# 

## GCSE MATHEMATICS 8300/1H

Higher Tier Paper 1 Non-Calculator

#### Mark scheme

June 2019

Version: 1.0 Final

\*196g83001H/MS\*

Mark schemes are prepared by the Lead Assessment Writer and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation events which all associates participate in and is the scheme which was used by them in this examination. The standardisation process ensures that the mark scheme covers the students' responses to questions and that every associate understands and applies it in the same correct way. As preparation for standardisation each associate analyses a number of students' scripts. Alternative answers not already covered by the mark scheme are discussed and legislated for. If, after the standardisation process, associates encounter unusual answers which have not been raised they are required to refer these to the Lead Assessment Writer.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of students' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

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#### **Glossary for Mark Schemes**

GCSE examinations are marked in such a way as to award positive achievement wherever possible. Thus, for GCSE Mathematics papers, marks are awarded under various categories.

If a student uses a method which is not explicitly covered by the mark scheme the same principles of marking should be applied. Credit should be given to any valid methods. Examiners should seek advice from their senior examiner if in any doubt.

| Μ               | Method marks are awarded for a correct method which could lead to a correct answer.  |
|-----------------|--|
| Α               | Accuracy marks are awarded when following on from a correct method. It is not necessary to always see the method. This can be implied. |
| В               | Marks awarded independent of method.   |
| ft              | Follow through marks. Marks awarded for correct working following a mistake in an earlier step.  |
| SC              | Special case. Marks awarded for a common misinterpretation which has some mathematical worth.  |
| М dep           | A method mark dependent on a previous method mark being awarded.   |
| B dep           | A mark that can only be awarded if a previous independent mark has been awarded.   |
| oe              | Or equivalent. Accept answers that are equivalent.   |
|                 | eg accept 0.5 as well as $\frac{1}{2}$   |
| [a, b]          | Accept values between a and b inclusive.   |
| [a, b)          | Accept values a ≤ value < b  |
| 3.14            | Accept answers which begin 3.14 eg 3.14, 3.142, 3.1416   |
| Use of brackets | It is not necessary to see the bracketed work to award the marks.  |

Examiners should consistently apply the following principles

#### Diagrams

Diagrams that have working on them should be treated like normal responses. If a diagram has been written on but the correct response is within the answer space, the work within the answer space should be marked. Working on diagrams that contradicts work within the answer space is not to be considered as choice but as working, and is not, therefore, penalised.

#### Responses which appear to come from incorrect methods

Whenever there is doubt as to whether a student has used an incorrect method to obtain an answer, as a general principle, the benefit of doubt must be given to the student. In cases where there is no doubt that the answer has come from incorrect working then the student should be penalised.

#### Questions which ask students to show working

Instructions on marking will be given but usually marks are not awarded to students who show no working.

#### Questions which do not ask students to show working

As a general principle, a correct response is awarded full marks.

#### Misread or miscopy

Students often copy values from a question incorrectly. If the examiner thinks that the student has made a genuine misread, then only the accuracy marks (A or B marks), up to a maximum of 2 marks are penalised. The method marks can still be awarded.

#### **Further work**

Once the correct answer has been seen, further working may be ignored unless it goes on to contradict the correct answer.

#### Choice

When a choice of answers and/or methods is given, mark each attempt. If both methods are valid then M marks can be awarded but any incorrect answer or method would result in marks being lost.

#### Work not replaced

Erased or crossed out work that is still legible should be marked.

#### Work replaced

Erased or crossed out work that has been replaced is not awarded marks.

#### Premature approximation

Rounding off too early can lead to inaccuracy in the final answer. This should be penalised by 1 mark unless instructed otherwise.

#### **Continental notation**

Accept a comma used instead of a decimal point (for example, in measurements or currency), provided that it is clear to the examiner that the student intended it to be a decimal point.

| Question | Answer   | Mark       | Commer   | nts |
|----------|--|------------|----------|-----|
| 1        | 9  | B1         |          |     |
| 2        | 2 <mark>7</mark> 9   | B1         |          |     |
| 3        | 6π   | B1         |          |     |
| 4        | <u>37</u><br>8   | B1         |          |     |
|          | 9.7 × 10 <sup>-4</sup>                                     | B1         |          |     |
|          | Ade  | ditional G | Buidance |     |
| 5(a)     | Condone 9.7 . $10^{-4}$ or $9.7 \cdot 10^{-4}$             |            |          | B1  |
|          | Ignore zeroes before the '9' eg $\ 00009.7 \times 10^{-4}$ |            |          | B1  |
|          | 9.7 × 10 <sup>4-</sup>                                     |            |          | B0  |

| Question  | Answer  | Mark | Commer | nts          |  |
|---|---|------|--------|--------------|--|
|   | 300 000 and 4000<br>or<br>$(10^5 \div 10^3 =) 10^2$<br>or $(10^5 \div 10^3 =) 100$<br>or $7.5 \times 10^{(1)}$ or $75 \times 10^0$<br>or<br>$\frac{3 \times 10^2}{4}$ or $\frac{300}{4}$  | M1   |        |              |  |
|   | 75  | A1   |        |              |  |
|   | Additional Guidance   |      |        |              |  |
| 5(b)  | If the answer is given in standard form and as 75 the student must<br>indicate that 75 is their chosen answer or it must be the final answer<br>given<br>eg1 $7.5 \times 10^{(1)} = 75$ on the answer line<br>eg2 $75 = 7.5 \times 10^{(1)}$ on the answer line |      |        | M1A1<br>M1A0 |  |
| $\frac{300}{4} \text{ or } 75 \text{ from incorrect working scores ze}$ $eg1 \ 3 \times 10^5 = 30000 \text{ and } 4 \times 10^3 = 400 \text{ and}$ $eg2 \ \frac{30000}{400} = 75$ |   |      |        | M0A0<br>M0A0 |  |
|   | For the method mark, ignore incorrect work from a correct expression eg $0.75 \times 10^2 = 7.5 \times 10^3$  |      |        | M1A0         |  |
|   | If the student attempts two methods (<br>attempting to convert to ordinary num<br>award the higher mark   |      |        |              |  |

| Question | Answer  | Mark        | Comments  |  |  |
|----------|---|-------------|---|--|--|
| 6(a)     | $\frac{1}{6} \text{ on '1' and } \frac{1}{3} \text{ or } \frac{2}{6} \text{ on '2 or 3'}$<br>and<br>$\frac{1}{2} \text{ on each of 'Odd' and 'Even'}$ | B2          | oe fraction, decimal or percentage<br>B1<br>$\frac{1}{6}$ on '1' and $\frac{1}{3}$ or $\frac{2}{6}$ on '2 or 3'<br>or<br>$\frac{1}{2}$ on each of 'Odd' and 'Even'<br>or<br>all correct unsimplified probabilities with<br>one or more simplification errors<br>eg $\frac{3}{6}$ on 'Odd' simplified to $\frac{1}{3}$ |  |  |
|          | Additional Guidance   |             |   |  |  |
|          | Accept decimals or percentages roun least 2 significant figures   | ded or tru  | incated correctly to at   |  |  |
|          | Only withhold a mark for simplification awarded   | n errors if | B2 would otherwise be   |  |  |
|          | Ignore extra branches added   |             |   |  |  |
|          | Ignore attempts to work out combined probabilities to the right of the tree diagram   |             |   |  |  |
|          | If an answer line is blank, the student elsewhere on the branch   | may have    | e written their answer  |  |  |

