



ADVANCED SUBSIDIARY GCE
MATHEMATICS (MEI)
 Statistics 1

4766

Candidates answer on the Answer Booklet

OCR Supplied Materials:

- 8 page Answer Booklet
- Graph paper
- MEI Examination Formulae and Tables (MF2)

Other Materials Required:

None

Monday 25 January 2010
Morning

Duration: 1 hour 30 minutes



INSTRUCTIONS TO CANDIDATES

- Write your name clearly in capital letters, your Centre Number and Candidate Number in the spaces provided on the Answer Booklet.
- Use black ink. Pencil may be used for graphs and diagrams only.
- Read each question carefully and make sure that you know what you have to do before starting your answer.
- Answer **all** the questions.
- Do **not** write in the bar codes.
- You are permitted to use a graphical calculator in this paper.
- Final answers should be given to a degree of accuracy appropriate to the context.

INFORMATION FOR CANDIDATES

- The number of marks is given in brackets [] at the end of each question or part question.
- You are advised that an answer may receive **no marks** unless you show sufficient detail of the working to indicate that a correct method is being used.
- The total number of marks for this paper is **72**.
- This document consists of **8** pages. Any blank pages are indicated.

Section A (36 marks)

- 1** A camera records the speeds in miles per hour of 15 vehicles on a motorway. The speeds are given below.

73 67 75 64 52 63 75 81 77 72 68 74 79 72 71

- (i) Construct a sorted stem and leaf diagram to represent these data, taking stem values of 50, 60, [4]
- (ii) Write down the median and midrange of the data. [2]
- (iii) Which of the median and midrange would you recommend to measure the central tendency of the data? Briefly explain your answer. [2]
- 2** In her purse, Katharine has two £5 notes, two £10 notes and one £20 note. She decides to select two of these notes at random to donate to a charity. The total value of these two notes is denoted by the random variable £ X .
- (i) (A) Show that $P(X = 10) = 0.1$. [1]
- (B) Show that $P(X = 30) = 0.2$. [2]

The table shows the probability distribution of X .

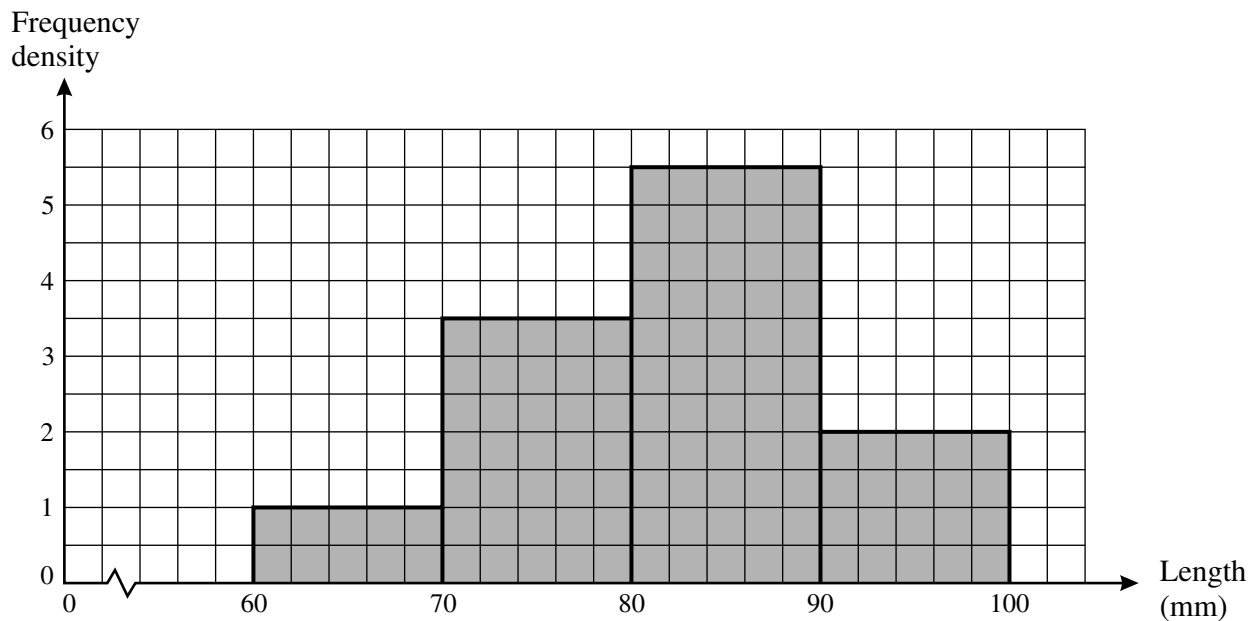
r	10	15	20	25	30
$P(X = r)$	0.1	0.4	0.1	0.2	0.2

