



# Markscheme

November 2018

Physics

Higher level

Paper 3

26 pages

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**Section A**

Question		Answers	Notes	Total
1.	a	$m^{\frac{3}{2}}$ ✓	Accept other power of tens multiples of $m^{\frac{3}{2}}$ , eg: $cm^{\frac{3}{2}}$ .	1
1.	b	measured uncertainties «for one oscillation and for 20 oscillations» are the same/similar/OWTTE <b>OR</b> % uncertainty is less for 20 oscillations than for one ✓ dividing «by 20» / finding mean reduces the random error ✓		2

(continued...)

(Question 1 continued)

Question			Answers	Notes	Total
1.	c	i	<p>Straight line touching at least 3 points drawn across the range ✓</p>	<p><i>It is not required to extend the line to pass through the origin.</i></p>	1
1.	c	ii	<p>theory predicts proportional relation «<math>T \propto \frac{1}{d}</math>, slope = <math>Td = \frac{c}{\sqrt{g}}</math> = constant » ✓</p> <p>the graph is «straight» line <u>through the origin</u> ✓</p>		2

(continued...)



Question		Answers	Notes	Total
2.	a	to provide a constant heating rate / power <b>OR</b> to have $m$ proportional to $t$ ✓		1
2.	b	due to heat losses « $V/t$ is larger than heat into liquid» ✓ $L_v$ calculated will be larger ✓		2
2.	c	heat losses will be similar / the same for both experiments <b>OR</b> heat loss presents systematic error ✓ taking the difference cancels/eliminates the effect of these losses <b>OR</b> use a graph to eliminate the effect ✓		2

**Section B**

**Option A — Relativity**

Question			Answers	Notes	Total
3.	a		a set of rulers and clocks / set of coordinates to record the position and time of events ✓		1
3.	b	i	<p><b>ALTERNATIVE 1:</b>                      the time in frame S' is <math>t' = \frac{L}{c}</math> ✓                      but time is absolute in Galilean relativity so is the same in S ✓</p> <p><b>ALTERNATIVE 2:</b>                      In frame S, light rays travel at <math>c + v</math> ✓</p> <p>so <math>t = \frac{L}{(c+v)-v} = \frac{L}{c}</math> ✓</p>	<i>In Alternative 1, they must refer to S'</i>	2
3.	b	ii	<p><math>x = x' + vt</math> and <math>x' = L</math> ✓                      «substitution to get answer»</p>		1

Question			Answers	Notes	Total
4.	a		$\frac{0.82c + 0.40c}{1 + \frac{0.82c \times 0.40c}{c^2}} \checkmark$ $0.92c \checkmark$		2
4.	b	i	$\Delta t' = \frac{120}{0.40c} \checkmark$ $\Delta t' = 1.0 \times 10^{-6} \text{ «s» } \checkmark$		2
4.	b	ii	$\gamma = \left\langle \frac{1}{\sqrt{1 - 0.82^2}} \right\rangle = 1.747 \checkmark$ $\Delta t = \left\langle \gamma \left( \Delta t' + \frac{v \Delta x'}{c^2} \right) \right\rangle = 1.747 \times \left( 1.0 \times 10^{-6} + \frac{0.82c \times 120}{c^2} \right)$ <p><b>OR</b></p> $\Delta t = \frac{120}{1.747 \times (0.92 - 0.82)c} \checkmark$ $2.3 \times 10^{-6} \text{ «s» } \checkmark$		3



Question			Answers	Notes	Total
5.	a	i	$\gamma = \left\langle \frac{1}{\sqrt{1-0.745^2}} \right\rangle = 1.499 \checkmark$ $x' = \left\langle \gamma(x - vt) \right\rangle = 1.499 \times (1.0 - 0) \checkmark$ $\left\langle x' = 1.5 \text{ m} \right\rangle$		2
5.	a	ii	$t' = \left\langle \gamma \left( t - \frac{vx}{c^2} \right) \right\rangle = 1.499 \times \left( 0 - \frac{0.745c \times 1}{c^2} \right) \left\langle = -\frac{1.11}{c} \right\rangle$ $\left\langle ct' = -1.1 \text{ m} \right\rangle$ <p><b>OR</b></p> $\text{using spacetime interval } 0 - 1^2 = (ct')^2 - 1.5^2 \Rightarrow \left\langle ct' = -1.11 \right\rangle \checkmark$		1

(continued...)