| Question | Answer   | Mark      | Comments  |
|----------|--|-----------|---|
|          | Alternative method 1: P(1) + P(4, 5                                      | or 6) × P | (Odd)   |
|          | $\frac{1}{2}$ × their $\frac{1}{2}$ or $\frac{1}{4}$                     | M1        | oe  |
|          | their $\frac{1}{4}$ + their $\frac{1}{6}$                                | M1dep     | oe  |
|          | $(P(win) =) \frac{10}{24} \text{ or } \frac{5}{12}$                      | A1ft      | oe ft their tree diagram  |
|          | Lose (and P(Lose) = $\frac{14}{24}$ or $\frac{7}{12}$ oe)                | A1ft      | ft correct decision for their $\frac{5}{12}$ (and their $\frac{7}{12}$ ) with M2 scored |
| 6(b)     | Alternative method 2: 1 – P(2 or 3)                                      | – P(4, 5  | or 6) × P(Even)   |
|          | $\frac{1}{2}$ × their $\frac{1}{2}$ or $\frac{1}{4}$                     | M1        | oe  |
|          | their $\frac{1}{4}$ + their $\frac{1}{3}$<br>or P(lose) = $\frac{7}{12}$ | M1dep     | oe<br>ft their tree diagram   |
|          | (P(win) =) $\frac{10}{24}$ or $\frac{5}{12}$                             | A1ft      | oe ft their tree diagram  |
|          | Lose (and P(Lose) = $\frac{14}{24}$ or $\frac{7}{12}$ oe)                | A1ft      | ft correct decision for their $\frac{5}{12}$ (and their $\frac{7}{12}$ ) with M2 scored |
|          | Additional Guidance is on the follo                                      | wing pag  | le  |

| Question | Answer  | Mark                           | Comme                  | nts      |
|----------|---|--------------------------------|------------------------|----------|
|          | Add   | itional G                      | uidance                |          |
| -        | Check the tree diagram for working  |                                |                        |          |
|          | Any 'their' or ft probability must be > 0   | and < 1 f                      | or marks to be awarded |          |
| -        | For the second A1ft, the ft can be from<br>score 4 marks) or an arithmetic error (<br>M1M1A0A1ft) |                                |                        |          |
| -        | Accept equivalent fractions or decimal equivalent fractions, decimals or perce                    |                                |                        |          |
|          | Accept decimals or percentages round least 2 significant figures                                  |                                |                        |          |
| 6(b)     | Condone $\frac{1}{2} \times$ their $\frac{1}{2}$ as part of a lor                                 |                                |                        |          |
| cont     | eg $\frac{1}{2} \times \frac{1}{2} \times \frac{1}{6}$  |                                |                        | M1M0A0A0 |
|          | Condone decimals used within fraction   | าร                             |                        |          |
|          | eg P(Win) = $\frac{2.5}{6}$   | at least<br>M1M1A1             |                        |          |
| -        | For the method marks, condone incorr  | at least M1M1<br>(may go on to |                        |          |
|          | eg $\frac{1}{2} \times \frac{1}{2} = \frac{1}{4} + \frac{1}{6} = \dots$                           | score 3 or 4<br>marks)         |                        |          |
|          | For the second A1ft, if the student give P(Win) + their P(Lose) must equal 1                      | for P(Lose), their             |                        |          |
|          | However, allow a comparison to $\frac{1}{2}$ un   |                                |                        |          |
|          | for P(Lose)   |                                |                        |          |

| Question | Answer   | Mark      | Comments              |  |  |
|----------|--|-----------|-----------------------|--|--|
|          | Alternative method 1   |           |                       |  |  |
|          | $3 \div \frac{20}{100}$ or $3 \times 5$ or $15$<br>or $3 \times 6$ | M1        | oe                    |  |  |
|          | 18   | A1        |                       |  |  |
| 7        | Alternative method 2   |           |                       |  |  |
|          | 1.2x = x + 3   | M1        | oe equation           |  |  |
|          | 18   | A1        |                       |  |  |
| -        | Additional Guidance  |           |                       |  |  |
|          | Trial and improvement scores 0 or 2                                | unless M1 | can be awarded for 15 |  |  |
|          | 15 seen scores M1  |           |                       |  |  |

| Question | Answer  | Mark       | Commen                              | ts     |
|----------|---|------------|-------------------------------------|--------|
| Question | $(3^{12} =) 531441$<br>or<br>$(3^{5} =) 243$<br>or<br>$(3^{12} \div 3^{5} =) 3^{7} \text{ or } (3^{12} \div 3^{5} =) 2187$<br>or<br>$(3^{2} \times 3 =) 3^{3} \text{ or } (3^{2} \times 3 =) 27$<br>or<br>$3^{12} \div 3^{5} \div 3^{2} \div 3$<br>or<br>$\frac{3^{12}}{3^{5}} \times \frac{1}{3^{2} \times 3}$ | M1         |                                     |        |
|          | $3^{7} \div 3^{3}$ or $3^{7} \div 27$<br>or<br>$3^{(12-5-2-1)}$<br>or<br>$\frac{3^{12}}{3^{8}}$<br>or<br>$3^{4}$<br>or<br>$2187 \div 27$  | M1dep      | oe in the form $3^n \div 3^{(n-4)}$ | )      |
|          | 81  | A1         |                                     |        |
|          | Ado   | ditional G | uidance                             |        |
|          | 3 <sup>4</sup> and 81 on the answer line in either  | order      |                                     | M1M1A1 |
|          | 81 in working and 3 <sup>4</sup> on the answer li   | ne         |                                     | M1M1A0 |

