



GCE

Mathematics (MEI)

Advanced GCE 4757

Further Applications of Advanced Mathematics (FP3)

Mark Scheme for June 2010

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4757

Mark Scheme

June 2010

1 (i)	$\overrightarrow{AC} \times \overrightarrow{AB} = \begin{pmatrix} 5 \\ -8 \\ -26 \end{pmatrix} \times \begin{pmatrix} 2 \\ 1 \\ -2 \end{pmatrix} = \begin{pmatrix} 42 \\ -42 \\ 21 \end{pmatrix}$ <p>Perpendicular distance is $\frac{ \overrightarrow{AC} \times \overrightarrow{AB} }{ \overrightarrow{AB} }$</p> $= \frac{\sqrt{42^2 + 42^2 + 21^2}}{\sqrt{2^2 + 1^2 + 2^2}} = \frac{63}{3} = 21$	B2 M1 M1 A1	Give B1 for one component correct Calculating magnitude of a vector product www 5
	<p>OR $\left[\begin{pmatrix} 3+2\lambda \\ 8+\lambda \\ 27-2\lambda \end{pmatrix} - \begin{pmatrix} 8 \\ 0 \\ 1 \end{pmatrix} \right] \cdot \begin{pmatrix} 2 \\ 1 \\ -2 \end{pmatrix} = 0$</p> $2(2\lambda-5) + (\lambda+8) - 2(-2\lambda+26) = 0$ $\lambda = 6 \quad [\text{F is } (15, 14, 15)]$ $CF = \sqrt{7^2 + 14^2 + 14^2} = 21$	M1 A1 A1 ft M1A1	Appropriate scalar product
(ii)	$\overrightarrow{AB} \times \overrightarrow{CD} = \begin{pmatrix} 2 \\ 1 \\ -2 \end{pmatrix} \times \begin{pmatrix} 3 \\ p \\ p-1 \end{pmatrix} = \begin{pmatrix} 3p-1 \\ -2p-4 \\ 2p-3 \end{pmatrix}$ $\overrightarrow{AC} \cdot (\overrightarrow{AB} \times \overrightarrow{CD}) = \begin{pmatrix} 5 \\ -8 \\ -26 \end{pmatrix} \cdot \begin{pmatrix} 3p-1 \\ -2p-4 \\ 2p-3 \end{pmatrix}$ $= 5(3p-1) - 8(-2p-4) - 26(2p-3) \quad [= -21p+105]$ $ \overrightarrow{AB} \times \overrightarrow{CD} = \sqrt{(3p-1)^2 + (-2p-4)^2 + (2p-3)^2}$ $= \sqrt{17p^2 - 2p + 26}$ <p>Distance is $\frac{ \overrightarrow{AC} \cdot (\overrightarrow{AB} \times \overrightarrow{CD}) }{ \overrightarrow{AB} \times \overrightarrow{CD} } = \frac{21 p-5 }{\sqrt{17p^2 - 2p + 26}}$</p>	B1 B1 B1 M1 A1 ft B1 ft M1A1 (ag)	Correctly obtained 8
(iii)	$V = (\pm) \frac{1}{6} (\overrightarrow{AC} \times \overrightarrow{AB}) \cdot \overrightarrow{AD} = (\pm) \frac{1}{6} \begin{pmatrix} 42 \\ -42 \\ 21 \end{pmatrix} \cdot \begin{pmatrix} 8 \\ p-8 \\ p-27 \end{pmatrix}$ $= (\pm) 56 - 7(p-8) + \frac{7}{2}(p-27)$ $= (\pm) \frac{35}{2} - \frac{7}{2}p$ $= \frac{7}{2} p-5 $	M1 A1 ft M1 A1 A1	Appropriate scalar triple product In any form Evaluation of scalar triple product <i>Dependent on previous M1</i> $\frac{1}{6}(105-21p)$ or better 4
(iv)	<p>Intersect when $p = 5$</p> $\begin{pmatrix} 3 \\ 8 \\ 27 \end{pmatrix} + \lambda \begin{pmatrix} 2 \\ 1 \\ -2 \end{pmatrix} = \begin{pmatrix} 8 \\ 0 \\ 1 \end{pmatrix} + \mu \begin{pmatrix} 3 \\ 5 \\ 4 \end{pmatrix}$ $3+2\lambda = 8+3\mu$ $8+\lambda = 5\mu \quad [8+\lambda = p\mu]$ $27-2\lambda = 1+4\mu \quad [27-2\lambda = 1+(p-1)\mu]$ $\lambda = 7, \mu = 3$ <p>Point of intersection is $(17, 15, 13)$</p>	B1 B1 ft M1 A1 ft A1 ft M1 A1	Equations of both lines (<i>may involve p</i>) Equation for intersection (<i>must have different parameters</i>) Equation involving λ and μ Second equation involving λ and μ <i>or</i> Two equations in λ , μ , p Obtaining λ or μ 7

