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Markscheme

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Mathematical studies

Standard level

Paper 2

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Paper 2 Markscheme
Instructions to Examiners

Notes: **If in doubt about these instructions or any other marking issues, contact your team leader for clarification.**

1   Abbreviations

M   Marks awarded for **Method**

A   Marks awarded for an **Answer** or for **Accuracy**

R   Marks awarded for clear **Reasoning**

G   Marks awarded for correct solutions obtained from a **Graphic Display Calculator**, when no working shown.

AG   **Answer Given** in the question and consequently, marks not awarded.

ft   Marks that can be awarded as **follow through** from previous results in the question.

2   Method of Marking

(a)   All marking must be done in RM Assessor using the mathematical studies annotations and in accordance with the current document for guidance in e-marking Mathematical Studies SL. It is essential that you read this document before you start marking.

(b)   If a question part is completely correct use the number tick annotations to award full marks. If a part is completely wrong use the *A0* annotation, otherwise full annotations must be shown.

(c)   Working crossed out by the candidate should not be awarded any marks.

(d)   Where candidates have written two solutions to a question, only the first solution should be marked.

(e)   If correct working results in a correct answer but then further working is developed, indicating a lack of mathematical understanding full marks should **not** be awarded. In most such cases it will be a single final answer mark that is lost. An exception to this may be in numerical answers, where a correct exact value is followed by an incorrect decimal.

Example:

	Correct answer seen	Further working seen	Action
1.	$8\sqrt{2}$	5.65685... *(incorrect decimal value)*	Award the final *(A1)* *(ignore the further working)*
2.	$(x-6)(x+1)$	$x=6$ and -1	Do **not** award the final *(A1)*

Example: Calculate the gradient of the line passing through the points $(5,3)$ and $(0,9)$.

Markscheme	Candidates' Scripts	Marking
$\dfrac{9-3}{0-5}$ *(M1)* *Award* ***(M1)*** *for correct substitution in gradient formula* $=-\dfrac{6}{5}$ *(A1)*	(i) $\dfrac{9-3}{0-5}=-\dfrac{6}{5}$ Gradient is $=-\dfrac{6}{5}$ *(There is clear understanding of the gradient.)* $y=-\dfrac{6}{5}x+9$ (ii) $\dfrac{9-3}{0-5}=-\dfrac{6}{5}$ $y=-\dfrac{6}{5}x+9$ *(There is confusion about what is required.)*	*(M1)* *(A1)* *(M1)* *(A0)*

3 **Follow-through (ft) Marks**

Errors made at any step of a solution affect all working that follows. To limit the severity of the penalty, **follow through (ft)** marks can be awarded. Markschemes will indicate where it is appropriate to apply follow through in a question with **'(ft)'**.

(a) Follow through applies only from one part of a question to a subsequent part of the question. Follow through does not apply within the same part.

(b) If an answer resulting from follow through is extremely unrealistic (*eg*, negative distances or incorrect by large order of magnitude) then the final **A** mark should not be awarded.

(c) If a question is transformed by an error into a **different**, **much simpler question** then follow through may not apply.

(d) To award follow through marks for a question part, **there must be working present for that part**. An isolated follow through answer, without working is regarded as incorrect and receives no marks **even if it is approximately correct**.

(e) The exception to the above would be in a question which is testing the candidate's use of the GDC, where working will not be expected. **The markscheme will clearly indicate where this applies.**

(f) Inadvertent use of radians will be penalized the first time it occurs. The markscheme will give clear instructions to ensure that only one mark per paper can be lost for the use of radians.

Example: Finding angles and lengths using trigonometry

Markscheme	Candidates' Scripts	Marking
(a) $\dfrac{\sin A}{3} = \dfrac{\sin 30}{4}$ **(M1)(A1)** *Award **(M1)** for substitution in sine rule formula, **(A1)** for correct substitutions.* $A = 22.0°\ (22.0243\ldots)$ **(A1)(G2)**	(a) $\dfrac{\sin A}{4} = \dfrac{\sin 30}{3}$ $A = 41.8°$	**(M1)(A0)** *(use of sine rule but with wrong values)* **(A0)** **(Note:** *the 2nd **(A1)** here was not marked **(ft)** and cannot be awarded because there was an earlier error in the **same** question part.)*
(b) $x = 7\tan(22.0243\ldots°)$ **(M1)** $= 2.83\,(2.83163\ldots)$ **(A1)(ft)**	(b) case (i) $x = 7\tan 41.8°$ $= 6.26$ ***but*** case (ii) $\quad\quad 6.26$	**(M1)** **(A1)(ft)** **(G0)** *since no working shown*