| Question | Answer   | Mark      | Comments  |  |  |
|----------|--|-----------|---|--|--|
|          | Alternative method 1: areas  |           |   |  |  |
|          | $\pi \times 10^2$ or $100\pi$  | M1        | implied by [314, 314.2]   |  |  |
|          | $\pi \times (8 \div 2)^2$ or $\pi \times 4^2$ or $16\pi$<br>or $\pi \times (8 \div 2)^2 \div 2$ or $\pi \times 4^2 \div 2$<br>or $16\pi \div 2$ or $8\pi$                            | M1        | implied by [50.2, 50.3] or [25.12, 25.14]<br>92 $\pi$ or 84 $\pi$ or 92 : 8 or 8 : 92<br>or 84 : 16 or 16 : 84 implies M1M1   |  |  |
|          | (their $100(\pi)$ – their $8(\pi)$ ) ÷ their<br>$8(\pi)$<br>or $92(\pi) \div 8(\pi)$<br>or<br>their $100(\pi) \div$ their $8(\pi)$ (– 1)<br>or $12\frac{1}{2}$ (– 1) or $12.5$ (– 1) | M1dep     | dep on M2<br>absence of $\pi$ must be consistent<br>condone 16( $\pi$ ) as their 8( $\pi$ ) in first<br>calculation only, ie condone<br>(their 100( $\pi$ ) – their 16( $\pi$ )) ÷ their 16( $\pi$ )<br>or 84( $\pi$ ) ÷ 16( $\pi$ ),<br>but not their 100( $\pi$ ) ÷ their 16( $\pi$ ) (– 1) |  |  |
|          | $11\frac{1}{2}$ or 11.5  | A1        | condone $\frac{23}{2}$  |  |  |
| 9        | Alternative method 2: scale factor   |           |   |  |  |
|          | $\frac{10}{8 \div 2} \text{ or } \frac{10}{4} \text{ or } \frac{5}{2}$<br>or $\frac{10 \times 2}{8} \text{ or } \frac{20}{8} \text{ or } 2.5$  | M1        | oe scale factor of lengths eg $\frac{2}{5}$ or 0.4<br>accept 2 : 5 or 5 : 2 oe ratio<br>$\pi$ may be present, but must be consistent<br>in numerator and denominator  |  |  |
|          | (their $\frac{5}{2}$ ) <sup>2</sup> or $\frac{25}{4}$  | M1dep     | oe scale factor of areas eg $\frac{4}{25}$ accept 4 : 25 or 25 : 4 oe ratio   |  |  |
|          | 2 × their $\frac{25}{4}$ (-1) or $\frac{25}{2}$ (-1)<br>or $12\frac{1}{2}$ (-1) or 12.5 (-1)   | M1dep     | oe eg $2 \div$ their $\frac{4}{25}$ (- 1)   |  |  |
|          | $11\frac{1}{2}$ or 11.5  | A1        | condone $\frac{23}{2}$  |  |  |
|          | Additional Guidance is on the follo  | owing pag | Je  |  |  |

| Question | Answer  | Mark            | Comme                 | nts      |
|----------|---|-----------------|-----------------------|----------|
|          | Ade   | uidance         |                       |          |
|          | Accept, for example, $\pi 8$ or $\pi \times 8$ or   | $8	imes\pi$ for | 8π                    |          |
|          | An answer of $11.5\pi$ with no incorrect  | working         |                       | M1M1M1A0 |
|          | Consistent use of $\pi d^2$ for the area of a as $400\pi$ , the area of the semicircle as part as $368\pi$ . This also gives the answer         | $32\pi$ and     | he area of the shaded | MOMOMOAO |
|          | Irrespective of where their answer co<br>other measures such as circumference<br>marks of alternative method 1 if it is c<br>given are for area |                 |                       |          |
| 9        | eg 1  |                 |                       |          |
| (cont)   | Big area = $100\pi$ , little area = $8\pi$ , big circumference = $20\pi$ , little circumference = $4\pi$ , $20 \div 4 = 5$                      |                 |                       | M1M1M0A0 |
|          | eg 2  |                 |                       |          |
|          | 100π, 8π, 20π, 4π   |                 |                       | MOMO     |
| -        | Do not award the second mark if the value of $8\pi$ comes from $\pi d$  |                 |                       | M?M0     |
|          | This is implied by, eg, 'Area of circle = $20\pi$ , area of semi-circle = $8\pi$ '  |                 |                       | MOMO     |
|          | $\frac{100(\pi) - 16(\pi)}{16(\pi)}$ (which may give an answer of 5.25)   |                 |                       | M1M1M1A0 |
|          | $\frac{100(\pi)}{16(\pi)}$ (which may give an answer  | M1M1M0A0        |                       |          |

| Question | Answer   | Mark       | Comments                       |  |  |
|----------|--|------------|--------------------------------|--|--|
|          | Plots the points (1, 60), (2, 30),<br>(3, 20) and (4, 15)  | M1         | $\pm \frac{1}{2}$ small square |  |  |
|          | Correct smooth curve through correct four points   | A1         | $\pm \frac{1}{2}$ small square |  |  |
|          | Ade  | ditional G | uidance                        |  |  |
|          | Ignore any calculations and mark the   | graph on   | у                              |  |  |
| 10(a)    | Points cannot be implied by a bar chart or vertical line graph, but condone crosses at the top of a vertical line graph for M1 and the correct curve superimposed for M1A1 |            |                                |  |  |
|          | For M1, ignore the curve outside the domain $1 \le t \le 4$<br>For A1, whether or not the curve extends outside the domain $1 \le t \le 4$                                 |            |                                |  |  |
|          | it must not have a positive gradient at any pointIf there is no curve, for M1 there must be no other points with<br>x-coordinate 1, 2, 3 or 4                              |            |                                |  |  |
|          | The curve should be a single line with no feathering   |            |                                |  |  |
|          | Unless it affects the shape of the curve (in which case A1 cannot be awarded), ignore incorrect evaluations of 60 ÷ a non-integer value                                    |            |                                |  |  |
|          | eg 60 ÷ 1.5 =  |            |                                |  |  |

| Question | Answer  | Mark  | Commen  | ts              |
|----------|---|---|---|-----------------|
|          | Vertical line from $3\frac{1}{2}$ minutes to their graph  | M1  | $\pm \frac{1}{2}$ small square<br>implied by mark at correct<br>graph or on the vertical at<br>the horizontal axis) or by<br>from their graph | xis (but not on |
|          | Correct reading from their graph for $t = 3.5$  | raph for A1ft ft their graph $\pm \frac{1}{2}$ small so |   | square          |
| 10(b)    | Additional Guidance   |   |   |                 |
|          | Correct reading for their graph, with c   | M1A1  |   |                 |
|          | No graph in (a)   |   |   | M0A0            |
|          | To score any marks, their graph must be decreasing in the domain $1 \le t \le 4$ , but may be a straight line or series of connected straight |   | •   |                 |
|          | Answer from 60 ÷ 3.5 with no graph, or which does not match graph   |   |   | M0A0            |
|          | Reading from 3.3  |   |   | M0A0            |