4757

Mark Scheme

June 2010

2 (i)	$\frac{\partial g}{\partial x} = (y + xy + z^2)e^{x-2y}$ $\frac{\partial g}{\partial y} = (x - 2xy - 2z^2)e^{x-2y}$ $\frac{\partial g}{\partial z} = 2ze^{x-2y}$	M1 A1 A1 4	Partial differentiation
(ii)	At $(2, 1, -1)$, $\frac{\partial g}{\partial x} = 4$, $\frac{\partial g}{\partial y} = -4$, $\frac{\partial g}{\partial z} = -2$ Normal has direction $\begin{pmatrix} 4 \\ -4 \\ -2 \end{pmatrix}$ L passes through $(2, 1, -1)$ and has this direction	M1 A1 M1 A1 (ag) 4	
(iii)	When $g = 0$, $xy + z^2 = 0$ $(2 - 2\lambda)(1 + 2\lambda) + (-1 + \lambda)^2 = 0$ $3 - 3\lambda^2 = 0$ $\lambda = \pm 1$ $\lambda = 1$ gives $P(0, 3, 0)$ $\lambda = -1$ gives $Q(4, -1, -2)$	M1 M1 A1 (ag) A1 4	Obtaining a value of λ Or B1 for verifying $g(0, 3, 0) = 0$ and showing that P is on L
(iv)	At P , $\frac{\partial g}{\partial x} = 3e^{-6}$, $\frac{\partial g}{\partial y} = 0$, $\frac{\partial g}{\partial z} = 0$ $\delta g \approx \frac{\partial g}{\partial x} \delta x + \frac{\partial g}{\partial y} \delta y + \frac{\partial g}{\partial z} \delta z$ $= 3e^{-6}(-2\mu) + 0 + 0 = -6\mu e^{-6}$	M1 M1 A1 (ag) 3	OR give M2 A1 www for $g(-2\mu, 3 + 2\mu, \mu)$ $= (-3\mu^2 - 6\mu)e^{-6\mu-6} \approx -6\mu e^{-6}$
(v)	When $-6\mu e^{-6} \approx h$, $\mu \approx -\frac{1}{6}e^6 h$ Point $(-2\mu, 3 + 2\mu, \mu)$ is approximately $(\frac{1}{3}e^6 h, 3 - \frac{1}{3}e^6 h, -\frac{1}{6}e^6 h)$	M1 A1 (ag) 2	
(vi)	At Q , $\frac{\partial g}{\partial x} = -e^6$, $\frac{\partial g}{\partial y} = 4e^6$, $\frac{\partial g}{\partial z} = -4e^6$ When $x = 4 - 2\mu$, $y = -1 + 2\mu$, $z = -2 + \mu$ $\delta g \approx (-e^6)(-2\mu) + (4e^6)(2\mu) + (-4e^6)(\mu)$ $= 6\mu e^6$ If $6\mu e^6 \approx h$, then $\mu \approx \frac{1}{6}e^{-6} h$ Point is approximately $(4 - \frac{1}{3}e^{-6} h, -1 + \frac{1}{3}e^{-6} h, -2 + \frac{1}{6}e^{-6} h)$	M1 M1 M1A1 M1 A2 7	OR give M1 M2 A1 www for $g(4 - 2\mu, -1 + 2\mu, -2 + \mu)$ $= (-3\mu^2 + 6\mu)e^{-6\mu+6} \approx 6\mu e^6$ Give A1 for one coordinate correct If partial derivatives are not evaluated at Q , max mark is M0M1M0M0

