



**GCE**

**Mathematics A**

Unit **H240/03**: Pure Mathematics and Mechanics

Advanced GCE

**Mark Scheme for June 2018**

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This mark scheme is published as an aid to teachers and students, to indicate the requirements of the examination. It shows the basis on which marks were awarded by examiners. It does not indicate the details of the discussions which took place at an examiners' meeting before marking commenced.

All examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

Mark schemes should be read in conjunction with the published question papers and the report on the examination.

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## Annotations and abbreviations

<b>Annotation in scoris</b>	<b>Meaning</b>
✓ and ✕	
BOD	Benefit of doubt
FT	Follow through
ISW	Ignore subsequent working
M0, M1	Method mark awarded 0, 1
A0, A1	Accuracy mark awarded 0, 1
B0, B1	Independent mark awarded 0, 1
SC	Special case
^	Omission sign
MR	Misread
Highlighting	
<b>Other abbreviations in mark scheme</b>	<b>Meaning</b>
E1	Mark for explaining a result or establishing a given result
dep*	Mark dependent on a previous mark, indicated by *
cao	Correct answer only
oe	Or equivalent
rot	Rounded or truncated
soi	Seen or implied
www	Without wrong working
AG	Answer given
awrt	Anything which rounds to
BC	By Calculator
DR	This question included the instruction: In this question you must show detailed reasoning.

**Subject-specific Marking Instructions for A Level Mathematics A**

- a Annotations should be used whenever appropriate during your marking. The A, M and B annotations must be used on your standardisation scripts for responses that are not awarded either 0 or full marks. It is vital that you annotate standardisation scripts fully to show how the marks have been awarded. For subsequent marking you must make it clear how you have arrived at the mark you have awarded.
- b An element of professional judgement is required in the marking of any written paper. Remember that the mark scheme is designed to assist in marking incorrect solutions. Correct solutions leading to correct answers are awarded full marks but work must not be judged on the answer alone, and answers that are given in the question, especially, must be validly obtained; key steps in the working must always be looked at and anything unfamiliar must be investigated thoroughly. Correct but unfamiliar or unexpected methods are often signalled by a correct result following an apparently incorrect method. Such work must be carefully assessed. When a candidate adopts a method which does not correspond to the mark scheme, escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner.  
If you are in any doubt whatsoever you should contact your Team Leader.
- c The following types of marks are available.

**M**

A suitable method has been selected and *applied* in a manner which shows that the method is essentially understood. Method marks are not usually lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. In some cases the nature of the errors allowed for the award of an M mark may be specified.

**A**

Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated Method mark is earned (or implied). Therefore M0 A1 cannot ever be awarded.

**B**

Mark for a correct result or statement independent of Method marks.

**E**

Mark for explaining a result or establishing a given result. This usually requires more working or explanation than the establishment of an unknown result.

Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored. Sometimes this is reinforced in the mark scheme by the abbreviation *isw*. However, this would not apply to a case where a candidate passes through the correct answer as part of a wrong argument.

- d When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. (The notation 'dep\*' is used to indicate that a particular mark is dependent on an earlier, asterisked, mark in the scheme.) Of course, in practice it may happen that when a candidate has once gone wrong in a part of a question, the work from there on is worthless so that no more marks can sensibly be given. On the other hand, when two or more steps are successfully run together by the candidate, the earlier marks are implied and full credit must be given.
- e The abbreviation FT implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A and B marks are given for correct work only – differences in notation are of course permitted. A (accuracy) marks are not given for answers obtained from incorrect working. When A or B marks are awarded for work at an intermediate stage of a solution, there may be various alternatives that are equally acceptable. In such cases, what is acceptable will be detailed in the mark scheme. If this is not the case please, escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner. Sometimes the answer to one part of a question is used in a later part of the same question. In this case, A marks will often be 'follow through'. In such cases you must ensure that you refer back to the answer of the previous part question even if this is not shown within the image zone. You may find it easier to mark follow through questions candidate-by-candidate rather than question-by-question.
- f Unless units are specifically requested, there is no penalty for wrong or missing units as long as the answer is numerically correct and expressed either in SI or in the units of the question. (e.g. lengths will be assumed to be in metres unless in a particular question all the lengths are in km, when this would be assumed to be the unspecified unit.) We are usually quite flexible about the accuracy to which the final answer is expressed; over-specification is usually only penalised where the scheme explicitly says so. When a value is given in the paper only accept an answer correct to at least as many significant figures as the given value. This rule should be applied to each case. When a value is not given in the paper accept any answer that agrees with the correct value to 2 s.f. Follow through should be used so that only one mark is lost for each distinct accuracy error, except for errors due to premature approximation which should be penalised only once in the examination. There is no penalty for using a wrong value for *g*. E marks will be lost except when results agree to the accuracy required in the question.
- g Rules for replaced work: if a candidate attempts a question more than once, and indicates which attempt he/she wishes to be marked, then examiners should do as the candidate requests; if there are two or more attempts at a question which have not been crossed out, examiners should mark what appears to be the last (complete) attempt and ignore the others. NB Follow these maths-specific instructions rather than those in the assessor handbook.
- h For a genuine misreading (of numbers or symbols) which is such that the object and the difficulty of the question remain unaltered, mark according to the scheme but following through from the candidate's data. A penalty is then applied; 1 mark is generally appropriate, though this may differ for some units. This is achieved by withholding one A mark in the question. Marks designated as cao may be awarded as long as there are no other errors. E marks are lost unless, by chance, the given results are established by equivalent working. 'Fresh starts' will not affect an earlier decision about a misread. Note that a miscopy of the candidate's own working is not a misread but an accuracy error.