| Question | Answer   | Mark         | Comments |  |  |
|----------|--|--------------|----------|--|--|
|          | Alternative method 1   |              |          |  |  |
|          | 330 ÷ (7 + 4) or 30  | M1           | ое       |  |  |
|          | 7 	imes their 30 or 210<br>and<br>4 	imes their 30 or 120                            | M1dep        | oe       |  |  |
|          | 45   | A1           |          |  |  |
|          | Alternative method 2   | · · · ·      |          |  |  |
|          | 330 ÷ (7 + 4) or 30  | M1           | oe       |  |  |
|          | (7 – 4) × their 30 or 90   | M1dep        | oe       |  |  |
|          | 45   | A1           |          |  |  |
|          | Alternative method 3   |              |          |  |  |
| 11       | 330 ÷ (7 + 4) or 30  | M1           | oe       |  |  |
|          | $7 \times$ their 30 or 210<br>or $4 \times$ their 30 or 120<br>and<br>330 ÷ 2 or 165 | M1dep        | oe       |  |  |
|          | 45   | A1           |          |  |  |
|          | Alternative method 4   |              |          |  |  |
|          | 330 ÷ (7 + 4) or 30  | M1           | ое       |  |  |
|          | their $30 \times 1.5$  | M1dep        | ое       |  |  |
|          | 45   | A1           |          |  |  |
|          |  | Additional G | Buidance |  |  |
|          |  |              |          |  |  |

| Question | Answer   | Mark               | Comments  |
|----------|--|--------------------|---|
| 12       | -9 2 -7 -5 -12   | B1                 |   |
|          | One of<br>$(102 \rightarrow) 100$<br>$(8.14 \rightarrow) 8$  | M1                 |   |
|          | their 100 = $0.5 \times x^2 \times$ their 8<br>or<br>$(x^2 =)$ their 100 $\div$ 8 $\times$ 2<br>or<br>$(x^2 =)$ 100 $\div$ their 8 $\times$ 2            |                    | oe<br>must have used at least one correct 1 sf<br>value |
| 13       | or<br>25<br>or<br>their $8 \times 5 \times 5 \times 0.5 = 100$   | M1dep              |   |
|          | or<br>$8 \times 5 \times 5 \times 0.5 = 100$   |                    |   |
|          | 5 with M2 seen   | A1<br>Additional G | uidance   |
|          | If working is done with approximations and with the given values ignore<br>the working with the given values and mark the working with<br>approximations |                    |   |

| Question | Answer   | Mark        | Comments   |  |  |
|----------|--|-------------|--|--|--|
|          | Alternative method 1: work out the   | value of k  | ooth angles  |  |  |
|          | $(b =) 90 \div 5 \times 3 \text{ or } 54$  | M1          | oe may be on diagram for <i>b</i> or <i>x</i>  |  |  |
|          | $(x =) \frac{360 - 90 - \text{their 54}}{3 + 1} \text{ or } \frac{216}{4}$   | M1dep       | Oe   |  |  |
|          | (b =) 54 and $(x =) 54with M2 awarded$   | A1          |  |  |  |
|          | Alternative method 2: assumes both angles are equal and uses sum of angles in a quadrilateral  |             |  |  |  |
|          | $(b =) 90 \div 5 \times 3 \text{ or } 54$  | M1          | oe may be on diagram for $b$ or $x$  |  |  |
| 14       | 90 + their 54 + their 54 + 3 × their<br>54<br>or<br>360 - 90 - their 54 - their 54<br>and either<br>$3 \times$ their 54<br>or<br>their 162 ÷ 3 or their 162 ÷ 54<br>90 + 54 + 54 + 162 = 360<br>and 54 × 3 = 162<br>or<br>360 - 90 - 54 - 54 = 162<br>and $162 \div 3 = 54$ or $162 \div 54 = 3$ | M1dep<br>A1 | oe<br>addition of the four angles in the<br>quadrilateral or subtraction of 90 and the<br>two equal angles from 360<br>and<br>multiplication to work out the fourth angle<br>or division of the fourth angle by 3 or 54<br>to act as a check<br>Oe |  |  |
|          | Alternative method 3: assumes bo   | th angles   | are equal and uses ratio to check 90°  |  |  |
|          | 5:3:3:9  | M1          |  |  |  |
|          | $\begin{array}{c c} 360 \div (5 + 3 + 3 + 9) \times 5 \\ \text{or} \ 360 \div 20 \times 5 \end{array} \qquad \qquad \text{M1dep} \end{array} \text{oe}$  | oe          |  |  |  |
|          | $360 \div 20 \times 5 = 90$<br>with M2 awarded   | A1          |  |  |  |
|          | Ad   | ditional G  | Buidance   |  |  |
|          | Any correct method to work out 54 so   | cores M1 o  | on alt 1 or alt 2  |  |  |

| Question | Answer   | Mark         | Commer  | its        |
|----------|--|--------------|---|------------|
| 15(a)    | 20 48 88 108 120   | B1           |   |            |
|          | All 5 points plotted using upper class bounds and their cf values                                    | M1           | $\pm \frac{1}{2}$ small square must be increasing |            |
|          | Smooth curve or polygon for their cf values  | A1ft         | $\pm \frac{1}{2}$ small square must be increasing |            |
|          | Ad   |              |   |            |
| 15(b)    | If (a) is correct, points should be at (10, 20), (20, 48), (30, 88), (40, 108) and (50, 120)         |              |   |            |
|          | For A1, the graph should start at (0, 0  | 0) or (1, 0) | or (10, 20)                                       |            |
|          | For A1, the graph should end at $m = 50$ unless it followed by a horizontal line adjoining (50, 120) |              |   |            |
|          | Histogram only   |              |   | M0A0       |
|          | Histogram and graph  |              |   | Mark curve |

|       | Line from 15 marks to their graph   | M1         | $\pm \frac{1}{2}$ small square<br>implied by mark at correct<br>graph or on the vertical a<br>the horizontal axis) or by<br>from their graph | ixis (but not on |
|-------|---|------------|--|------------------|
| 15(c) | Correct reading from their graph for 15 marks   | A1ft       | $\pm \frac{1}{2}$ small square   |                  |
|       | Ad  | ditional   | Guidance   |                  |
|       | Correct reading for their graph, with c   | or without | evidence of using graph  | M1A1             |
|       | No graph in (b)   |            | M0A0   |                  |
|       | For M1 and A1ft the domain of their graph must be at least $10 \le m \le 20$<br>and their graph must be increasing in the domain $10 \le m \le 50$ or from<br>m = 10 if their graph does not extend to $m = 50$ |            |  |                  |

| Question | Answer  | Mark         | Comme   | nts  |
|----------|---|--------------|---|------|
|          | Correct factorisation of numerator<br>$2(2x - 4x^2)$ or $4(x - 2x^2)$<br>or $x(4 - 8x)$ or $2x(2 - 4x)$<br>or $4x(1 - 2x)$<br>or<br>correct factorisation of denominator<br>2(6x - 3) or $3(4x - 2)$ or $6(2x - 1)orcorrect cancelling by 2 throughout\frac{2x - 4x^2}{6x - 3}$ | M1           | oe with negative coeffici   | ents |
| 16       | Correct fraction with numerator<br>4x(1-2x) or $-4x(2x-1)and denominator6(2x-1)$ or $-6(1-2x)or-\frac{4x}{6} or \frac{-4x}{6} or \frac{4x}{-6}or\frac{2x(2-4x)}{-3(2-4x)} or \frac{2x(2-4x)}{3(4x-2)}$  | M1dep        | oe with cancelling of 2 th<br>eg $\frac{2x(1-2x)}{3(2x-1)} \text{ or } \frac{2x(1-2x)}{-3(1-2x)}$ |      |
|          | $-\frac{2x}{3}$ or $-\frac{2}{3}x$  | A1           | allow $\frac{-2x}{3}$ or $\frac{2x}{-3}$  |      |
|          | Ad  | ditional G   | uidance   |      |
|          | Allow multiplication signs up to M1M <sup>2</sup>   | l            |   |      |
|          | Allow $-0.6$ for $-\frac{2}{3}$   |              |   |      |
|          | Do not allow $-0.66$ for $-\frac{2}{3}$   |              |   |      |
|          | For the first M1 only, allow any correct attempts   | ct factorisa | ation seen within multiple  |      |