4   Using the Markscheme

(a)   *A* marks are **dependent** on the preceding *M* mark being awarded, it is **not** possible to award *(M0)(A1)*. Once an *(M0)* has been awarded, all subsequent *A* marks are lost in that part of the question, even if calculations are performed correctly, until the next *M* mark.
The only exception to this will be for an answer where the accuracy is specified in the question – see section 5.

(b)   *A* marks are **dependent** on the *R* mark being awarded, it is **not** possible to award *(A1)(R0)*. Hence the *(A1)* cannot be awarded for an answer which is correct when no reason or the wrong reason is given.

(c)   In paper 2 candidates are expected to demonstrate their ability to communicate mathematics using appropriate working. Answers which are correct but not supported by adequate working will **not always receive full marks**, these unsupported answers are designated *G* in the mark scheme as an alternative to the full marks. Example *(M1)(A1)(A1)(G2)*.

Example: Using trigonometry to calculate an angle in a triangle.

Markscheme	Candidates' Scripts	Marking
(a) $\dfrac{\sin A}{3} = \dfrac{\sin 30}{4}$ *(M1)(A1)* *Award (M1) for substitution in sine rule formula, (A1) for correct substitutions.* $A = 22.0°$ $(22.0243…)$ *(A1)(G2)*	(i) $\dfrac{\sin A}{3} = \dfrac{\sin 30}{4}$ $A = 22.0°$ (ii) $A = 22.0°$ **Note: G** *marks are used only if no working has been shown and the answer is correct.*	*(M1)(A1)* *(A1)* *(G2)*

(d)   **Alternative methods** may not always be included. Thus, if an answer is wrong then the working must be carefully analysed in order that marks are awarded for a different method consistent with the markscheme.
Where alternative methods for complete questions are included in the markscheme, they are indicated by '**OR**' *etc*.

(e)   Unless the question specifies otherwise, accept **equivalent forms**. For example: $\dfrac{\sin\theta}{\cos\theta}$ for $\tan\theta$.

On the markscheme, these equivalent numerical or algebraic forms will sometimes be written in brackets after the required answer.
Where numerical answers are required as the final answer to a part of a question in the markscheme, the scheme will show, in order:
the 3 significant figure answer worked through from full calculator display;
the exact value $\left(\text{for example } \dfrac{2}{3} \text{ if applicable}\right)$;

the full calculator display in the form $2.83163…$ as in the example above.
Where answers are given to 3 significant figures and are then used in subsequent parts of the question leading to a **different** 3 significant figure answer, these solutions will also be given.

(f)   As this is an international examination, all valid **alternative forms of notation** should be accepted. Some examples of these are:

Decimal points: 1.7; $1'7$; $1 \cdot 7$; $1,7$.

Decimal numbers less than 1 may be written with or without a leading zero: 0.49 or $.49$.

Different descriptions of an interval: $3 < x < 5$; $(3, 5)$; $] \, 3, 5 \, [$.

Different forms of notation for set properties (*e.g.* complement): A'; $\overline{A}$; A^c; $U - A$; $(A$; $U \setminus A$.

Different forms of logic notation: $\neg p$; p' ; $\tilde{p}$; $\overline{p}$; $\sim p$; $- p$.
$$p \Rightarrow q \, ; \, p \rightarrow q \, ; \, q \Leftarrow p \, .$$

Significance level may be written as α .

(g)   Discretionary marks: There will be very rare occasions where the markscheme does not cover the work seen. In such cases the annotation DM should be used to indicate where an examiner has used discretion. Discretion should be used sparingly and if there is doubt an exception should be raised through RM Assessor to the team leader.

As with previous sessions there will be no whole paper penalty marks for accuracy AP, financial accuracy FP and units UP. Instead these skills will be assessed in particular questions and the marks applied according to the rules given in sections 5, 6 and 7 below.