- i If a calculator is used, some answers may be obtained with little or no working visible. Allow full marks for correct answers (provided, of course, that there is nothing in the wording of the question specifying that analytical methods are required). Where an answer is wrong but there is some evidence of method, allow appropriate method marks. Wrong answers with no supporting method score zero. If in doubt, consult your Team Leader.
  
- j If in any case the scheme operates with considerable unfairness consult your Team Leader.

Question		Answer	Marks	AO		Guidance	
1	(i)	$(x+4)^2 - 16 + (y-1)^2 - 1 - 7 = 0$	M1	1.1	E	Correct method to find centre of circle	e.g. $(x \pm 4)^2$ and $(y \pm 1)^2$ seen (or implied)
		$(x+4)^2 + (y-1)^2 = 24$	A1	1.1	E		
		$C(-4,1)$	[2]				
1	(ii)	Radius = $\sqrt{24}$	B1	1.1	E	oe e.g. $2\sqrt{6}$	
			[1]				
2		Attempt process for finding both values	M1	1.1a	E	e.g. squaring both sides to obtain 3 terms on both sides	Or consider two linear equations $(2x-1) = \pm(x+3)$ 1 correct solution for A1 SC one correct solution from one linear equation B1
		$3x^2 - 10x - 8 (= 0)$	A1	1.1	E	$(4x^2 - 4x + 1 = x^2 + 6x + 9)$	
		Obtain 4 and $-\frac{2}{3}$	A1	1.1	E	BC	
			[3]				
3		DR	M1	3.1b	E	Accept any inequality or equals and any letter for the width	M1A1 correct answer with no working SC B1: $x < \sqrt{60}$ B1: $x \geq 29/6$
		$x+3 \geq 14.5$	A1	1.1	E	Correct inequality (seen or implied)	
		$x \geq 11.5$	M1	3.1b	E	Accept any inequality or equals	
		$x(x+3) < 180$	M1	1.1	E	Correct expansion and attempt to solve three term quadratic	
		$x^2 + 3x - 180 (< 0) \Rightarrow (x-12)(x+15) (< 0)$	A1	1.1	C	Correct inequalities (seen or implied)	
		$-15 < x < 12$	B1	1.1	C		
$11.5 \leq x < 12$	[6]						