| Question | Answer  | Mark       | Comme  | nts                   |
|----------|---|------------|--|-----------------------|
|          | $y^2 = \frac{1}{2}y(y+3)$   | B2         | oe equation<br>eg $2y^2 = y^2 + 3y$ or $y^2 =$<br>or $y = 3$ or $y = 0$ or 3<br>B1<br>$\frac{1}{2}y(y + 3)$ oe expression<br>or an otherwise correct of<br>different unknown or con-<br>unknowns | n<br>equation using a |
|          | Additional Guidance   |            |  |                       |
| 17(a)    | Allow multiplication signs<br>eg $y \times y = \frac{y}{2} \times (y + 3)$                        |            |  | B2                    |
|          | $y^2 = \frac{1}{2}y(y + 3)$ followed by incorrect simplification or attempt to solve the equation |            |  | B2                    |
|          | $y^2 = \frac{1}{2}y + y + 3$  |            | B0   |                       |
|          | 3 only or 0 only or 0 and 3 only  |            |  | В0                    |
|          | Do not allow missing or partially missing brackets unless recovered                               |            |  |                       |
|          | eg1 $y^2 = \frac{1}{2}y \times y + 3$ without correct equation seen                               |            |  | B0                    |
|          | eg2 $y^2 = \frac{1}{2}y(y+3)$ without correct e   | quation se | een  | B0                    |

| Question | Answer   | Mark        | Commer  | nts |
|----------|--|-------------|---|-----|
|          | Correct comment<br>or<br>shows correct working   | B1          | eg1 he hasn't square roo<br>eg2 it should be $\sqrt{8} x =$<br>eg3 he should have divid<br>square rooting | 3   |
| -        | Ac   | ditional (  | Guidance  |     |
|          | $\sqrt{8}$ may be given as $2\sqrt{2}$   |             |   |     |
| -        | Comment that he shouldn't have a ne  | egative ar  | iswer   | B0  |
|          | Mathematically incorrect statement   |             |   | B0  |
|          | Correct comment and an incorrect co  | omment      |   | В0  |
|          | Ex   | cample re   | sponses   |     |
|          | He has taken it as $(8x)^2$<br>He has divided $8x^2$ by <i>x</i> (instead of square rooting) and square rooted the 9 |             |   | B1  |
|          |  |             |   | B1  |
| 17(b)    | He $$ first when supposed to divide it by 8  |             |   | B1  |
| -        | He didn't divide 9 by 8 to get $x^2$   |             |   | B1  |
|          | At the start he took the 8 over when you want $\sqrt{\frac{9}{8}}$   |             |   | B1  |
|          | Toby should have got $\pm \sqrt{\frac{9}{8}}$  |             |   | B1  |
| -        | He should have divided by 8  |             |   | B0  |
|          | Toby didn't square root 8x   |             |   | B0  |
|          | He hasn't square rooted the $8x^2$ to leave x on its own   |             | ts own  | B0  |
|          | He hasn't square rooted the other side to just get <i>x</i>  |             |   | B0  |
|          | Didn't divide by 8   |             |   | В0  |
|          | He should have divided by $8x$   |             |   | B0  |
|          | He found the square root of 9 but did  | n't write 🔨 | $\sqrt{8x} = 9$   | B0  |

| Question | Answer   | Mark       | Comme        | nts  |
|----------|--|------------|--------------|------|
|          | (193 + 7)(193 – 7) or (200)(186)<br>or 200 (×) 186               | M1         | either order |      |
| 18(a)    | (200)(186) = 37 200<br>or<br>200 (×) 186 = 37 200                | A1         |              |      |
| 10(4)    | 37200 with correct method not seen                               | Buidance   | M0A0         |      |
|          | 37 200 from 37 249 – 49 only                                     |            |              | M0A0 |
|          | 37 200 from (200)(186) or 200 (×) 186 and 37 249 – 49 also given |            |              | M1A1 |
|          | Do not award M1 for a 'misread' eg (                             | 193 + 2)(1 | 93 – 2)      | M0A0 |

|       | (10a + 9b)(10a - 9b)<br>or<br>(9b + 10a)(10a - 9b) | B1                          | either order                  |    |
|-------|--|-----------------------------|-------------------------------|----|
| 18(b) | Ade  | ditional G                  | Juidance                      |    |
|       | Condone missing final bracket, eg (1               | 0 <i>a</i> + 9 <i>b</i> )(  | 10 <i>a</i> – 9 <i>b</i>      | B1 |
|       | Condone a multiplication sign eg (10               | 0 <i>a</i> + 9 <i>b</i> ) × | a (10 <i>a</i> – 9 <i>b</i> ) | B1 |

| 19 | <u>1</u><br>9 | B1 |  |
|----|---------------|----|--|
|----|---------------|----|--|

| Question | Answer   | Mark       | Comments   |  |  |
|----------|--|------------|--|--|--|
|          | Alternative method 1: shows that BAC = ACD and alternate angles  |            |  |  |  |
|          | ACD = ABC  | M1         | accept both with same letter on diagram  |  |  |
|          | ABC = BAC  | M1         | accept both with same letter on diagram  |  |  |
|          | BAC = ACD<br>and alternate segment (theorem)<br>with M2 awarded  | M1dep      | dep on M2  |  |  |
|          | Other two correct reasons given with M3 awarded  | A1         | eg<br>(base angles of) isosceles triangle<br>and alternate angles                      |  |  |
| 20(a)    | Alternative method 2: shows that <i>ABC</i> + <i>BCD</i> = 180 and co-interior angles                        |            |  |  |  |
| 20(0)    | ACD = ABC  | M1         | accept both with same letter on diagram  |  |  |
|          | ABC = BAC  | M1         | accept both with same letter on diagram  |  |  |
|          | BCD = 180 - (BAC + ABC) + ACD<br>and $ABC + BCD = 180$<br>and alternate segment (theorem)<br>with M2 awarded | M1dep      | oe<br>dep on M2  |  |  |
|          | Other two correct reasons given with M3 awarded  | A1         | eg<br>(base angles of) isosceles triangle<br>and (co-)interior angles or allied angles |  |  |
| -        | The mark scheme for question 20(   | a) continu | ues on the next page   |  |  |

