>(</i> 1 -1)	
		ng up equation in k with their coefficient/term $28k^2x^6 = 63x^6, \binom{8}{6}k^2 = 63$	(M1)	
	eg	$20k \ x - 05x$, $(6)^{k} = 05$		
	<i>k</i> = :	±1.5 (exact)	A1A1	N3 [5 marks]





– 10 –

6. **METHOD 1**

recognize that the distance walked each minute is a geometric sequence $eg = r = 0.9$, valid use of 0.9	(M1)
recognize that total distance walked is the sum of a geometric sequence	(M1)
$eg \qquad S_n, \ a\left(\frac{1-r^n}{1-r}\right)$	
correct substitution into the sum of a geometric sequence	(A1)
$eg = 80\left(\frac{1-0.9^n}{1-0.9}\right)$	
any correct equation with sum of a geometric sequence	(A1)

any correct equation with sum of a geometric sequence 1

eg
$$80\left(\frac{0.9^n-1}{0.9-1}\right) = 660, 1-0.9^n = \frac{66}{80}$$

attempt to solve their equation involving the sum of a GP (M1) eg graph, algebraic approach

n = 16.54290788	A1	
since $n > 15$ he will be late	R1 AG	NO

Note: Do not award the *R* mark without the preceding *A* mark.

continued...

– 12 – M15/5/MATME/SP2/ENG/TZ2/XX/M

Question 6 continued

METHOD 2

recognize that the distance walked each minute is a geometric sequence $eg = r = 0.9$, valid use of 0.9	(M1)
recognize that total distance walked is the sum of a geometric sequence eg S_n , $a\left(\frac{1-r^n}{1-r}\right)$	(M1)
correct substitution into the sum of a geometric sequence $eg = 80\left(\frac{1-0.9^n}{1-0.9}\right)$	(A1)
attempt to substitute $n = 15$ into sum of a geometric sequence eg S_{15}	(M1)
correct substitution eg $80\left(\frac{0.9^{15}-1}{0.9-1}\right)$	(A1)
$S_{15} = 635.287$	A1
since $S < 660$ he will not be there on time Note: Do not award the <i>R</i> mark without the preceding <i>A</i> mark.	R1 AG
METHOD 3 recognize that the distance walked each minute is a geometric sequence eg = r = 0.9, valid use of 0.9	(M1)
recognize that total distance walked is the sum of a geometric sequence eg S_n , $a\left(\frac{1-r^n}{1-r}\right)$	(M1)
listing at least 5 correct terms of the GP	(M1)
15 correct terms 80, 72, 64.8, 58.32, 52.488, 47.2392, 42.5152, 38.2637, 34.4373, 30.9936, 27.894 25.1048, 22.59436, 20.3349, 18.3014	A1 2,
attempt to find the sum of the terms	(M1)
eg S_{15} , $80 + 72 + 64.8 + 58.32 + 52.488 + + 18.301433$	
$S_{15} = 635.287$	A1
since $S < 660$ he will not be there on time	R1 AG

Note: Do not award the *R* mark without the preceding *A* mark.

[7 marks]

N0

N0

– 13 – M15/5/MATME/SP2/ENG/TZ2/XX/M

7.	attempt to set up equation eg $f = g$, $kx^2 + kx = x - 0.8$	(M1)	
	rearranging their equation to equal zero eg $kx^2 + kx - x + 0.8 = 0$, $kx^2 + x(k-1) + 0.8 = 0$	М1	
	evidence of discriminant (if seen explicitly, not just in quadratic formula) eg $b^2 - 4ac$, $\Delta = (k-1)^2 - 4k \times 0.8$, $D = 0$	(M1)	
	correct discriminant eg $(k-1)^2 - 4k \times 0.8, k^2 - 5.2k + 1$	(A1)	
	evidence of correct discriminant greater than zero eg $k^2 - 5.2k + 1 > 0$, $(k-1)^2 - 4k \times 0.8 > 0$, correct answer	R1	
	both correct values $eg = 0.2, 5$	(A1)	
	correct answer eq $k < 0.2, k \neq 0, k > 5$	A2	N3
	eg $k < 0.2, k \neq 0, k > 5$	[8	8 marks]

– 14 – M15/5/MATME/SP2/ENG/TZ2/XX/M

Section B

	(M1)	attempt to find intersection eg $f = g$
Na	A1A1	p = 1, q = 3
marks		
N2	A2	f'(p) = -1
marks		
	(A1)	(i) correct approach to find the gradient of the normal
		eg $m_1m_2 = -1$, $-\frac{1}{f'(p)}$, correct value of 1
		EITHER
	(M1)	attempt to substitute coordinates (in any order) and correct normal gradient to find c
		eg $3 = -\frac{1}{f'(p)} \times 1 + c$, $1 = 1 \times 3 + c$
	(A1)	<i>c</i> = 2
N2	A1	y = x + 2
		OR
	(M1)	attempt to substitute coordinates (in any order) and correct normal gradient into equation of a straight line
		eg $y-3 = -\frac{1}{f'(p)}(x-1), y-1 = 1 \times (x-3)$
		correct working
	(A1)	eg y = (x-1)+3
N2	A1	y = x + 2
N 1	A1	(ii) (0, 2)
marks		
	(M1)	appropriate approach involving subtraction
		eg $\int_{a}^{b} (L-g) dx$, $\int (3x^{2} - (x+2))$
	(A1)	substitution of their limits or function
		eg $\int_{0}^{p} (L-g) dx$, $\int ((x+2)-3x^{2})$
N2	A1	area=1.5
marks		