Question			Answer	Marks	AO		Guidance	
4	(i)	(a)	$fg(x) = f(x^2 + 2) = (x^2 + 2)^3$	<b>B1</b>  [1]	<b>1.1</b>	E		
4	(i)	(b)	$gf(x) = g(x^3) = (x^3)^2 + 2(= x^6 + 2)$	<b>B1</b>  [1]	<b>1.1</b>	E	No simplification required	
4	(ii)		<b>DR</b> $(x^2 + 2)^3 = (x^2)^3 + 3(x^2)^2(2) + 3(x^2)(2)^2 + 2^3$  $fg(x) = x^6 + 6x^4 + 12x^2 + 8$ $fg(x) - gf(x) = 24 \Rightarrow 6x^4 + 12x^2 - 18 = 0$ $x^4 + 2x^2 - 3 = 0 \Rightarrow (x^2 - 1)(x^2 + 3) = 0$  $x^2 + 3 = 0$ has no real solutions $x^2 - 1 = 0 \Rightarrow x = \pm 1$	<b>M1</b>  <b>A1</b> <b>A1</b> <b>M1</b>  <b>A1</b> <b>A1</b>  [6]	<b>1.1</b>  <b>1.1</b> <b>2.1</b> <b>1.1</b>  <b>2.4</b> <b>2.2a</b>	E  C C C  A A	Binomial expansion of their $(x^2 + 2)^3$ - correct powers and coefficients  Correct method for solving their quadratic in $x^2$  $x^2 + 3 \neq 0$ is acceptable for this mark	Allow one slip   If M0 next two marks become B marks
5	(i)		$h = 2$ $\frac{h}{2} \left[ \frac{1}{2} + \frac{1}{4} + 2 \left( \frac{1}{2 + \sqrt{2}} \right) \right]$  $I \approx \frac{3}{4} + \frac{2}{2 + \sqrt{2}}$  $\frac{1}{2 + \sqrt{2}} = \frac{(2 - \sqrt{2})}{(2 + \sqrt{2})(2 - \sqrt{2})} = \frac{2 - \sqrt{2}}{2}$  $I \approx \frac{3}{4} + (2 - \sqrt{2}) = \frac{11}{4} - \sqrt{2}$	<b>B1</b> <b>M1</b>  <b>A1</b>  <b>M1</b>  <b>A1</b> [5]	<b>1.1</b> <b>2.1</b>  <b>1.1</b>  <b>3.1a</b>  <b>2.2a</b>	E E  C  E  A	Use of correct formula with correct (exact) $y$ -values with their $h$   Correct method for rationalising the denominator of their surd together with correct simplification  <b>AG</b> – at least one step of intermediate working (from application of trapezium rule to given result)	Condone one error in values     Must be convincing as AG



Question		Answer	Marks	AO	Guidance		
5	(ii)	$x = u^2 \Rightarrow dx = 2u du$	<b>M1*</b>	<b>3.1a</b>	E	An attempt at integration by sub - allow any genuine attempt (as a minimum must differentiate their sub. and remove all x's)	Limits not required for first four marks
		$\int_0^4 \frac{dx}{2+\sqrt{x}} = \int_0^2 \frac{2u}{2+u} du$	<b>A1</b>	<b>1.1</b>	C	Correct integral in terms of $u$	
		$= 2 \int_0^2 \frac{2+u-2}{2+u} du = 2 \int_0^2 1 - \frac{2}{2+u} du$	<b>Dep*M1</b>	<b>2.1</b>	C	Re-writes integral in the form $\int a + \frac{b}{1+u} du$	Or use $t = 2 + u$ to obtain integral of the form $\int a + \frac{b}{t} dt$
		$= 2[u - 2\ln(2+u)]_0^2$	<b>A1ft</b>	<b>1.1</b>	A	Correctly integrates their $\int a + \frac{b}{1+u} du$	$\int 2 - \frac{4}{t} dt$ $= 2t - 4\ln t$
		$= 2\{(2 - 2\ln(2+2)) - (0 - 2\ln(2+0))\}$ $= 2(2 - 2\ln 2)$	<b>M1</b> <b>A1</b> <b>[6]</b>	<b>1.1</b> <b>2.2a</b>	C A	Uses correct limits correctly (dependent on both previous M marks) oe e.g. $4 - 4 \ln 4 + 4 \ln 2$	
5	(iii)	$\frac{11}{4} - \sqrt{2} \approx 2(2 - 2\ln 2)$	<b>M1</b>	<b>1.1a</b>	C	Setting the given result approx. equal to their (ii)	
		$\ln 2 \approx \frac{5}{16} + \frac{\sqrt{2}}{4}$	<b>A1</b> <b>[2]</b>	<b>2.2a</b>	A	$k = \frac{5}{16}$	