| Question        | Answer  | Mark            | Commei  | nts              |  |
|-----------------|---|-----------------|---|------------------|--|
|                 | Alternative method 3: line from midpoint of <i>AB</i> to <i>C</i> is perpendicular to <i>AB</i> and <i>CD</i>   |                 |   |                  |  |
|                 | Let <i>M</i> be the midpoint of <i>AB</i><br>and<br><i>MC</i> is perpendicular to <i>AB</i>   | M1              | any letter  |                  |  |
| -               | MC is perpendicular to CD   | M1              |   |                  |  |
|                 | AB and CD are both perpendicular to MC with M2 awarded  | M1dep           | oe<br>dep on M2   |                  |  |
| -               | Three correct reasons given with<br>M3 awarded  | A1              | eg<br>(perpendicular bisector of<br>triangle<br>and <i>MC</i> goes through th<br>circle | ne centre of the |  |
| -               | Ad  | cular to radius |   |                  |  |
| 20(a)<br>(cont) | Other correct methods can be found by extending one or more of the lines. For example, by extending <i>BC</i> it is possible to use corresponding angles as a proof instead of alternating angles. This should be reflected in the reasons required for the last mark |                 |   |                  |  |
| -               | In the scheme, <i>ACD</i> (for example) means angle <i>ACD</i> and not triangle <i>ACD</i>  |                 |   |                  |  |
|                 | Accept equality of angles indicated b not by arcs   |                 |   |                  |  |
|                 | Accept (angle) <i>B</i> for angle <i>ABC</i><br>Do not accept (angle) <i>A</i> for angle <i>BAC</i> or (angle) <i>C</i> for angle <i>ACB</i><br>unless intention is clear from annotation of the diagram  |                 |   |                  |  |
| -               | For the third mark in alternative meth for angles if clearly marked on the di   |                 |   |                  |  |
| -               | Do not award marks for an argument<br>angles, but ignore 60° marked on dia  |                 |   |                  |  |
| -               | Ignore an angle marked at ADC   |                 |   |                  |  |
|                 | Ignore incorrect statements that do not affect the proof<br>eg ACD is an isosceles triangle (but not used in proof)   |                 |   |                  |  |

| Question | Answer  | Mark        | Comments |
|----------|---|-------------|----------|
| 20(b)    | AB is parallel to DC     AC bisects angle BCD | B1          |          |
|          | AC bisects angle BAD                          | dditional C | Guidance |

| Question | Answer  | Mark             | Comments  |  |  |
|----------|---|------------------|---|--|--|
|          | Alternative method 1: substitution of $2x + p$ for y  |                  |   |  |  |
|          | 2x + 3(2x + p) = 5p   | M1               | oe equation<br>eg $2x + 6x + 3p = 5p$   |  |  |
|          | 6x + 2x = 5p - 3p or $8x = 2p$  | M1dep            | oe equation with terms collected<br>condone incorrect expansion before<br>rearrangement   |  |  |
| 21       | Correct simplified terms<br>$(x =) \frac{p}{4} \text{ or } \frac{1}{4}p \text{ or } 0.25p$<br>and<br>$(y =) \frac{3p}{2} \text{ or } \frac{3}{2}p \text{ or } 1\frac{1}{2}p \text{ or } 1.5p$<br>Alternative method 2: substitution | A2<br>of y - p f | A1<br>one correct simplified term<br>or<br>otherwise correct terms for both with 'p'<br>omitted<br>eg $x = 0.25$ and $y = 1.5$<br>or<br>correct unsimplified terms for both<br>eg $x = \frac{2p}{8}$ and $y = \frac{6p}{4}$<br>for $2x$ |  |  |
| -        | y - p + 3y = 5p   | M1               | oe equation   |  |  |
| -        | y + 3y = 5p + p or $4y = 6p$  | M1dep            | oe equation with terms collected  |  |  |
|          | Correct simplified terms<br>$(x =) \frac{p}{4}$ or $\frac{1}{4}p$ or $0.25p$<br>and<br>$(y =) \frac{3p}{2}$ or $\frac{3}{2}p$ or $1\frac{1}{2}p$ or $1.5p$  | A2               | A1<br>one correct simplified term<br>or<br>otherwise correct terms for both with 'p'<br>omitted<br>eg $x = 0.25$ and $y = 1.5$<br>or<br>correct unsimplified terms for both<br>eg $x = \frac{2p}{8}$ and $y = \frac{6p}{4}$             |  |  |
| -        | The mark scheme for question 21 continues on the next page  |                  |   |  |  |

| Question | Answer  | Mark  | Comments  |  |
|----------|---|-------|---|--|
|          | Alternative method 3: elimination of <i>x</i>   |       |   |  |
|          | y - 2x = p  | M1    | oe with multiplication of both equations  |  |
|          | y + 3y = 5p + p or $4y = 6p$  | M1dep | oe<br>addition must be seen if result is incorrect  |  |
| 21       | Correct simplified terms<br>$(x =) \frac{p}{4} \text{ or } \frac{1}{4}p \text{ or } 0.25p$<br>and<br>$(y =) \frac{3p}{2} \text{ or } \frac{3}{2}p \text{ or } 1\frac{1}{2}p \text{ or } 1.5p$ | A2    | A1<br>one correct simplified term<br>or<br>otherwise correct terms for both with 'p'<br>omitted<br>eg $x = 0.25$ and $y = 1.5$<br>or<br>correct unsimplified terms for both<br>eg $x = \frac{2p}{8}$ and $y = \frac{6p}{4}$ |  |
| (cont)   | Alternative method 4: elimination of y  |       |   |  |
|          | 3y - 6x = 3p  | M1    | oe with multiplication of both equations  |  |
|          | 2x - (-6x) = 5p - 3p or $8x = 2p$   | M1dep | oe<br>subtraction must be seen if result is<br>incorrect  |  |
|          | Correct simplified terms<br>$(x =) \frac{p}{4} \text{ or } \frac{1}{4}p \text{ or } 0.25p$<br>and<br>$(y =) \frac{3p}{2} \text{ or } \frac{3}{2}p \text{ or } 1\frac{1}{2}p \text{ or } 1.5p$ | A2    | A1<br>one correct simplified term<br>or<br>otherwise correct terms for both with 'p'<br>omitted<br>eg $x = 0.25$ and $y = 1.5$<br>or<br>correct unsimplified terms for both<br>eg $x = \frac{2p}{8}$ and $y = \frac{6p}{4}$ |  |

