

## **Mathematics (MEI)**

Advanced GCE **4773**

Decision Mathematics Computation

# **Mark Scheme for June 2010**

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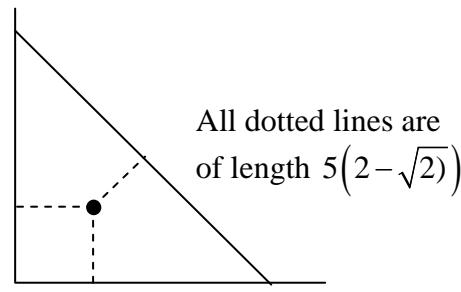
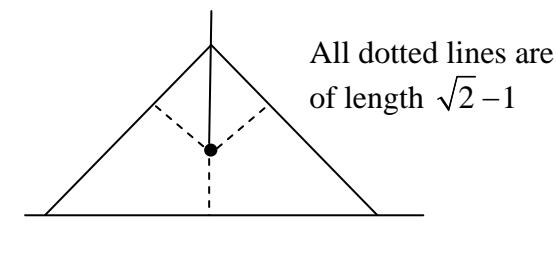
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1.

(i) $u_n = 1.05u_{n-1} - 60$	M1 A2
(ii) $u_n = 1000 \times 1.05^n - 60 \frac{(1.05^n - 1)}{0.05}$ = $1200 - 200 \times 1.05^n$	M1 A2 A1
or $u_n = \lambda 1.05^n + \mu$ $1000 = \lambda + \mu$ $990 = 1.05\lambda + \mu$ , etc	
(iii) $\text{int}(\log(6)/\log(1.05)) = 36$ years (or spreadsheet)	M1 A1
(iv)	
1000	M1
1025	A1
990.625	A1
1015.391	A1
980.7754	
1005.295	
etc.	
(v) 37 years (+ 6 months OK)	B1 cao
(vi)	
1000	M1
970	A1
989.25	A1
959.25	interest OK
977.9625	A1
947.9625	
etc.	
(vii) 35 years	B1 cao

2.

(i) $5\sqrt{2}$	B1												
(ii) e.g:	(negatives of these OK)												
$\begin{aligned} \text{min } & m \\ \text{st } & p-m < 0 \\ & -p-m < 0 \\ & q-m < 0 \\ & -q-m < 0 \\ & -p-q-1.414214m < -10 \\ & p+q-1.414214m < 10 \\ & \text{end} \end{aligned}$	M1 first 2 pairs A1 first pair A1 second pair A1 last pair												
(iii) Objective value: 2.928932													
<table border="1" data-bbox="309 685 1040 797"> <thead> <tr> <th>Variable</th> <th>Value</th> <th>Reduced Cost</th> </tr> </thead> <tbody> <tr> <td>M</td> <td>2.928932</td> <td>0.000000</td> </tr> <tr> <td>P</td> <td>2.928932</td> <td>0.000000</td> </tr> <tr> <td>Q</td> <td>2.928932</td> <td>0.000000</td> </tr> </tbody> </table>	Variable	Value	Reduced Cost	M	2.928932	0.000000	P	2.928932	0.000000	Q	2.928932	0.000000	B1
Variable	Value	Reduced Cost											
M	2.928932	0.000000											
P	2.928932	0.000000											
Q	2.928932	0.000000											
	M1 drawing A1 lines A1 point B1 equidistant												
(iv) e.g: $\begin{aligned} \text{min } & m \\ \text{st } & q-m < 0 \\ & -q-m < 0 \\ & p+q-1.414214m < 1 \\ & -p-q-1.414214m < -1 \\ & p-q-1.414214m < -1 \\ & -p+q-1.414214m < 1 \\ & \text{end} \end{aligned}$	M1 A1 first pair A1 second pair A1 third pair												
(v) Objective value: 0.4142135													
<table border="1" data-bbox="309 1527 1040 1650"> <thead> <tr> <th>Variable</th> <th>Value</th> <th>Reduced Cost</th> </tr> </thead> <tbody> <tr> <td>M</td> <td>0.4142135</td> <td>0.000000</td> </tr> <tr> <td>Q</td> <td>0.4142135</td> <td>0.000000</td> </tr> <tr> <td>P</td> <td>0.000000</td> <td>0.000000</td> </tr> </tbody> </table>	Variable	Value	Reduced Cost	M	0.4142135	0.000000	Q	0.4142135	0.000000	P	0.000000	0.000000	B1
Variable	Value	Reduced Cost											
M	0.4142135	0.000000											
Q	0.4142135	0.000000											
P	0.000000	0.000000											
(vi) 	B1 lines B1 point B1 distances												

3.