Question		Answer	Marks	AO		Guidance
6	(i)	$\sin\left(2\theta + \frac{\pi}{4}\right) = 3\cos\left(2\theta + \frac{\pi}{4}\right)$ $\sin 2\theta \cos \frac{\pi}{4} + \sin \frac{\pi}{4} \cos 2\theta = 3\cos 2\theta \cos \frac{\pi}{4} - 3\sin 2\theta \sin \frac{\pi}{4}$ $4\sin 2\theta = 2\cos 2\theta$ $2\frac{\sin 2\theta}{\cos 2\theta} = 1 \Rightarrow \tan 2\theta = \frac{1}{2}$	M1 A1 A1 [3]	1.1 1.1 2.2a	E E E	Correct use of compound angle formulae at least once Not from incorrect working AG – at least one step of intermediate working seen
		<b>ALT:</b> $\tan\left(2\theta + \frac{\pi}{4}\right) = 3$ $\frac{\tan 2\theta + 1}{1 - \tan 2\theta} = 3 \Rightarrow \tan 2\theta + 1 = 3(1 - \tan 2\theta)$ $\tan 2\theta = \frac{1}{2}$	B1 M1 A1			Correct use of compound angle formula for tan and removal of fraction
6	(ii)	$\tan 2\theta = \frac{1}{2} \Rightarrow \frac{2\tan\theta}{1 - \tan^2\theta} = \frac{1}{2}$ $\tan^2\theta + 4\tan\theta - 1 = 0$ $\tan\theta = -2 \pm \sqrt{5}$ $-2 + \sqrt{5} > 0 \text{ so } \tan\theta = -2 + \sqrt{5} \text{ gives acute angle}$ $\therefore \tan\theta = -2 - \sqrt{5}$	M1* Dep*M1 A1 A1 A1 [5]	3.1a 1.1 1.1 2.3 2.2a	E E C A A	Double angle formula for $\tan 2\theta$ Rearranges correctly to form 3-term quadratic in tan BC - One correct exact value Explicit rejection and reason for rejection This value only

Question	Answer	Marks	AO	Guidance	
7	$(2x-1)^3 \frac{dy}{dx} + 4y^2 = 0$ $-\frac{1}{4} \int \frac{dy}{y^2} = \int \frac{dx}{(2x-1)^3}$ $\int \frac{dy}{y^2} = -\frac{1}{y}$ $\int \frac{dx}{(2x-1)^3} = \frac{(2x-1)^{-2}}{(2)(-2)}$ $\frac{1}{4y} = -\frac{1}{4(2x-1)^2} + c, (1,1) \Rightarrow c = \dots$ $\frac{1}{y} = -\frac{1}{(2x-1)^2} + 2$ $\frac{1}{y} = \frac{2(2x-1)^2 - 1}{(2x-1)^2}$ $y = \frac{(2x-1)^2}{2(2x-1)^2 - 1}$ $y = \frac{4x^2 - 4x + 1}{8x^2 - 8x + 1}$	<p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>[9]</p>	<p>2.5</p> <p>1.1</p> <p>1.1</p> <p>1.1</p> <p>2.1</p> <p>2.2a</p> <p>3.1a</p> <p>1.1</p> <p>2.2a</p>	<p>E</p> <p>E</p> <p>E</p> <p>C</p> <p>C</p> <p>A</p> <p>A</p> <p>A</p>	<p>Attempt to separate variables</p> <p>M1 for <math>k(2x-1)^{-2}</math></p> <p>Use of (1, 1) to find <math>c</math> – dependent on the previous two M marks and substituted into correct form</p> <p>Oe</p> <p>Correct method for combining both terms on rhs (dependent on previous M mark) before taking the reciprocal</p> <p>Taking the reciprocal (dependent on previous M marks) and making <math>y</math> the subject</p> <p><math>a = 4, b = 8</math></p> <p>Or re-write in terms of <math>y</math></p> <p>Remove triple-decker fractions</p>