5   Accuracy of Answers

Incorrect accuracy should be penalized once only in each question according to the rules below.

Unless otherwise stated in the question, all numerical answers should be given exactly or correct to 3 significant figures.

1.   If the **candidate's answer** is seen to 4 sf or greater **and** would round to the required 3 sf answer, then award **(A1)** and ignore subsequent rounding.

2.   If the candidate's unrounded answer is **not** seen then award **(A1)** if the answer given is **correctly** rounded to 2 or more significant figures, otherwise **(A0)**.

Note: If the candidate's unrounded answer is **not** seen and the answer is given correct to 1 sf (correct or not), the answer will be considered wrong and will not count as incorrect accuracy. If this answer is used in subsequent parts, then working must be shown for further marks to be awarded.

3.   If a correct 2 sf answer is used in subsequent parts, then working **must** be shown for further marks to be awarded. (This treatment is the same as for following through from an incorrect answer.)

These 3 points (see numbers in superscript) have been summarized in the table below and illustrated in the examples following.

	If candidates final answer is given …					
	Exact or to 4 or more sf (and would **round to the correct 3 sf**)	**Correct to 3 sf**	**Incorrect to 3 sf**	Correct to 2 sf [3]	Incorrect to 2 sf	Correct or incorrect to 1 sf
Unrounded answer seen[1]	Award the final **(A1)** irrespective of correct or incorrect rounding					
Unrounded answer not seen[2]	**(A1)**	**(A1)**	**(A0)**	**(A1)**	**(A0)**	**(A0)**
Treatment of subsequent parts	As per MS		Treat as follow through, only if working is seen.[3]			

Examples:

Markscheme	Candidates' Scripts		Marking
9.43 (9.43398…) **(A1)**	(i)	9.43398… is seen followed by 9; 9.4; 9.43; 9.434 *etc.* (correctly rounded)	**(A1)**
	(ii)	9.43398… is seen followed by 9.433; 9.44 *etc.* (incorrectly rounded)	**(A1)**
	(iii)	9.4	**(A1)**
	(iv)	9	**(A0)** *(correct to 1 sf)*
	(v)	9.3	**(A0)** *(incorrectly rounded to 2 sf)*
	(vi)	9.44	**(A0)** *(incorrectly rounded to 3 sf)*

Markscheme	Candidates' Scripts		Marking
7.44 (7.43798…) **(A1)**	(i)	7.43798… is seen followed by 7; 7.4; 7.44; 7.438 *etc.* (correctly rounded)	**(A1)**
	(ii)	7.43798… is seen followed by 7.437; 7.43 *etc.* (incorrectly rounded)	**(A1)**
	(iii)	7.4	**(A1)**
	(iv)	7	**(A0)** *(correct to 1 sf)*
	(v)	7.5	**(A0)** *(incorrectly rounded to 2 sf)*
	(vi)	7.43	**(A0)** *(incorrectly rounded to 3 sf)*

Example: ABC is a right angled triangle with angle $ABC = 90°$, $AC = 32 \text{ cm}$ and $AB = 30 \text{ cm}$. Find (a) the length of BC, (b) The area of triangle ABC.

Markscheme	Candidates' Scripts	Marking
(a) $BC = \sqrt{32^2 - 30^2}$ **(M1)** *Award **(M1)** for correct substitution in Pythagoras' formula* $= 11.1 \left(\sqrt{124}, 11.1355...\right)(\text{cm})$ **(A1)**	(a) $BC = \sqrt{32^2 - 30^2}$ **(M1)** $11 (\text{cm})$ **(A1)** *(2 sf answer only seen, but correct)*	
(b) $\text{Area} = \frac{1}{2} \times 30 \times 11.1355...$ **(M1)** *Award **(M1)** for correct substitution in area of triangle formula* $= 167(167.032...)(\text{cm}^2)$ **(A1)(ft)**	(b) case (i) $\text{Area} = \frac{1}{2} \times 30 \times 11$ **(M1)** *(working shown)* $= 165 (\text{cm}^2)$ **(A1)(ft)** case (ii) $= 165 (\text{cm}^2)$ **(M0)(A0)(ft)** *(No working shown, the answer 11 is treated as a ft, so no marks awarded here)*	

Certain answers obtained from the GDC are worth 2 marks and working will not be seen. In these cases only one mark should be lost for accuracy.