3 (i)	$\frac{dy}{dx} = \frac{1}{2}x^{-\frac{1}{2}} - \frac{1}{2}x^{\frac{1}{2}}$ $1 + \left(\frac{dy}{dx} \right)^2 = 1 + \left(\frac{1}{2}x^{-\frac{1}{2}} - \frac{1}{2}x^{\frac{1}{2}} \right)^2$ $= 1 + \frac{1}{4}x^{-1} - \frac{1}{2} + \frac{1}{4}x = \frac{1}{4}x^{-1} + \frac{1}{2} + \frac{1}{4}x$ $= \left(\frac{1}{2}x^{-\frac{1}{2}} + \frac{1}{2}x^{\frac{1}{2}} \right)^2$	B1 M1 A1	
	Arc length is $\int_0^a \left(\frac{1}{2}x^{-\frac{1}{2}} + \frac{1}{2}x^{\frac{1}{2}} \right) dx$ $= \left[x^{\frac{1}{2}} + \frac{1}{3}x^{\frac{3}{2}} \right]_0^a$ $= a^{\frac{1}{2}} + \frac{1}{3}a^{\frac{3}{2}}$	M1 A1 (ag)	5
(ii)	Curved surface area is $\int 2\pi y \, ds$ $= \int_0^3 2\pi \left(x^{\frac{1}{2}} - \frac{1}{3}x^{\frac{3}{2}} \right) \left(\frac{1}{2}x^{-\frac{1}{2}} + \frac{1}{2}x^{\frac{1}{2}} \right) dx$ $= 2\pi \int_0^3 \left(\frac{1}{2} + \frac{1}{3}x - \frac{1}{6}x^2 \right) dx$ $= 2\pi \left[\frac{1}{2}x + \frac{1}{6}x^2 - \frac{1}{18}x^3 \right]_0^3$ $= 3\pi$	M1 A1 M1A1 A1	For $\int y \, ds$ Correct integral form <i>including limits</i> For $\frac{1}{2}x + \frac{1}{6}x^2 - \frac{1}{18}x^3$ 5
(iii)	When $x = 4$, $\frac{dy}{dx} = -\frac{3}{4}$ Unit normal vector is $\begin{pmatrix} -\frac{3}{5} \\ -\frac{4}{5} \end{pmatrix}$ $\frac{d^2y}{dx^2} = -\frac{1}{4}x^{-\frac{3}{2}} - \frac{1}{4}x^{-\frac{1}{2}} \quad (= -\frac{5}{32})$ $\rho = \frac{\left\{ 1 + (-\frac{3}{4})^2 \right\}^{\frac{3}{2}}}{(-\frac{5}{32})} \quad (= \frac{125/64}{5/32} = \frac{25}{2})$ $\mathbf{c} = \begin{pmatrix} 4 \\ -\frac{2}{3} \end{pmatrix} + \frac{25}{2} \begin{pmatrix} -\frac{3}{5} \\ -\frac{4}{5} \end{pmatrix}$ $= \begin{pmatrix} -3\frac{1}{2} \\ -10\frac{2}{3} \end{pmatrix}$	B1 M1 A1 ft B1 M1 A1 ft M1 A1	Finding a normal vector Correct unit normal (either direction) Applying formula for ρ or κ 9
(iv)	Differentiating partially w.r.t. p $0 = 2p x^{\frac{1}{2}} - p^2 x^{\frac{3}{2}}$ $p = \frac{2}{x}$ Envelope is $y = \frac{4}{x^2} x^{\frac{1}{2}} - \frac{1}{3} \frac{8}{x^3} x^{\frac{3}{2}}$ $y = \frac{4}{3} x^{-\frac{3}{2}}$	M1 A1 M1 A1 M1 A1	