Question		Answer	Marks	AO		Guidance	
8	(i)	$\mathbf{g} = \begin{pmatrix} 0 \\ -9.8 \end{pmatrix}$	<b>B1</b>	<b>1.2</b>	E		
		$\begin{pmatrix} 15 \\ -8 \end{pmatrix} + \begin{pmatrix} -7 \\ -2 \end{pmatrix} + 5 \begin{pmatrix} 0 \\ -9.8 \end{pmatrix} = 5\mathbf{a}$	<b>M1</b>	<b>3.3</b>	E	Use of $\mathbf{F} = m\mathbf{a}$ with correct $m$ and two terms of $\mathbf{F}$ correct	
		$\mathbf{a} = \begin{pmatrix} 1.6 \\ -11.8 \end{pmatrix}$ or $\begin{pmatrix} 1.6 \\ -g-2 \end{pmatrix}$	<b>A1</b> <b>[3]</b>	<b>3.4</b>	C		
8	(ii)	$\mathbf{s} = \frac{1}{2} \begin{pmatrix} 1.6 \\ -11.8 \end{pmatrix} (10)^2$	<b>M1</b>	<b>3.4</b>	E	Use of $\mathbf{s} = \mathbf{u}t + \frac{1}{2}\mathbf{a}t^2$ with $t = 10$	
		$\mathbf{s} = \begin{pmatrix} 80 \\ -590 \end{pmatrix}$	<b>A1ft</b>	<b>1.1</b>	E	50a	
		Position vector is $\begin{pmatrix} 82 \\ -545 \end{pmatrix}$	<b>A1</b>	<b>1.1</b>	C		
		<b>[3]</b>					
9	(i)	25N	<b>B1</b> <b>[1]</b>	<b>3.4</b>	E		
9	(ii)	$2(100) = 75x + (x + 0.5)(25)$	<b>M1</b>	<b>3.3</b>	E	eg moments about A – correct number of terms	
		$x = 1.875$	<b>A1ft</b>	<b>1.1</b>	C	Follow through their 25 only	
			<b>A1</b> <b>[3]</b>	<b>1.1</b>	C		
9	(iii)	$(x + 0.5 - 2)(100) = W(4 - 0.5 - x)$	<b>M1</b>	<b>3.3</b>	E	moments about D – correct number of terms – oe (leading to an equation in W)	
		$W = 23.1\text{N}$	<b>A1ft</b>	<b>1.1</b>	C	Follow through their $x$ only	
			<b>A1</b> <b>[3]</b>	<b>1.1</b>	A	Accept 23 or better	23.076923...

Question			Answer	Marks	AO		Guidance	
9	(iv)	(a)	Modelling the stone as a particle assumes that the weight of the stone block acts exactly at <i>B</i> therefore the block's dimensions (or the distribution of the mass of the block) have not been taken into consideration	<b>B1</b> [1]	<b>3.5b</b>	A	Accept 'uniform'	
9	(iv)	(b)	Modelling the plank as a rigid rod assumes that the plank remains in a straight line and does not bend	<b>B1</b> [1]	<b>3.5b</b>	A		
10	(i)		$4\sin 2\theta = 6\sin \theta$ $8\sin \theta \cos \theta = 6\sin \theta$ $\cos \theta = \frac{3}{4} \Rightarrow \theta = 41.4^\circ$	<b>B1</b> <b>M1</b> <b>A1</b> <b>A1</b> [4]	<b>3.3</b> <b>3.1a</b> <b>1.1</b> <b>2.2a</b>	E E E C	Resolving horizontally Use of double angle formulae <b>AG</b>	41.409622...
10	(ii)		$P = 4\cos 2\theta + 6\cos \theta$ $P = 5$	<b>M1</b> <b>A1</b> [2]	<b>3.3</b> <b>1.1</b>	E E	Resolving vertically – allow sin/cos errors Accept 5.002 or better	
10	(iii)	(a)	$3\sin \theta$ and $P - 3\cos \theta$  $\sqrt{(3\sin \theta)^2 + (P - 3\cos \theta)^2}$ Magnitude is 3.39 N	<b>B1</b>  <b>M1</b> <b>A1</b> [3]	<b>1.1</b>  <b>1.1</b> <b>2.2a</b>	E  E C	Resolving horizontally and vertically  Pythagoras on two forces – both must include 41.4 3.4 or better	<b>Alt</b> – M1 for cosine rule with their <i>P</i> , 3 and 41.4, A1 for 11.4966... or 11.5  3.3911649...