eg, Chi-squared, correlation coefficient, mean

Markscheme	Candidates' Scripts	Marking
Chi-squared $7.68 (7.67543…)$ **(A2)**	(a) 7.7	**(G2)**
	(b) 7.67	**(G1)**
	(c) 7.6	**(G1)**
	(d) 8	**(G0)**
	(e) 7	**(G0)**
	(e) 7.66	**(G0)**

Regression line

Markscheme	Candidates' Scripts		Marking
$y = 0.888x + 13.5$ **(A2)** ($y = 0.887686\ldots x + 13.4895\ldots$) If an answer is not in the form of an equation award at most **(A1)(A0)**.	(a)	$y = 0.89x + 13$	**(G2)** *(both accepted)*
	(b)	$y = 0.88x + 13$	**(G1)** *(one rounding error)*
	(c)	$y = 0.88x + 14$	**(G1)** *(rounding error repeated)*
	(d) (i)	$y = 0.9x + 13$	
	(ii)	$y = 0.8x + 13$	**(G1)** *(1 sf not accepted)*
	(e)	$0.88x + 13$	**(G0)** *(one rounding error and not an equation)*

Maximum/minimum/points of intersection

Markscheme	Candidates' Scripts		Marking
$(2.06, 4.49)$ **(A1)(A1)** $(2.06020\ldots, 4.49253\ldots)$	(a)	$(2.1, 4.5)$	**(A1)(A1)** *(both accepted)*
	(b)	$(2.0, 4.4)$	**(A1)** *(same rounding error twice)*
	(c)	$(2.06, 4.4)$	**(A1)** *(one rounding error)*
	(d)	$(2, 4.4)$	**(A0)** *(1sf not accepted, one rounding error)*

Rounding of an exact answer to 3 significant figures **should be accepted if performed correctly**. Exact answers such as $\dfrac{1}{4}$ can be written as decimals to fewer than 3 significant figures if the result is still exact. Reduction of a fraction to its lowest terms is **not** essential, however where an answer simplifies to an integer this is expected. Fractions that include a decimal in the numerator and/or the denominator are acceptable for showing correct substitution, but not as a final answer.

Ratios of π and answers taking the form of square roots of integers or any rational power of an integer (*eg,* $\sqrt{13}, 2^{\frac{2}{3}}, \sqrt[4]{5}$,) may be accepted as exact answers. All other powers (*eg,* of non-integers) and values of transcendental functions such as sine and cosine must be evaluated.

If the level of accuracy is specified in the question, a mark will be allocated for giving the answer to the required accuracy. In **all** such cases the final mark is not awarded if the rounding does not follow the instructions given in the question. A mark for specified accuracy can be regarded as a **(ft)** mark regardless of an immediately preceding **(M0)**.

6 **Level of accuracy in finance questions**

The accuracy level required for answers will be specified in all questions involving money. This will usually be either whole units or two decimal places. The first answer not given to the specified level of accuracy will not be awarded the final **A** mark. The markscheme will give clear instructions to ensure that only one mark per paper can be lost for incorrect accuracy in a financial question.

Example: A financial question demands accuracy correct to 2 dp.

Markscheme	Candidates' Scripts	Marking
$231.62 (231.6189) **(A1)**	(i) 231.6	**(A0)**
	(ii) 232	**(A0)** *(Correct rounding to incorrect level)*
	(iii) 231.61	**(A0)**
	(iv) 232.00	**(A0)** *(Parts (iii) and (iv) are both incorrect rounding to correct level)*

7 **Units in answers**

There will be specific questions for which the units are required and this will be indicated clearly in the markscheme. The first correct answer with no units or incorrect units will not be awarded the final **A** mark. The markscheme will give clear instructions to ensure that only one or two mark per paper can be lost for lack of units or incorrect units.
The units are considered only when the numerical answer is awarded **(A1)** under the accuracy rules given in Section 5.

Example:

Markscheme	Candidates' Scripts	Marking
(a) $37000 \, \text{m}^2$ **(A1)**	(a) $36000 \, \text{m}^2$	**(A0)** *(Incorrect answer so units not considered)*
(b) $3200 \, \text{m}^3$ **(A1)**	(b) $3200 \, \text{m}^2$	**(A0)** *(Incorrect units)*

If no method is shown and the answer is correct but with incorrect or missing units award G marks with a one mark penalty.