[3 marks] Total [13 marks] – 15 – M15/5/MATME/SP2/ENG/TZ2/XX/M

(a)	valid approach	(M1)	
	eg $\frac{L-\mu}{\sigma}$, using a value for σ , using 68% and 95%		
	correct working		
	P(-1 < Z < 2), correct probabilities $(0.6826+0.1359)$	(A1)	
	$P(50 - \sigma < L < 50 + 2\sigma) = 0.818594$		
	$P(50 - \sigma < L < 50 + 2\sigma) = 0.819$	A1	[3 ma
(b)	<i>z</i> = 1.95996	(A1)	
	correct equation	A1	
	eg $\frac{53.92 - 50}{\sigma} = 1.95996, \ \sigma = 2.00004$		
	$\sigma = 2.00$	AG	
			[2 ma
(c)	valid set up	М1	
	0.7		
	eg $P(L > t) = 0.75$, right tail,, 0.25		
	t = 48.6510		
	t = 48.7 (do not accept 48.5 from using $z = -0.75$)	A2	

continued...

– 16 – M15/5/MATME/SP2/ENG/TZ2/XX/M

Question 9 continued

(d)	(i)	correct approach eg from t to 50.1, $P(48.7 < X < 50.1)$, 0.269942	(A1)	
		recognize conditional probability (seen anywhere, including in correct working) eg $P(A B)$	R1	
		correct substitution eg $\frac{P(48.7 < X < 50.1)}{P(X > 48.7)}, \frac{0.269942}{0.75}$	(A1)	
		0.359923 0.360	A1	N3
	(ii)	$P(X \ge 2)$	(A1)	
		attempt to find $P(X \ge 2)$ eg $1-P(X = 0) - P(X = 1), P(X = 2) + P(X = 3) +$	(M1)	
		recognize binomial distribution eg $X \sim B(n, p)$	(M1)	
		0.923741 0.924	A1	N2

[8 marks]

Total [16 marks]

– 17 – M15/5/MATME/SP2/ENG/TZ2/XX/M

10.	(a)	area of $ABCD = AB^2$ (seen anywhere)	(A1)	
		choose cosine rule to find a side of the square eg $a^2 = b^2 + c^2 - 2bc\cos\theta$	(M1)	
		correct substitution (for triangle AOB) eg $r^2 + r^2 - 2 \times r \times r \cos \theta$, $OA^2 + OB^2 - 2 \times OA \times OB \cos \theta$	A1	
		correct working for AB ² eg $2r^2 - 2r^2 \cos \theta$	A1	
		$\operatorname{area} = 2r^2 \left(1 - \cos \theta\right)$	AG	NO
	No	ote: Award no marks if the only working is $2r^2 - 2r^2 \cos \theta$.		
			[·	4 marks]
	(b)	(i) $\frac{1}{2} \alpha r^2 (\operatorname{accept} 2r^2(1-\cos\alpha))$	A1	N1
		(ii) correct equation in one variable eg $2(1 - \cos \alpha) = \frac{1}{2}\alpha$	(A1)	
		$\alpha = 0.511024$ $\alpha = 0.511$ (accept $\theta = 0.511$)	A2	N2
		Note: Award A1 for $\alpha = 0.511$ and additional answers.	,	4
			14	4 marks]

continued...

– 18 – M15/5/MATME/SP2/ENG/TZ2/XX/M

Question 10 continued

(c)	Note: In this part, accept θ instead of β , and the use of equations instead of inequalities in the working.	
	attempt to find R eg subtraction of areas, square – segment	(M1)
	correct expression for segment area	(A1)

$$eg \quad \frac{1}{2}\beta r^2 - \frac{1}{2}r^2\sin\beta$$

correct expression for R

eg
$$2r^2(1-\cos\beta)-\left(\frac{1}{2}\beta r^2-\frac{1}{2}r^2\sin\beta\right)$$

correct inequality

eg
$$2r^2(1-\cos\beta) - \left(\frac{1}{2}\beta r^2 - \frac{1}{2}r^2\sin\beta\right) > 2\left(\frac{1}{2}\beta r^2\right)$$

correct inequality in terms of angle only

eg
$$2(1-\cos\beta)-\left(\frac{1}{2}\beta-\frac{1}{2}\sin\beta\right)>\beta$$

attempt to solve their inequality, must represent *R*> twice sector (M1) sketch, one correct value eg

Note: Do not award the second (M1) unless the first (M1) for attempting to find R has been awarded.

both correct values 1.30573 and 2.67369

correct inequality $1.31 < \beta < 2.67$

[8 marks]

N3

Total [16 marks]

A1

(A1)

A1

(A1)

(A1)