Question			Answer	Marks	AO	Guidance		
10	(iii)	(b)	$\tan \alpha = \frac{P - 3 \cos \theta}{3 \sin \theta}$ <p>54.2° below the horizontal</p>	<p><b>M1</b></p> <p><b>A1</b></p> <p>[2]</p>	<p><b>3.1a</b></p> <p><b>3.2a</b></p>	<p>E</p> <p>A</p>	<p>Where <math>\alpha</math> is the angle below the horizontal</p> <p>54.2 or better – must indicate ‘below horizontal’ or equivalent to the ‘downward vertical’ (35.8) – direction may be shown on diagram with minimum of arrow on resultant or arrows on both components</p>	<p><b>Alt</b> – M1 for <math>\frac{\sin \alpha}{3} = \frac{\sin 41.4}{'3.39'}</math> 54.18696...</p>
11	(i)		$a = k + 0.06t$ $k + 0.06(20) = 1.3$ $k = 1.3 - 1.2 = 0.1$	<p><b>B1</b></p> <p><b>M1</b></p> <p><b>A1</b></p> <p>[3]</p>	<p><b>1.1</b></p> <p><b>1.1</b></p> <p><b>1.1</b></p>	<p>E</p> <p>E</p> <p>E</p>	<p>Use of <math>t = 20</math> and <math>a = 1.3</math> in their <math>a</math></p>	
11	(ii)		$s = 0.05t^2 + 0.01t^3 (+c)$ $t = 0, s = 0 \Rightarrow c = 0$ $t = 20, v = 14$ $s_1 = 0.05(20)^2 + 0.01(20)^3$ $25^2 = 14^2 + 2(1.3)s_2$ <p>Total distance = <math>s_1 + s_2 = 265</math> m</p>	<p><b>M1*</b></p> <p><b>A1ft</b></p> <p><b>B1</b></p> <p><b>B1ft</b></p> <p><b>dep*M1</b></p> <p><b>M1</b></p> <p><b>A1</b></p> <p>[7]</p>	<p><b>3.1a</b></p> <p><b>1.1</b></p> <p><b>2.1</b></p> <p><b>1.1</b></p> <p><b>3.4</b></p> <p><b>3.3</b></p> <p><b>2.2a</b></p>	<p>E</p> <p>E</p> <p>A</p> <p>E</p> <p>C</p> <p>A</p> <p>A</p>	<p>Attempt to integrate – all powers increased by 1 (but not just multiplying by <math>t</math>)</p> $s = \frac{1}{2}kt^2 + 0.01t^3$ <p>From a correct expression for <math>s</math></p> <p>12 + 20k</p> <p>Finding distance travelled after 20 s (for reference <math>s_1 = 100</math>)</p> <p>Use of <math>v^2 = u^2 + 2as</math> with <math>v = 25</math> and <math>a = 1.3</math> and their <math>u</math></p> <p>All previous marks must have been awarded</p>	<p>If <math>c = 0</math> stated then must give a reason</p>

Question			Answer	Marks	AO	Guidance		
12	(i)	(a)	$R = mg \cos 30$ $T = \frac{1}{4}mg$  $T + F - mg \sin 30 = 0$ $F = \mu(mg \cos 30)$ $\frac{1}{4}mg + \mu\left(\frac{mg\sqrt{3}}{2}\right) - \frac{1}{2}mg = 0 \Rightarrow \mu = \dots$  $\mu = \frac{\sqrt{3}}{6}$	<b>B1</b> <b>B1</b> <b>M1</b>  <b>A1</b> <b>M1</b> <b>M1</b>  <b>A1</b>  <b>[7]</b>	<b>3.3</b> <b>1.1</b> <b>3.3</b>  <b>1.1</b> <b>3.3</b> <b>2.1</b>  <b>2.2a</b>	E E E  C E A  A	Resolving perpendicular to the plane Resolving vertically for $B$ Resolving parallel to the plane – three terms – allow signs and sin/cos confusion  Use of $F = \mu R$ Deriving equation in $\mu$ (and $m$ and $g$ ) and attempt to solve for $\mu$ – dependent on previous M marks and second B mark	
12	(i)	(b)	$F = mg \sin 30 - \lambda mg (> 0)$  $F > 0 \Rightarrow \lambda < \frac{1}{2}$	<b>M1</b>  <b>A1</b> <b>[2]</b>	<b>3.1a</b>  <b>2.2a</b>	A  A	Resolving parallel to the plane with $\lambda mg$	
12	(ii)		$T - F - mg \sin 30 = m\left(\frac{1}{4}g\right)$ $2mg - T = 2m\left(\frac{1}{4}g\right)$ $2mg - F - mg \sin 30 = \frac{3}{4}mg$ $2mg - \mu(mg \cos 30) - mg \sin 30 = \frac{3}{4}mg$  $\mu = \frac{\sqrt{3}}{2}$	<b>M1</b>  <b>B1</b> <b>A1</b> <b>A1</b>  <b>A1</b> <b>[5]</b>	<b>3.3</b> <b>3.3</b> <b>1.1</b> <b>2.1</b>  <b>2.2a</b>	C C C A  A	N, II parallel to the plane – four terms N, II for $B$ Correct method for eliminating $T$ Correct use of $F = \mu R$ and $R = mg \cos 30$	Allow $a$  Allow $a$

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