8 **Graphic Display Calculators**

Candidates will often be obtaining solutions directly from their calculators. They must use mathematical notation, not calculator notation. No method marks can be awarded for incorrect answers supported only by calculator notation. The comment 'I used my GDC' cannot receive a method mark.

1. (a) (i) 14   **(G1)**

   (ii) 54   **(G1)**

   (iii) 0.5   **(G2)**

                                                                                                         [4 marks]

   (b) (i) $m = 0.875$, $c = 41.75$ $\left(m = \dfrac{7}{8},\ c = \dfrac{167}{4} \right)$ **(A1)(A1)**

> **Note:** Award **(A1)** for 0.875 seen. Award **(A1)** for 41.75 seen.
> If 41.75 is rounded to 41.8 do not award **(A1)**.

   (ii) $y = 0.875(14) + 41.75$ **(M1)**

> **Note:** Award **(M1)** for their correct substitution into their regression line.
> Follow through from parts (a)(i) and (b)(i).

   $= 54$
   and so the mean point lies on the regression line   **(A1)**

   (accept 54 is $\overline{y}$, the mean value of the y data)

> **Note:** Do not award **(A1)** unless the conclusion is explicitly stated and the 54 seen.
> The **(A1)** can be awarded **only** if their conclusion is consistent with their
> equation and it lies on the line.
> The use of 41.8 as their c value precludes awarding **(A1)**.

   OR

   $54 = 0.875(14) + 41.75$ **(M1)**

   $54 = 54$

> **Note:** Award **(M1)** for their correct substitution into their regression line.
> Follow through from parts (a)(i) and (b)(i).

   and so the mean point lies on the regression line   **(A1)**

> **Note:** Do not award **(A1)** unless the conclusion is explicitly stated. Follow
> through from part (a). The use of 41.8 as their c value precludes the
> awarding of **(A1)**.

                                                                                                         [4 marks]

Question 1 continued

(c) (i) $y = 0.875(17) + 41.75$ **(M1)**

> **Note:** Award **(M1)** for correct substitution into their regression line.

$= 56.6 \quad (56.625)$ **(A1)(ft)(G2)**

> **Note:** Follow through from part (b)(i).

(ii) the estimate is valid **(A1)**
since this is interpolation **and** the correlation coefficient is large enough **(R1)**

OR

the estimate is not valid **(A1)**
since the correlation coefficient is not large enough **(R1)**

> **Note:** Do not award **(A1)(R0)**. The **(R1)** may be awarded for reasoning based on strength of correlation, but do not accept "correlation coefficient is not strong enough" or "correlation is not large enough".
> Award **(A0)(R0)** for this method if no numerical answer to part (a)(iii) is seen.

[4 marks]

(d) $\left| \dfrac{56.6 - 65}{65} \right| \times 100$ **(M1)**

> **Note:** Award **(M1)** for correct substitution into percentage error formula. Follow through from part (c)(i).

$= 12.9 \; (\%) \, (12.9230\ldots)$ **(A1)(ft)(G2)**

> **Note:** Follow through from part (c)(i). Condone use of percentage symbol.
> Award **(G0)** for an answer of -12.9 with no working.

[2 marks]

Total [14 marks]

2.   (a)   (i) $10 + 40 + 28 + 17$ **(M1)**
                  $= 95$ **(A1)(G2)**

         (ii) $20 + 12$ **(M1)**
                  $= 32$ **(A1)(G2)**

         (iii) $12 + 40$ **(M1)**
                  $= 52$ **(A1)(G2)**

Note: Award **(M1)** for each correct sum (for example: $10 + 40 + 28 + 17$) seen.

                                                                                          [6 marks]

(b)   (i)   78   **(A1)**

      (ii) 12   **(A1)**
                                                                                          [2 marks]

(c)   (i) $\dfrac{100}{160}$ $\left(\dfrac{5}{8},\ 0.625,\ 62.5\,\% \right)$ **(A1)(A1) (G2)**

      (ii) $\dfrac{42}{160}$ $\left(\dfrac{21}{80},\ 0.263\ (0.2625),\ 26.3\,\%\ (26.25\,\%) \right)$ **(A1)(A1) (G2)**

      (iii) $\dfrac{50}{70}$ $\left(\dfrac{5}{7},\ 0.714\ (0.714285...),\ 71.4\,\%\ (71.4285...\,\%) \right)$ **(A1)(A1) (G2)**

Note: Throughout part (c), award **(A1)** for correct numerator, **(A1)** for correct denominator. All answers must be probabilities to award **(A1)**.