(Question 5 continued)

Question			Answers	Notes	Total
5.	b	i	line through event E parallel to $ct'$ axis meeting $x'$ axis and labelled P ✓		1
5.	b	ii	point on $x'$ axis about $\frac{2}{3}$ of the way to P labelled Q ✓		1

(continued...)

(Question 5 continued)

Question			Answers	Notes	Total
5.	c	i	ends of rod must be recorded at the same time in frame $S'$ ✓ any vertical line from E crossing $x'$ , no label required ✓ right-hand end of rod intersects at R «whose co-ordinate is less than 1.0 m» ✓		<b>3</b>
5.	c	ii	0.7 m ✓		<b>1</b>

Question			Answers	Notes	Total
6.	a		$pc = \sqrt{E^2 - (mc^2)^2} = \sqrt{1.50^2 - 0.511^2} \llcorner = 1.410 \text{ MeV} \llcorner \checkmark$		1
6.	b	i	first equation is due to momentum conservation $\checkmark$ second equation is due to total energy conservation $\checkmark$		2
6.	b	ii	adding $2p_1 = 3.42 \text{ MeV c}^{-1} \Rightarrow p_1 = 1.71 \text{ MeV c}^{-1} \checkmark$ $p_2 = 0.30 \text{ MeV c}^{-1} \checkmark$		2

Question			Answers	Notes	Total
7.	a	i	the distance from the black hole at which the escape speed is the speed of light $\checkmark$		1
7.	a	ii	$R_s = \llcorner \frac{2GM}{c^2} = \frac{2 \times 6.67 \times 10^{-11} \times 4.0 \times 10^{36}}{9.0 \times 10^{16}} = \llcorner 5.9 \times 10^9 \llcorner \llcorner \text{m} \llcorner \checkmark$		1
7.	b		$2 = \frac{1}{\sqrt{1 - \frac{5.9 \times 10^9}{r}}} \checkmark$ rearranged to give $r$ <b>OR</b> $r = 1.33 \times 5.9 \times 10^9 \llcorner \text{m} \llcorner \checkmark$ $r = 7.9 \times 10^9 \llcorner \text{m} \llcorner \checkmark$		3

Option B — Engineering physics

Question			Answers	Notes	Total
8.	a		taking torques about the pivot $R \times 4.00 = 36.0 \times 2.5 \checkmark$ $R = 22.5 \text{ «N» } \checkmark$		2
8.	b	i	$36.0 \times 2.50 = 30.6 \times \alpha \checkmark$ $\alpha = 2.94 \text{ «rad s}^{-2}\text{» } \checkmark$		2
8.	b	ii	the equation can be applied only when the angular acceleration is constant $\checkmark$ any reasonable argument that explains torque is not constant, giving non constant acceleration $\checkmark$	<i>eg weight is no longer perpendicular to the rod</i>	2
8.	c	i	«from conservation of energy» Change in GPE = Change in rotational KE $\checkmark$ $W \frac{L}{2} = \frac{1}{2} I \omega^2 \checkmark$ $\omega = \sqrt{\frac{36.0 \times 5.00}{30.6}} \checkmark$ $\text{«} \omega = 2.4254 \text{ rad s}^{-1}\text{»}$		3
8.	c	ii	$L = 30.6 \times 2.43 = 74.4 \text{ «Js» } \checkmark$		1