4 (i)	$st(x) = s\left(\frac{x}{x-1}\right) = \frac{\frac{x}{x-1}-1}{\frac{x}{x-1}}$ $= \frac{x-(x-1)}{x} = \frac{1}{x} = r(x)$ $ts(x) = t\left(\frac{x-1}{x}\right) = \frac{\frac{x}{x-1}}{\frac{x-1}{x}-1}$ $= \frac{x-1}{(x-1)-x} = 1-x = q(x)$	M1 A1 (ag) M1 A1	4																																																	
(ii)	<table border="1" style="width: 100%; text-align: center;"> <tr> <td></td><td>p</td><td>q</td><td>r</td><td>s</td><td>t</td><td>u</td></tr> <tr> <td>p</td><td>p</td><td>q</td><td>r</td><td>s</td><td>t</td><td>u</td></tr> <tr> <td>q</td><td>q</td><td>p</td><td>s</td><td>r</td><td>u</td><td>t</td></tr> <tr> <td>r</td><td>r</td><td>u</td><td>p</td><td>t</td><td>s</td><td>q</td></tr> <tr> <td>s</td><td>s</td><td>t</td><td>q</td><td>u</td><td>r</td><td>p</td></tr> <tr> <td>t</td><td>t</td><td>s</td><td>u</td><td>q</td><td>p</td><td>r</td></tr> <tr> <td>u</td><td>u</td><td>r</td><td>t</td><td>p</td><td>q</td><td>s</td></tr> </table>		p	q	r	s	t	u	p	p	q	r	s	t	u	q	q	p	s	r	u	t	r	r	u	p	t	s	q	s	s	t	q	u	r	p	t	t	s	u	q	p	r	u	u	r	t	p	q	s	B3 3	Give B2 for 4 correct, B1 for 2 correct
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Element	p	q	r	s	t	u																																														
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(iv)	$\{p\}$, F $\{p, q\}$, $\{p, r\}$, $\{p, t\}$ $\{p, s, u\}$	B1B1B1 B1 4	<i>Ignore these in the marking</i> Deduct one mark for each non-trivial subgroup in excess of four																																																	
(v)	<table border="1" style="width: 100%; text-align: center;"> <tr> <td>Element</td><td>1</td><td>-1</td><td>$e^{\frac{\pi}{3}j}$</td><td>$e^{-\frac{\pi}{3}j}$</td><td>$e^{\frac{2\pi}{3}j}$</td><td>$e^{-\frac{2\pi}{3}j}$</td><td rowspan="2"></td></tr> <tr> <td>Order</td><td>1</td><td>2</td><td>6</td><td>6</td><td>3</td><td>3</td></tr> </table>	Element	1	-1	$e^{\frac{\pi}{3}j}$	$e^{-\frac{\pi}{3}j}$	$e^{\frac{2\pi}{3}j}$	$e^{-\frac{2\pi}{3}j}$		Order	1	2	6	6	3	3	B4 4	Give B3 for 4 correct, B2 for 3 correct B1 for 2 correct																																		
Element	1	-1	$e^{\frac{\pi}{3}j}$	$e^{-\frac{\pi}{3}j}$	$e^{\frac{2\pi}{3}j}$	$e^{-\frac{2\pi}{3}j}$																																														
Order	1	2	6	6	3	3																																														
(vi)	$2^1 = 2$, $2^2 = 4$, $2^3 = 8$, $2^4 = 16$, $2^5 = 13$, $2^6 = 7$ $2^7 = 14$, $2^8 = 9$, $2^9 = 18$, $2^{10} = 17$, $2^{11} = 15$, $2^{12} = 11$ $2^{13} = 3$, $2^{14} = 6$, $2^{15} = 12$, $2^{16} = 5$, $2^{17} = 10$, $2^{18} = 1$ Hence 2 has order 18	M1 A1 A1 3	Finding (at least two) powers of 2 For $2^6 = 7$ and $2^9 = 18$ Correctly shown <i>All powers listed implies final A1</i>																																																	
(vii)	G is abelian (so all its subgroups are abelian) F is not abelian	B1 1	<i>Can have 'cyclic' instead of 'abelian'</i>																																																	
(viii)	Subgroup of order 6 is $\{1, 2^3, 2^6, 2^9, 2^{12}, 2^{15}\}$ i.e. $\{1, 7, 8, 11, 12, 18\}$	M1 A1 2	or B2																																																	