| Question | Answer   | Mark | Commer                 | nts               |
|----------|--|------|------------------------|-------------------|
|          | -3b + 6a + 7.5b (= 6a + 4.5b)<br>or $6a + 7.5b - 3b (= 6a + 4.5b)$<br>or<br>6a + 7.5b - (6a + 4.5b) = 3b | B1   | oe rearranged equation | using all 5 terms |
| 22(a)    | Addition $3b + 6a + 4.5b = 6a + 7.5b$  |      |                        | B1                |
|          | 6 <b>a</b> + 4.5 <b>b</b> + 3 <b>b</b> = 6 <b>a</b> + 7.5 <b>b</b>                                       |      |                        | B1                |
|          | 7.5 <b>b</b> - 3 <b>b</b> = 4.5 <b>b</b> , so 6 <b>a</b> + 4.5 <b>b</b>                                  |      |                        | B0                |
|          | 6 <b>a</b> + 7.5 <b>b</b> – 3 <b>b</b> = 4.5 <b>b</b>  |      | B0                     |                   |

| Question | Answer  | Mark             | Comments                 |  |
|----------|---|------------------|--------------------------|--|
|          | Alternative method 1: equal ratios from $ka + 3b$ and $6a + 4.5b$   |                  |                          |  |
|          | ( <i>BC</i> =) k <b>a</b> + 3 <b>b</b><br>or k: 6 = 3: 4.5<br>or k: 3 = 6: 4.5  | M1               | oe ratio                 |  |
| -        | 3 × 6 <sub>÷</sub> 4.5<br>or 4 <b>a</b> + 3 <b>b</b>  | M1dep            | oe                       |  |
| -        | 4   | A1               |                          |  |
| -        | Alternative method 2: scale   | factor from ka + | - 3b and 6a + 4.5b       |  |
| 22(b)    | $(BC =) k\mathbf{a} + 3\mathbf{b}$<br>or $4.5 \div 3$ or $\frac{3}{2}$<br>or $3 \div 4.5$ or $\frac{2}{3}$<br>or $4.5 \div 6$ or $\frac{3}{4}$<br>or $6 \div 4.5$ or $\frac{4}{3}$                  | M1               | oe fractions or decimals |  |
|          | $6 \div \text{their } \frac{3}{2}$<br>or $6 \times \text{their } \frac{2}{3}$<br>or $3 \div \text{their } \frac{3}{4}$<br>or $3 \times \text{their } \frac{4}{3}$<br>or $4\mathbf{a} + 3\mathbf{b}$ | M1dep            | Oe                       |  |
| -        | 4   | A1               |                          |  |
| -        | The mark scheme for question  | on 22(b) continu | ues on the next page     |  |

| Question        | Answer   | Mark                           | Comments                 |  |
|-----------------|--|--------------------------------|--------------------------|--|
|                 | Alternative method 3: equal ratios from $(k + 6)a + 7.5b$ and $6a + 4.5b$  |                                |                          |  |
|                 | (BD =) ka + 6a + 7.5b<br>or $(BD =) (k + 6)a + 7.5b$<br>or $(k + 6) : 6 = 7.5 : 4.5$<br>or $(k + 6) : 7.5 = 6 : 4.5$ | M1                             | oe ratio                 |  |
|                 | 6 × 7.5 ÷ 4.5 − 6<br>or 4 <b>a</b> + 3 <b>b</b>  | M1dep                          | oe                       |  |
|                 | 4  | A1                             |                          |  |
|                 | Alternative method 4: scale factor   | <sup>•</sup> from ( <i>k</i> + | 6)a + 7.5b and 6a + 4.5b |  |
| -               | ( <i>BD</i> =) <i>k</i> <b>a</b> + 6 <b>a</b> + 7.5 <b>b</b>   |                                |                          |  |
|                 | or ( <i>BD</i> =) ( <i>k</i> + 6) <b>a</b> + 7.5 <b>b</b>  |                                |                          |  |
|                 | or 7.5 ÷ 4.5 or $\frac{5}{3}$  |                                | oe fractions or decimals |  |
| 22(b)<br>(cont) | or $4.5 \div 7.5$ or $\frac{3}{5}$   | M1                             |                          |  |
|                 | or $4.5 \div 6$ or $\frac{3}{4}$   |                                |                          |  |
|                 | or $6 \div 4.5$ or $\frac{4}{3}$   |                                |                          |  |
|                 | $6 \times \text{their } \frac{5}{3} - 6$   |                                | oe                       |  |
|                 | or $6 \div$ their $\frac{3}{5} - 6$  |                                |                          |  |
|                 | or 7.5 ÷ their $\frac{3}{4}$ – 6   | M1dep                          |                          |  |
|                 | or 7.5 × their $\frac{4}{3}$ – 6   |                                |                          |  |
|                 | or 4 <b>a</b> + 3 <b>b</b>   |                                |                          |  |
|                 | 4  | A1                             |                          |  |
|                 | Additional Guidance for question 2   | 2(b) is on                     | the next page            |  |

| Question        | Answer  | Mark | Comments         |  |  |  |
|-----------------|---|------|------------------|--|--|--|
|                 | uidance   |      |                  |  |  |  |
|                 | Check the diagram for working   |      |                  |  |  |  |
|                 | If working is not seen, only accept exact decimal values in place of fractions for method marks     |      |                  |  |  |  |
| 22(b)<br>(cont) | Answer 4 with no working or no incorre  | I N  | I1M1A1           |  |  |  |
|                 | Assumes that <i>BC</i> is $3a + 2.25b$ (half the or that <i>BC</i> is $2a + 1.5b$ (one third of the | , iv | 10M0A0<br>10M0A0 |  |  |  |
|                 | 4a on the answer line does not get the A mark, but may have scored the method marks                 |      |                  |  |  |  |

| Question | Answer  | Mark  | Comments   |  |
|----------|---|-------|--|--|
|          | Alternative method 1  |       |  |  |
|          | $(8^4 =) (2^3)^4$ or $2^{12}$   |       |  |  |
|          | Or 2 2  | M1    |  |  |
|          | $(32^{\frac{2}{5}} =) (2^5)^{\frac{2}{5}}$ or $2^2$   |       |  |  |
|          | $2^{12}$ and $2^{2}$  |       | or calculation in the form<br>$2^a \div 2^b$ where $a - b = 10$          |  |
|          |   | M1dep | $2 \div 2$ where $a - b = 10$<br>$2^{c} \times 2^{d}$ where $c + d = 10$ |  |
|          | 2 <sup>10</sup>   | A1    | Accept <i>m</i> = 10   |  |
|          | Alternative method 2  |       |  |  |
| 23       | $(8^4 =) 4096 \text{ or } (32^{\frac{2}{5}} =) 4$   | M1    |  |  |
|          | 1024  | M1dep |  |  |
|          | 2 <sup>10</sup>   | A1    | Accept $m = 10$  |  |
|          | Additional Guidance   |       |  |  |
|          | Note that 1024 from 32 × 32 scores 2 marks if 1024 is their final numerical answer  |       |  |  |
|          | However, if they then try to find $\sqrt[5]{1024}$ they are clearly processing $(32^{\frac{2}{5}} =)$ , so this would only score 0 marks without further work |       |  |  |
|          | If a numerical method and an index method are both attempted and an incorrect answer is given, award up to M1M1 from the better method                        |       |  |  |
|          |   |       |  |  |