Question			Answers	Notes	Total
9.	a	i	<p><b>ALTERNATIVE 1:</b></p> $P_c = P_B = \frac{P_A V_A}{V_B} \checkmark$ $= \frac{2.8 \times 10^6 \times 1 \times 10^{-4}}{2.8 \times 10^{-4}} \llcorner = 1.00 \times 10^6 \text{ Pa} \llcorner \checkmark$ <p><b>ALTERNATIVE 2</b></p> $2.80 \times 10^6 \times 1.00^{\frac{5}{3}} = P_c \times 1.85^{\frac{5}{3}} \checkmark$ $P_c = 2.80 \times 10^6 \times \frac{1.00^{\frac{3}{5}}}{1.85^{\frac{3}{5}}} \llcorner = 1.00 \times 10^6 \text{ Pa} \llcorner \checkmark$		2
9.	a	ii	<p><b>ALTERNATIVE 1:</b></p> <p>Since <math>T_B = T_A</math> then <math>T_C = \frac{V_C T_B}{V_B} \checkmark</math></p> $= \frac{1.85 \times 385}{2.8} \llcorner = 254.4 \text{ K} \llcorner \checkmark$ <p><b>ALTERNATIVE 2:</b></p> $\frac{2.80 \times 1.00}{385} = \frac{1.00 \times 1.85}{T_c} \llcorner \text{«K»} \llcorner \checkmark$ $T_c = 385 \times \frac{1.00 \times 1.85}{2.80} \llcorner = 254.4 \text{ K} \llcorner \checkmark$		2

(continued...)

(Question 9 continued)

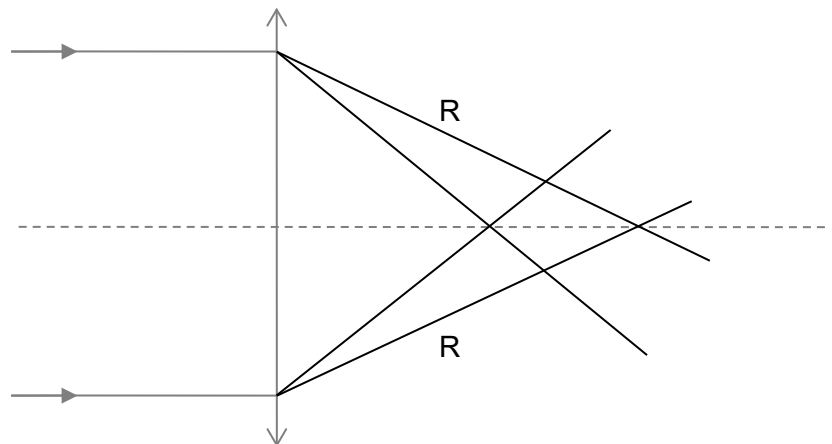
Question			Answers	Notes	Total
9.	b		work done = « $p\Delta V = 1.00 \times 10^6 \times (1.85 \times 10^{-4} - 2.80 \times 10^{-4}) = \text{»} -95 \text{ « J » } \checkmark$ change in internal energy = « $\frac{3}{2}p\Delta V = -\frac{3}{2} \times 95 = \text{»} -142.5 \text{ « J » } \checkmark$ $Q = -95 - 142.5 \checkmark$ « - 238 J »	Allow positive values.	3
9.	c	i	net work is $288 - 238 = 50 \text{ « J » } \checkmark$ efficiency = « $\frac{288 - 238}{288} = \text{»} 0.17 \checkmark$		2
9.	c	ii	along B → C $\checkmark$		1