- (ii) Find $E(X)$ and $\text{Var}(X)$. [5]
- 3** In a survey, a large number of young people are asked about their exercise habits. One of these people is selected at random.
- G is the event that this person goes to the gym.
 - R is the event that this person goes running.
- You are given that $P(G) = 0.24$, $P(R) = 0.13$ and $P(G \cap R) = 0.06$.
- (i) Draw a Venn diagram, showing the events G and R , and fill in the probability corresponding to each of the four regions of your diagram. [3]
- (ii) Determine whether the events G and R are independent. [2]
- (iii) Find $P(R | G)$. [3]

- 4 In a multiple-choice test there are 30 questions. For each question, there is a 60% chance that a randomly selected student answers correctly, independently of all other questions.
- (i) Find the probability that a randomly selected student gets a total of exactly 20 questions correct. [3]
- (ii) If 100 randomly selected students take the test, find the expected number of students who get exactly 20 questions correct. [2]
- 5 My credit card has a 4-digit code called a PIN. You should assume that any 4-digit number from 0000 to 9999 can be a PIN.
- (i) If I cannot remember any digits and guess my number, find the probability that I guess it correctly. [1]
- In fact my PIN consists of four different digits. I can remember all four digits, but cannot remember the correct order.
- (ii) If I now guess my number, find the probability that I guess it correctly. [2]
- 6 Three prizes, one for English, one for French and one for Spanish, are to be awarded in a class of 20 students.
- Find the number of different ways in which the three prizes can be awarded if
- (i) no student may win more than 1 prize, [2]
- (ii) no student may win all 3 prizes. [2]

Section B (36 marks)

- 7 A pear grower collects a random sample of 120 pears from his orchard. The histogram below shows the lengths, in mm, of these pears.



- (i) Calculate the number of pears which are between 90 and 100 mm long. [2]
- (ii) Calculate an estimate of the mean length of the pears. Explain why your answer is only an estimate. [4]
- (iii) Calculate an estimate of the standard deviation. [3]
- (iv) Use your answers to parts (ii) and (iii) to investigate whether there are any outliers. [4]
- (v) Name the type of skewness of the distribution. [1]
- (vi) Illustrate the data using a cumulative frequency diagram. [5]

- 8 An environmental health officer monitors the air pollution level in a city street. Each day the level of pollution is classified as low, medium or high. The probabilities of each level of pollution on a randomly chosen day are as given in the table.

Pollution level	Low	Medium	High
Probability	0.5	0.35	0.15

- (i) Three days are chosen at random. Find the probability that the pollution level is

(A) low on all 3 days, [2]

(B) low on at least one day, [2]

(C) low on one day, medium on another day, and high on the other day. [3]

- (ii) Ten days are chosen at random. Find the probability that

(A) there are no days when the pollution level is high, [2]

(B) there is exactly one day when the pollution level is high. [3]

The environmental health officer believes that pollution levels will be low more frequently in a different street. On 20 randomly selected days she monitors the pollution level in this street and finds that it is low on 15 occasions.

- (iii) Carry out a test at the 5% level to determine if there is evidence to suggest that she is correct. Use hypotheses $H_0: p = 0.5$, $H_1: p > 0.5$, where p represents the probability that the pollution level in this street is low. Explain why H_1 has this form. [5]

BLANK PAGE

BLANK PAGE

**Copyright Information**

OCR is committed to seeking permission to reproduce all third-party content that it uses in its assessment materials. OCR has attempted to identify and contact all copyright holders whose work is used in this paper. To avoid the issue of disclosure of answer-related information to candidates, all copyright acknowledgements are reproduced in the OCR Copyright Acknowledgements Booklet. This is produced for each series of examinations, is given to all schools that receive assessment material and is freely available to download from our public website (www.ocr.org.uk) after the live examination series.

If OCR has unwittingly failed to correctly acknowledge or clear any third-party content in this assessment material, OCR will be happy to correct its mistake at the earliest possible opportunity.

For queries or further information please contact the Copyright Team, First Floor, 9 Hills Road, Cambridge CB2 1GE.

OCR is part of the Cambridge Assessment Group; Cambridge Assessment is the brand name of University of Cambridge Local Examinations Syndicate (UCLES), which is itself a department of the University of Cambridge.