                                                                                          [6 marks]

                                                                                          Total [14 marks]

3. (a) (i)   60   **(A2)**

(ii) $68 - 48$ **(A1)(M1)**

> **Note:** Award **(A1)** for two correct quartiles seen, **(M1)** for finding the difference between their two quartiles.

$= 20$ **(A1)(ft)(G3)**

[5 marks]

(b) $3200 - 350 = 2850$ **(M1)**

> **Note:** Award **(M1)** for 2850 seen. Follow through from their 3200.

(Top grade boundary $=$) 76   **(A1)ft(G2)**

[2 marks]

(c) (i) $60 < x \leq 80$ **(A1)(A1)**

> **Note:** Award **(A1)** for 60, 80 seen, **(A1)** for correct strict and weak inequalities.

(ii)   70   **(A1)(ft)**

> **Note:** Follow through from part (c)(i).

[3 marks]

(d) (i)   57.2 (57.1875)   **(A2)(ft)**

> **Note:** Follow through from part (c)(ii).

(ii)   18.496   **(A1)**

> **Note:** Award **(A0)** for 18.499.

[3 marks]

(e) $57.2 - 18.5$ **(M1)**
$= 38.7$ (38.6918…)   **(A1)(ft)**

> **Note:** Award **(M1)** for subtracting their standard deviation from their mean. Follow through from part (d) even if no working is shown.
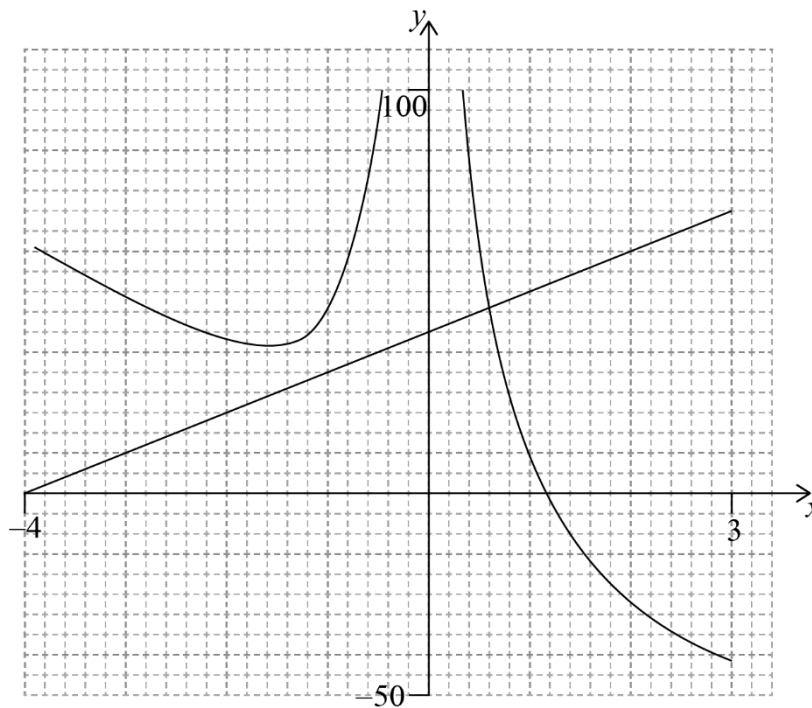
450 (students)   **(A1)(ft)(G2)**

> **Note:** Accept any answer within the range of 450 to 475, inclusive. Follow through from part (d), adjusting the acceptable range as necessary.