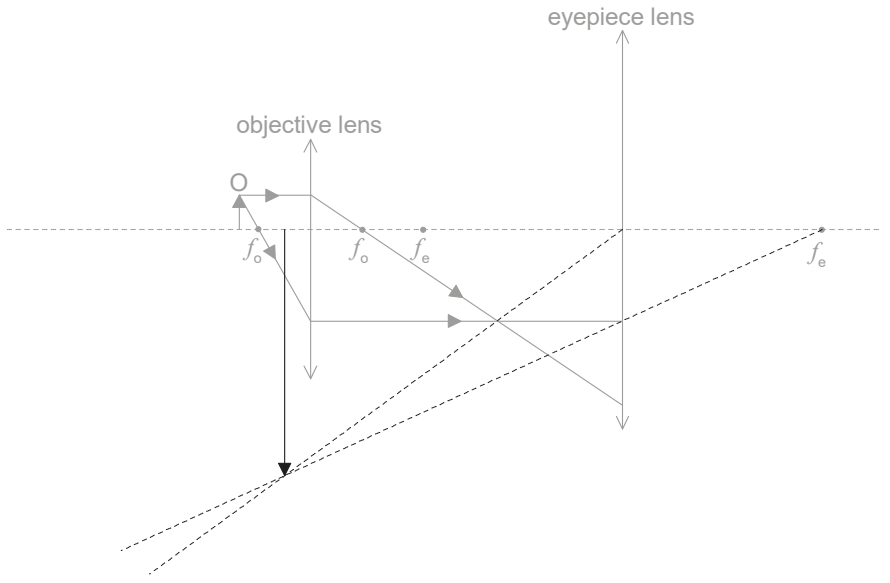
Question			Answers	Notes	Total
10.	a		ice displaces its own weight of water / OWTTE  <b>OR</b>  melted ice volume equals original volume displaced / OWTTE ✓  no change will take place ✓		2
10.	b	i	continuity equation says $v \times A_1 = u \times A_2$ ✓  «and» $A_1 = 4A_2$ ✓  «giving result»		2
10.	b	ii	<i>Bernoulli:</i>  « $\frac{1}{2} \rho v^2 + \rho g H + P_{\text{atm}} = \frac{1}{2} \rho u^2 + 0 + P_{\text{atm}}$ » gives $\frac{1}{2} \times 1000 \times \frac{u^2}{16} + 1000 \times 9.8 \times 5.0 = \frac{1}{2} \times 1000 \times u^2$ ✓  $u = 10.2$ «m s <sup>-1</sup> » ✓	<i>Accept solving directly via conservation of energy.</i>	2



Question		Answers	Notes	Total
11.	a	because the mass and the driver are out of phase «by $\pi$ » ✓ so upwards ✓	<i>Justification needed for MP2</i>	2
11.	b	<p><b>ALTERNATIVE 1:</b></p> $\left\langle Q = 2\pi \frac{A_0^2}{A_0^2 - A_1^2} \right\rangle \Rightarrow \frac{A_1^2}{A_0^2} = 1 - \frac{2\pi}{Q} \quad \checkmark$ $\frac{A_1}{A_0} = \left\langle \sqrt{1 - \frac{2\pi}{22}} \right\rangle \Rightarrow A_1 = 8.5 \text{ « cm » } \quad \checkmark$ <p><b>ALTERNATIVE 2:</b></p> driver amplitude is constant ✓ so mass amplitude is unchanged at 10 cm ✓		2

Option C — Imaging

Question			Answers	Notes	Total
12.	a		each incident ray shown splitting into two ✓ each pair symmetrically intersecting each other on principal axis ✓ for red, intersection further to the right ✓	 <p><i>For MP3, at least one of the rays must be labelled.</i></p>	3
12.	b	i	rays diverge after passing through lens <b>OR</b> the extension of the rays will intersect the principal axis on the side of incident rays/as if they were coming from the focal point/points in the left side/OWTTE ✓		1
12.	b	ii	by placing a diverging lens next to the converging lens <b>OR</b> make an achromatic doublet ✓	Further details are not required.	1