4757

Mark Scheme

June 2010

Pre-multiplication by transition matrix

5 (i)	$P = \begin{pmatrix} 0.16 & 0.28 & 0.43 & 1 \\ 0.84 & 0 & 0 & 0 \\ 0 & 0.72 & 0 & 0 \\ 0 & 0 & 0.57 & 0 \end{pmatrix}$	B2	Allow tolerance of ± 0.0001 in probabilities throughout this question Give B1 for two columns correct
(ii)	$P^9 = \begin{pmatrix} 1 \\ 0 \\ 0 \\ 0 \end{pmatrix} = \begin{pmatrix} 0.3349 \\ 0.3243 \\ 0.2231 \\ 0.1177 \end{pmatrix}$ Prob(C) = 0.2231	M2 A1	Using P^9 Give M1 for using P^{10}
(iii)	Week 5 $P^4 = \begin{pmatrix} 1 \\ 0 \\ 0 \\ 0 \end{pmatrix} = \begin{pmatrix} 0.5020 \\ 0.2851 \\ 0.1577 \\ 0.0552 \end{pmatrix}$	B1 M1 A1	First column of a power of P SC Give B0M1A1 for Week 9 and 0.3860 0.3098 0.2066 0.0976
(iv)	$P^7 = \begin{pmatrix} \cdot & \cdot & \cdot & \cdot \\ 0.2869 & \cdot & \cdot & \cdot \\ \cdot & \cdot & \cdot & \cdot \\ \cdot & \cdot & \cdot & \cdot \end{pmatrix}$ $P^8 = \begin{pmatrix} \cdot & \cdot & \cdot & \cdot \\ \cdot & \cdot & \cdot & \cdot \\ \cdot & 0.2262 & \cdot & \cdot \\ \cdot & \cdot & \cdot & \cdot \end{pmatrix}$ Probability is $0.2869 \times 0.2262 = 0.0649$	M1M1 M1 A1	Elements from P^7 and P^8 Multiplying appropriate probabilities
(v)	Expected run length is $\frac{1}{1-0.16} = 1.19$ (3 sf)	M1 A1	Allow 1.2
(vi)	$P^n \rightarrow \begin{pmatrix} 0.3585 & 0.3585 & 0.3585 & 0.3585 \\ 0.3011 & 0.3011 & 0.3011 & 0.3011 \\ 0.2168 & 0.2168 & 0.2168 & 0.2168 \\ 0.1236 & 0.1236 & 0.1236 & 0.1236 \end{pmatrix}$ A: 0.3585 B: 0.3011 C: 0.2168 D: 0.1236	M1 M1 A2	Evaluating P^n with $n \geq 10$ or Obtaining (at least) 3 equations from $\mathbf{Pp} = \mathbf{p}$ Limiting matrix with equal columns or Solving to obtain one equilib prob Give A1 for two correct
(vii)	Expected number is $145 \times 0.3585 \approx 52$	M1 A1 ft	
(viii)	$\begin{pmatrix} a & b & c & 1 \\ 1-a & 0 & 0 & 0 \\ 0 & 1-b & 0 & 0 \\ 0 & 0 & 1-c & 0 \end{pmatrix} \begin{pmatrix} 0.4 \\ 0.25 \\ 0.2 \\ 0.15 \end{pmatrix} = \begin{pmatrix} 0.4 \\ 0.25 \\ 0.2 \\ 0.15 \end{pmatrix}$ $0.4a + 0.25b + 0.2c + 0.15 = 0.4$ $0.4(1-a) = 0.25$ $0.25(1-b) = 0.2$ $0.2(1-c) = 0.15$ $a = 0.375, b = 0.2, c = 0.25$	M1 A1 M1 A1	Transition matrix and $\begin{pmatrix} 0.4 \\ 0.25 \\ 0.2 \\ 0.15 \end{pmatrix}$ Forming at least one equation Dependent on previous M1