| 24 | -1 | B1 |  |
|----|----|----|--|
|    |    |    |  |

| Question | Answer   | Mark       | Comme  | nts           |
|----------|--|------------|--|---------------|
|          |  |            |  |               |
|          | (gradient of $OP =$ ) $\frac{8-0}{4-0}$  | M1         | oe eg (gradient of <i>OP</i> =                         | $\frac{8}{4}$ |
|          | (gradient of $OP =$ ) 2 or $\frac{2}{1}$   |            | oe   |               |
|          | and  | A1         | accept 'negative reciprocal, so $-\frac{1}{2}$ '       |               |
|          | $-1 \div 2 = -\frac{1}{2}$ or $2 \times -\frac{1}{2} = -1$   |            | or 'product of gradients is $-1$ , so $-\frac{1}{2}$ ' |               |
| 25(a)    | with M1 seen   |            | oe comment   |               |
|          | Ad   | ditional G | Buidance   |               |
|          | $4 \div 8 = \frac{1}{2}$ but slope is negative, so $-\frac{1}{2}$  |            |  | M0A0          |
|          | Do not accept a gradient including x   |            |  |               |
|          | eg $\frac{8}{4}$ = 2, so gradient of <i>OP</i> = 2 <i>x</i> , product of gradients is -1, so $-\frac{1}{2}x$ |            |  | M1A0          |

| Question | Answer  | Mark      | Comments                               |  |
|----------|---|-----------|--|--|
|          | Alternative method 1: $y = -\frac{1}{2}x + c$ and substitutes 8 and 4   |           |  |  |
|          | $8 = -\frac{1}{2} \times 4 + c$ or $(c =) 10$   | M1        | oe implied by $y = -\frac{1}{2}x + 10$ |  |
|          | $0 = -\frac{1}{2}x + \text{their 10 or } (x =) 20$  | M1dep     | oe                                     |  |
|          | their $20^2$ + their $10^2$ or 500 or $\sqrt{500}$  | M1dep     | oe eg 2 $\sqrt{125}$<br>dep on M2      |  |
|          | 10 √5   | A1        | accept $a = 10$ with $\sqrt{500}$ seen |  |
|          | Alternative method 2: uses the formula for a line and substitutes $x = 0$ and $y = 0$                               |           |  |  |
| 25(b)    | $y - 8 = -\frac{1}{2}(x - 4)$<br>and substitutes $x = 0$ or $y = 0$<br>or $(x =) 20$ or $(y =) 10$                  | M1        | oe equation<br>eg $x + 2y = 20$        |  |
|          | $y - 8 = -\frac{1}{2}(x - 4)$<br>and substitutes $x = 0$<br>and substitutes $y = 0$<br>or $(x =) 20$ and $(y =) 10$ | M1        | oe equation<br>eg $x + 2y = 20$        |  |
|          | their $20^2$ + their $10^2$ or 500<br>or $\sqrt{500}$   | M1dep     | oe eg 2 $\sqrt{125}$ dep on M2         |  |
|          | 10 \sqrt{5}   | A1        | accept $a = 10$ with $\sqrt{500}$ seen |  |
|          | The mark scheme for question 25(  | b) contin | ues on the next page                   |  |

| Question        | Answer  | Mark  | Commer  | nts                          |  |  |
|-----------------|---|-------|---|------------------------------|--|--|
|                 | Alternative method 3: uses formula for gradient with points A and B   |       |   |                              |  |  |
| 25(b)<br>(cont) | $\frac{8-0}{4-x} = -\frac{1}{2}$ or (x =) 20  | M1    | oe correct method to work out the<br>x-coordinate of point A        |                              |  |  |
|                 | $\frac{y-8}{0-4} = -\frac{1}{2}$ or $(y =) 10$  | M1    | oe correct method to work out the<br>y-coordinate of point <i>B</i> |                              |  |  |
|                 | their $20^2$ + their $10^2$ or 500<br>or $\sqrt{500}$   | M1dep | oe eg 2 $\sqrt{125}$ dep on M2                                      |                              |  |  |
|                 | 10√5  | A1    | accept $a = 10$ with $\sqrt{500}$                                   | 0 seen                       |  |  |
|                 | Additional Guidance   |       |   |                              |  |  |
|                 | Check the diagram and 25(a) for possible correct working or values<br>eg 1 20 marked on axis at A<br>eg 2 10 marked on axis at <i>B</i>       |       |   | M1<br>M1                     |  |  |
|                 | On alternative method 2, if using $y - 8 = -\frac{1}{2}(x - 4)$ , they must substitute $x = 0$ or $y = 0$ for M1 and both separately for M1M1 |       |   |                              |  |  |
|                 | On alternative method 2, incorrect rearrangement of $y - 8 = -\frac{1}{2}(x - 4)$ can score up to 3 marks                                     |       |   |                              |  |  |
|                 | eg $y-8 = -\frac{1}{2}(x-4), 2y-8 = -x-4,$  |       |   |                              |  |  |
|                 | when $y = 0, x = 4$ , when $x = 0, y = 2$ , $\sqrt{4^2 + 2^2} = \sqrt{20}$  |       |   | M1M1M1                       |  |  |
| 26              | $(x - 2)^2$ or $(x + 2)^2$ or $a = 2$   | M1    | oe implied by $x^2 + 2x +$<br>or $x^2 + 4x + 4 (+ b)$               | 2 <i>x</i> + 4 (+ <i>b</i> ) |  |  |
|                 | $1 = (3+2)^2 + b$   | M1dep | ое  |                              |  |  |
|                 | -24   | A1    | accept (–2, –24)  | accept (-2, -24)             |  |  |
|                 | Additional Guidance   |       |   |                              |  |  |
|                 | $(x-2)^2 1 = (3-2)^2 + b$   |       |   | M0<br>M0                     |  |  |

| Question | Answer   | Mark  | Comments  |  |  |
|----------|--|-------|---|--|--|
| 27       | $\sin 60^{\circ} = \frac{\sqrt{3}}{2}$<br>or $\tan 30^{\circ} = \frac{\sqrt{3}}{3}$ or $\frac{1}{\sqrt{3}}$<br>or $\tan 30^{\circ} (= \frac{\sin 30}{\cos 30}) = \frac{\frac{1}{2}}{\frac{\sqrt{3}}{2}}$ | M1    | oe<br>may be in a table<br>may be implied by position in<br>multiplication          |  |  |
|          | $\frac{\sqrt{3}}{2} \times \frac{1}{\sqrt{3}} = \frac{1}{2}$<br>or $\cos x = \frac{1}{2}$<br>or $(x =) \cos^{-1} \frac{1}{2}$  | M1dep | oe works out the value of cos <i>x</i> as a fraction or decimal with no surd values |  |  |
|          | 60 with M2 awarded   | A1    |   |  |  |
|          | Additional Guidance  |       |   |  |  |
|          | $\cos x = 60$ does not score the final mark  |       |   |  |  |
|          |  |       |   |  |  |