Question		Answers	Notes	Total
13.	a	proper construction lines ✓ image at intersection of proper construction lines ✓	 <p>The diagram illustrates the ray tracing for a telescope. It features two lenses: an objective lens on the left and an eyepiece lens on the right. A horizontal dashed line represents the optical axis. The focal point of the objective lens is labeled <math>f_o</math>, and the focal point of the eyepiece lens is labeled <math>f_e</math>. An object, labeled 'O', is positioned to the left of the objective lens. Three rays are shown: 1) A ray from the top of the object that is parallel to the optical axis, which refracts through the objective lens and passes through its focal point <math>f_o</math>. 2) A ray from the top of the object that passes through the optical center of the objective lens and continues straight through. 3) A ray from the top of the object that passes through the focal point <math>f_o</math> of the objective lens and becomes parallel to the optical axis after refraction. These three rays converge to form a real, inverted intermediate image. This intermediate image is located between the two lenses and is positioned at the focal point <math>f_e</math> of the eyepiece lens. The eyepiece lens then refracts these rays so that they emerge as parallel rays, forming a virtual, upright, and magnified image at infinity. Labels 'objective lens' and 'eyepiece lens' are placed above their respective lenses. The object 'O' is labeled at the top left. Focal points <math>f_o</math> and <math>f_e</math> are marked on the optical axis.</p>	2

(continued...)

(Question 13 continued)

Question			Answers	Notes	Total
13.	b	i	distance of intermediate image from objective is $\frac{1}{v} = \frac{1}{20} - \frac{1}{24} \quad \text{ie: } v = 120 \text{ «mm» } \checkmark$ distance of intermediate image from eyepiece is $\frac{1}{u} = \frac{1}{60} - \left(-\frac{1}{240}\right) \quad \text{ie: } u = 48 \text{ «mm» } \checkmark$ lens separation 168 «mm» $\checkmark$		3
13.	b	ii	<p><b>ALTERNATIVE 1:</b></p> eyepiece: $m = \frac{-v}{u} = \frac{240}{48} = 5$		2
			<p><b>AND</b></p> objective $m = \frac{-v}{u} = \frac{-120}{24} = -5 \checkmark$		
			Total $m = -5 \times 5 = -25 \checkmark$		
			<p><b>ALTERNATIVE 2:</b></p> $m = \left(\frac{240}{60} + 1\right) \times \left(-\frac{120}{24}\right) \checkmark$ $m = -25 \checkmark$		

Question			Answers	Notes	Total
14.	a	i	$\llcorner \sin \theta_c = \frac{n_1}{n_2} \gg n_1 = 1.52 \times \sin 84.0^\circ \checkmark$ $n_1 = 1.51 \checkmark$		2
14.	a	ii	to have a critical angle close to $90^\circ \checkmark$ so only rays parallel to the axis are transmitted $\checkmark$ to reduce waveguide/modal dispersion $\checkmark$	Do not accept "so that most rays are reflected".	1 max
14.	b	i	long path is $\frac{12 \times 10^3}{\sin 84^\circ} \checkmark$ $= 12066 \llcorner \text{m} \gg \checkmark$ $\llcorner \text{so } 66 \text{ m longer} \gg$		2
14.	b	ii	speed of light in core is $\frac{3.0 \times 10^8}{1.52} = 1.97 \times 10^8 \llcorner \text{m s}^{-1} \gg \checkmark$ time delay is $\frac{66}{1.97 \times 10^8} = 3.35 \times 10^{-7} \llcorner \text{s} \gg \checkmark$		2
14.	b	iii	no, period of signal is $1 \times 10^{-8} \llcorner \text{s} \gg$ which is smaller than the time delay/OWTTE $\checkmark$		1

Question		Answers	Notes	Total
15.	a	protons spin direction changes <b>OR</b> proton energy state changes ✓		1
15.	b	Relaxation time «of signal/proton spin» ✓ Location/time delay of the emitted RF signal ✓		2
15.	c	Relaxation time gives information on tissue type/density/health/OWTTE✓  Location information provides 3D image/OWTTE✓		2