[3 marks]

Total [16 marks]

4. (a)

(A1)(A1)(A1)(A1)

Note:	Award *(A1)* for axis labels and some indication of scale; accept y or $f(x)$. Use of graph paper is not required. If no scale is given, assume the given window for zero and minimum point. Award *(A1)* for smooth curve with correct general shape. Award *(A1)* for x-intercept closer to y-axis than to end of sketch. Award *(A1)* for correct local minimum with x-coordinate closer to y-axis than end of sketch and y-coordinate less than half way to top of sketch. Award at most *(A1)(A0)(A1)(A1)* if the sketch intersects the y-axis or if the sketch curves away from the y-axis as x approaches zero.

[4 marks]

continued…

Question 4 continued

(b) (i) 1.19 $(1.19055\ldots)$ **(A1)**

> **Note:** Accept an answer of $(1.19,\, 0)$.
> Do not follow through from an incorrect sketch.

(ii) $(-1.5,\, 36)$ **(A1)(A1)**

> **Note:** Award **(A0)(A1)** if parentheses are omitted.
> Accept $x = -1.5$, $y = 36$.

(iii) $y = -9.25x + 20.3$ $(y = -9.25x + 20.25)$ **(A1)(A1)**

> **Note:** Award **(A1)** for $-9.25x$, award **(A1)** for $+20.25$, award a
> maximum of **(A0)(A1)** if answer is not an equation.

[5 marks]

(c) correct line, $y = 10x + 40$, seen on sketch **(A1)(A1)**

> **Note:** Award **(A1)** for straight line with positive gradient, award **(A1)** for x-intercept
> and y-intercept in approximately the correct positions. Award at most **(A0)(A1)**
> if ruler not used. If the straight line is drawn on different axes to part (a), award
> at most **(A0)(A1)**.

[2 marks]

(d) 0.684 $(0.68362\ldots)$ **(G2)**

> **Note:** Award at most **(G1)** if y-value (46.8) is also given.
> Award **(G1)** for 0.683.

[2 marks]

Total [13 marks]

5.   **units are required in part (b)**

(a) $\dfrac{\sin 43.7°}{100} = \dfrac{\sin \mathrm{BAC}}{50}$ **(M1)(A1)**

> **Note:**   Award **(M1)** for substitution into sine rule formula, **(A1)** for correct substitution.

$\mathrm{BAC} = 20.2087… = 20.2°$ **(A1)(AG)**

> **Note:**   Award **(A1)** only if both the correct unrounded and rounded answers are seen.

[3 marks]

(b) $\dfrac{1}{2}(100)(50)\sin(116.1)$ **(A1)(M1)(A1)**

> **Note:**   Award **(A1)** for 116.1 or unrounded value or 116 seen, **(M1)** for substitution into area of triangle formula, **(A1)** for correct substitution.

$= 2250\,\mathrm{m}^2 \quad (2245.06…\,\mathrm{m}^2)$ **(A1)(G3)**

> **Note:**   The answer is $2250\,\mathrm{m}^2$; the units are required. Use of $20.2087…$ gives $2245.23…$.

[4 marks]

(c) $\dfrac{100}{\sin 43.7} = \dfrac{\mathrm{AC}}{\sin(116.1)}$ **(M1)(A1)(ft)**

> **Note:**   Award **(M1)** for substitution into sine rule formula, **(A1)(ft)** for their correct substitution. Follow through from their 116.1.

$\mathrm{AC} = 130\,(\mathrm{m}) \quad (129.982…\,(\mathrm{m}))$ **(A1)(ft)(G2)**

> **Note:**   Use of $20.2087…$ gives $129.992…$.

continued…

Question 5 continued

OR

$$AC^2 = 100^2 + 50^2 - 2(100)(50)\cos(116.1)$$ *(M1)(A1)(ft)*

> **Note:** Award *(M1)* for substitution into cosine rule formula, *(A1)(ft)* for their correct substitution. Follow through from their 116.1.

$$AC = 130\,(m)\quad(129.997\ldots(m))$$ *(A1)(ft)(G2)*

> **Note:** Award *(M1)* for substitution into cosine rule formula, *(A1)(ft)* for their correct substitution.