4757

Mark Scheme

June 2010

Post-multiplication by transition matrix

5 (i)	$\mathbf{P} = \begin{pmatrix} 0.16 & 0.84 & 0 & 0 \\ 0.28 & 0 & 0.72 & 0 \\ 0.43 & 0 & 0 & 0.57 \\ 1 & 0 & 0 & 0 \end{pmatrix}$	B2	2	Allow tolerance of ± 0.0001 in probabilities throughout this question Give B1 for two rows correct
(ii)	$(1 \ 0 \ 0 \ 0) \mathbf{P}^9$ $= (0.3349 \ 0.3243 \ 0.2231 \ 0.1177)$ $\text{Prob}(C) = 0.2231$	M2 A1	3	Using \mathbf{P}^9 Give M1 for using \mathbf{P}^{10}
(iii)	Week 5 $(1 \ 0 \ 0 \ 0) \mathbf{P}^4$ $= (0.5020 \ 0.2851 \ 0.1577 \ 0.0552)$	B1 M1 A1	3	First row of a power of \mathbf{P} SC Give B0M1A1 for Week 9 and 0.3860 0.3098 0.2066 0.0976
(iv)	$\mathbf{P}^7 = \begin{pmatrix} \cdot & 0.2869 & \cdot & \cdot \\ \cdot & \cdot & \cdot & \cdot \\ \cdot & \cdot & \cdot & \cdot \\ \cdot & \cdot & \cdot & \cdot \end{pmatrix} \quad \mathbf{P}^8 = \begin{pmatrix} \cdot & \cdot & \cdot & \cdot \\ \cdot & \cdot & 0.2262 & \cdot \\ \cdot & \cdot & \cdot & \cdot \\ \cdot & \cdot & \cdot & \cdot \end{pmatrix}$ Probability is 0.2869×0.2262 $= 0.0649$	M1M1 M1 A1	4	Elements from \mathbf{P}^7 and \mathbf{P}^8 Multiplying appropriate probabilities
(v)	Expected run length is $\frac{1}{1-0.16} = 1.19$ (3 sf)	M1 A1	2	Allow 1.2
(vi)	$\mathbf{P}^n \rightarrow \begin{pmatrix} 0.3585 & 0.3011 & 0.2168 & 0.1236 \\ 0.3585 & 0.3011 & 0.2168 & 0.1236 \\ 0.3585 & 0.3011 & 0.2168 & 0.1236 \\ 0.3585 & 0.3011 & 0.2168 & 0.1236 \end{pmatrix}$ A: 0.3585 B: 0.3011 C: 0.2168 D: 0.1236	M1 M1 A2	4	Evaluating \mathbf{P}^n with $n \geq 10$ or Obtaining (at least) 3 equations from $\mathbf{p}\mathbf{P} = \mathbf{p}$ Limiting matrix with equal rows or Solving to obtain one equilib prob Give A1 for two correct
(vii)	Expected number is 145×0.3585 ≈ 52	M1 A1 ft	2	
(viii)	$(0.4 \ 0.25 \ 0.2 \ 0.15) \begin{pmatrix} a & 1-a & 0 & 0 \\ b & 0 & 1-b & 0 \\ c & 0 & 0 & 1-c \\ 1 & 0 & 0 & 0 \end{pmatrix}$ $= (0.4 \ 0.25 \ 0.2 \ 0.15)$ $0.4a + 0.25b + 0.2c + 0.15 = 0.4$ $0.4(1-a) = 0.25$ $0.25(1-b) = 0.2$ $0.2(1-c) = 0.15$ $a = 0.375, \ b = 0.2, \ c = 0.25$	M1 A1 M1 A1	4	Transition matrix and $(0.4 \ 0.25 \ 0.2 \ 0.15)$ Forming at least one equation Dependent on previous M1

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1 Hills Road
Cambridge
CB1 2EU

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