Question		Answers	Notes	Total
16.	a	$I_0 e^{-23 \times 0.041}$ ✓ $= 0.39 I_0$ ✓		2
16.	b	$R = \left( \frac{6.3 \times 10^6 - 1.7 \times 10^6}{6.3 \times 10^6 + 1.7 \times 10^6} \right)^2 = 0.33$ ✓ so reflected intensity is $0.33 \times 0.39 I_0 = 0.13 I_0$ ✓		2
16.	c	$0.13 I_0 \times 0.39 = 0.05 I_0$ ✓		1

Option D — Astrophysics

Question			Answers	Notes	Total
17.	a		In cluster, stars are gravitationally bound <b>OR</b> constellation not ✓ In cluster, stars are the same/similar age <b>OR</b> in constellation not ✓ Stars in cluster are close in space/the same distance <b>OR</b> in constellation not ✓ Cluster stars appear closer in night sky than constellation ✓ Clusters originate from same gas cloud <b>OR</b> constellation does not ✓		2 max
17.	b	i	$d = 275$ «pc» ✓		1
17.	b	ii	because of the difficulty of measuring very small angles ✓		1
17.	c		mass of gas cloud > Jeans mass ✓ «magnitude of» gravitational potential energy > $E_k$ of particles ✓ cloud collapses/coalesces «to form a protostar» ✓		2 max

Question			Answers	Notes	Total
18.	a	i	$\lambda = \left\langle \frac{2.9 \times 10^{-3}}{4600} \right\rangle \Rightarrow 630 \text{ nm} \checkmark$		1
18.	a	ii	black body curve shape $\checkmark$ peaked at a value from range 600 to 660 nm $\checkmark$		2
18.	a	iii	$\frac{L}{L_{\odot}} = \left( \frac{0.73 R_{\odot}}{R_{\odot}} \right)^2 \times \left( \frac{4600}{5800} \right)^4 \checkmark$ $L = 0.211 L_{\odot} \checkmark$		2
18.	b		$M = \left\langle 0.21^{\frac{1}{3.5}} M_{\odot} \right\rangle \Rightarrow 0.640 M_{\odot} \checkmark$	Accept reverse argument $0.64^{3.5} = 0.21$	1
18.	c		$\frac{T_E}{T_{\odot}} = \left\langle \frac{\frac{M_E}{L_E}}{\frac{M_{\odot}}{L_{\odot}}} \right\rangle = \frac{0.64}{0.21} \Rightarrow 3.0 \checkmark$ $T \approx 27 \text{ billion years} \checkmark$		2
18.	d		red giant $\checkmark$ planetary nebula $\checkmark$ white dwarf $\checkmark$	do <b>NOT</b> accept supernova, red supergiant, neutron star or black hole as stages	3



Question		Answers	Notes	Total
19.	a	measured redshift «z» of star ✓ use of Doppler formula <b>OR</b> $z \sim v/c$ <b>OR</b> $v = \frac{c\Delta\lambda}{\lambda}$ to find v ✓	OWTTE	2
19.	b	use of gradient or any point on the line to obtain any expression for either $H = \frac{v}{d}$ or $t = \frac{d}{v}$ ✓ correct conversion of <i>d</i> to m and v to m/s ✓  $= 4.6 \times 10^{17}$ «s» ✓		3

Question		Answers	Notes	Total
20.	a	energy filling all space ✓ resulting in a repulsive force/force opposing gravity ✓ accounts for the accelerating universe ✓ makes up about 70% of «the energy» of universe ✓		2 max
20.	b	black hole ✓ brown dwarf ✓ massive compact halo object /MACHO ✓ neutrinos ✓ weakly interacting massive particle /WIMP ✓		2 max

Question		Answers	Notes	Total
21.	a	<p>«wavelength of light/CBR» <math>\lambda \propto R</math> ✓</p> <p>reference to Wien's law showing that <math>\lambda \propto \frac{1}{T}</math> ✓</p> <p>combine to get result ✓</p>	OWTTE	3
21.	b	$\frac{R_{\text{past}}}{R_{\text{now}}} = \frac{3}{300} = 0.01$ ✓		1