[3 marks]

(d) $$BM^2 = 100^2 + 65^2 - 2(100)(65)\cos(20.2°)$$ *(M1)(A1)(ft)*

OR

$$BM^2 = 50^2 + 65^2 - 2(50)(65)\cos(43.7°)$$ *(M1)(A1)(ft)*

> **Note:** Award *(M1)* for substitution into cosine rule formula, *(A1)(ft)* for correct substitution, including half their AC.

$$BM = 45.0\quad(44.9954\ldots\ \textbf{OR}\ 45.0079\ldots)$$ *(A1)(ft)*

> **Note:** Use of $20.2052\ldots$ gives 45. Award *(G2)* for 45.0 seen without working.

$$\tan(TMB) = \frac{25}{their\ BM}$$ *(M1)*

> **Note:** Award *(M1)* for correct substitution into tangent formula.

$$T\hat{M}B = 29.1°\ (29.0546\ldots°)$$ *(A1)(ft)(G4)*

> **Note:** Follow through within part (d) provided their BM is seen. Use of 44.9954 gives $29.0570\ldots$ and use of $45.0079\ldots$ gives $29.0503\ldots$. Follow through from their AC in part (c).

[5 marks]

Total [15 marks]

6. (a) $36 \times 12 + 2(9 \times 12) + 2(9 \times 36)$ **(M1)**

> **Note:** Award **(M1)** for correct substitution into surface area of cuboid formula.

   $= 1300\,(\text{cm}^2)\ \left(1296\,(\text{cm}^2)\right)$ **(A1)(G2)**

[2 marks]

(b) $36 \times 9 \times 12$ **(M1)**

> **Note:** Award **(M1)** for correct substitution into volume of cuboid formula.

   $= 3890\,(\text{cm}^3)\ \ (3888\,(\text{cm}^3))$ **(A1)(G2)**

[2 marks]

(c) $3x \times x \times y = 3888$ **(M1)**

> **Note:** Award **(M1)** for correct substitution into volume of cuboid formula
>   and equated to 3888.

   $x^2 y = 1296$ **(A1)(G2)**

> **Note:** Award **(A1)** for correct fully simplified volume of cuboid.
>   Accept $y = \dfrac{1296}{x^2}$.

[2 marks]

(d) $(A =)\ 3x^2 + 2(xy) + 2(3xy)$ **(M1)**

> **Note:** Award **(M1)** for correct substitution into surface area of cuboid formula.

   $(A =)\ 3x^2 + 8xy$ **(A1)(G2)**

> **Note:** Award **(A1)** for correct simplified surface area of cuboid formula.

[2 marks]

(e) $A = 3x^2 + 8x\left(\dfrac{1296}{x^2}\right)$ **(A1)(ft)(M1)**

> **Note:** Award **(A1)(ft)** for correct rearrangement of their part (c) seen (rearrangement
>   may be seen in part(c)), award **(M1)** for substitution of their part (c) into their
>   part (d) but only if this leads to the given answer, which must be shown.

   $A = 3x^2 + \dfrac{10368}{x}$ **(AG)**

[2 marks]

Question 6 continued

(f) $\left(\dfrac{\mathrm{d}A}{\mathrm{d}x}\right) = 6x - \dfrac{10368}{x^2}$ **(A1)(A1)(A1)**

> **Note:** Award **(A1)** for $6x$, **(A1)** for -10368, **(A1)** for x^{-2}. Award a maximum of **(A1)(A1)(A0)** if any extra terms seen.

[3 marks]

(g) $6x - \dfrac{10368}{x^2} = 0$ **(M1)**

> **Note:** Award **(M1)** for equating their $\dfrac{\mathrm{d}A}{\mathrm{d}x}$ to zero.

$6x^3 = 10368$ **OR** $6x^3 - 10368 = 0$ **OR** $x^3 - 1728 = 0$ **(M1)**

> **Note:** Award **(M1)** for correctly rearranging their equation so that fractions are removed.

$x = \sqrt[3]{1728}$ **(A1)**

$x = 12\,(\mathrm{cm})$ **(AG)**

> **Note:** The **(AG)** line must be seen for the final **(A1)** to be awarded. Substituting $x = 12$ invalidates the method, award a maximum of **(M1)(M0)(A0)**.

[3 marks]

(h) $\left(3(12)^2 + \dfrac{10368}{12}\right) \times 4$ **(M1)**

> **Note:** Award **(M1)** for substituting 12 into the area formula and for multiplying the area formula by 4.

$= 5180\,(\mathrm{JPY})$ $(5184\,(\mathrm{JPY}))$ **(A1)(G2)**

[2 marks]

Total [18 marks]