(i) Min $2x_{11} + 3x_{12} + 7x_{13} + x_{21} + 8x_{22} + 4x_{23}$ st $x_{11} + x_{12} + x_{13} = 10$ $x_{21} + x_{22} + x_{23} = 10$ $x_{11} + x_{21} < 7$ $x_{12} + x_{22} < 7$ $x_{13} + x_{23} < 7$ end	B1 supplies B1 depots																																							
(ii) Objective value: 55.00000 <table> <thead> <tr> <th>Variable</th> <th>Value</th> <th>Reduced Cost</th> </tr> </thead> <tbody> <tr> <td><math>x_{11}</math></td> <td>3.000000</td> <td>0.000000</td> </tr> <tr> <td><math>x_{12}</math></td> <td>7.000000</td> <td>0.000000</td> </tr> <tr> <td><math>x_{13}</math></td> <td>0.000000</td> <td>3.000000</td> </tr> <tr> <td><math>x_{21}</math></td> <td>4.000000</td> <td>0.000000</td> </tr> <tr> <td><math>x_{22}</math></td> <td>0.000000</td> <td>6.000000</td> </tr> <tr> <td><math>x_{23}</math></td> <td>6.000000</td> <td>0.000000</td> </tr> </tbody> </table> <p>3 containers from S1 to D1            7 containers from S1 to D2            4 containers from S2 to D1            6 containers from S2 to D3            total cost = 55</p>	Variable	Value	Reduced Cost	$x_{11}$	3.000000	0.000000	$x_{12}$	7.000000	0.000000	$x_{13}$	0.000000	3.000000	$x_{21}$	4.000000	0.000000	$x_{22}$	0.000000	6.000000	$x_{23}$	6.000000	0.000000	B1 logistics B1 cost																		
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(iii) Min $2y_{11} + 3y_{12} + 9y_{13} + y_{14} + 4y_{21} + 7y_{22} + 2y_{23}$ $+ 5y_{24} + y_{31} + 5y_{32} + 3y_{33} + 6y_{34}$ st $y_{11} + y_{12} + y_{13} + y_{14} = 7$ $y_{21} + y_{22} + y_{23} + y_{24} = 7$ $y_{31} + y_{32} + y_{33} + y_{34} = 6$ $y_{11} + y_{21} + y_{31} = 7$ $y_{12} + y_{22} + y_{32} = 4$ $y_{13} + y_{23} + y_{33} = 6$ $y_{14} + y_{24} + y_{34} = 3$ end	B1 depots B1 demands																																							
(iv) Objective value: 37.00000 <table> <thead> <tr> <th>Variable</th> <th>Value</th> <th>Reduced Cost</th> </tr> </thead> <tbody> <tr> <td><math>y_{11}</math></td> <td>0.000000</td> <td>2.000000</td> </tr> <tr> <td><math>y_{12}</math></td> <td>4.000000</td> <td>0.000000</td> </tr> <tr> <td><math>y_{13}</math></td> <td>0.000000</td> <td>11.000000</td> </tr> <tr> <td><math>y_{14}</math></td> <td>3.000000</td> <td>0.000000</td> </tr> <tr> <td><math>y_{21}</math></td> <td>1.000000</td> <td>0.000000</td> </tr> <tr> <td><math>y_{22}</math></td> <td>0.000000</td> <td>0.000000</td> </tr> <tr> <td><math>y_{23}</math></td> <td>6.000000</td> <td>0.000000</td> </tr> <tr> <td><math>y_{24}</math></td> <td>0.000000</td> <td>0.000000</td> </tr> <tr> <td><math>y_{31}</math></td> <td>6.000000</td> <td>0.000000</td> </tr> <tr> <td><math>y_{32}</math></td> <td>0.000000</td> <td>1.000000</td> </tr> <tr> <td><math>y_{33}</math></td> <td>0.000000</td> <td>4.000000</td> </tr> <tr> <td><math>y_{34}</math></td> <td>0.000000</td> <td>4.000000</td> </tr> </tbody> </table> <p>4 containers from D1 to C2            3 containers from D1 to C4            1 container from D2 to C1            6 containers from D2 to C3            6 containers from D3 to C1            total cost = 37</p>	Variable	Value	Reduced Cost	$y_{11}$	0.000000	2.000000	$y_{12}$	4.000000	0.000000	$y_{13}$	0.000000	11.000000	$y_{14}$	3.000000	0.000000	$y_{21}$	1.000000	0.000000	$y_{22}$	0.000000	0.000000	$y_{23}$	6.000000	0.000000	$y_{24}$	0.000000	0.000000	$y_{31}$	6.000000	0.000000	$y_{32}$	0.000000	1.000000	$y_{33}$	0.000000	4.000000	$y_{34}$	0.000000	4.000000	B1 logistics + cost
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(v)	$  \begin{aligned}  \text{min} \quad & 2x_{11} + 3x_{12} + 7x_{13} + x_{21} + 8x_{22} + 4x_{23} + 2y_{11} + 3y_{12} \\  & + 9y_{13} + y_{14} + 4y_{21} + 7y_{22} + 2y_{23} + 5y_{24} + y_{31} + 5y_{32} \\  & + 3y_{33} + 6y_{34} \\  \text{st} \quad & x_{11} + x_{12} + x_{13} = 10 \\  & x_{21} + x_{22} + x_{23} = 10 \\  & y_{11} + y_{21} + y_{31} = 7 \\  & y_{12} + y_{22} + y_{32} = 4 \\  & y_{13} + y_{23} + y_{33} = 6 \\  & y_{14} + y_{24} + y_{34} = 3 \\  & x_{11} + x_{21} < 7 \\  & x_{12} + x_{22} < 7 \\  & x_{13} + x_{23} < 7 \\  & y_{11} + y_{12} + y_{13} + y_{14} - x_{11} - x_{21} = 0 \\  & y_{21} + y_{22} + y_{23} + y_{24} - x_{12} - x_{22} = 0 \\  & y_{31} + y_{32} + y_{33} + y_{34} - x_{13} - x_{23} = 0  \end{aligned}  $ <p>end</p>	B1																																																									
(vi)	Objective value: 91.00000																																																										
	<table> <thead> <tr> <th>Variable</th> <th>Value</th> <th>Reduced Cost</th> </tr> </thead> <tbody> <tr><td>x<sub>11</sub></td><td>4.000000</td><td>0.000000</td></tr> <tr><td>x<sub>12</sub></td><td>6.000000</td><td>0.000000</td></tr> <tr><td>x<sub>13</sub></td><td>0.000000</td><td>2.000000</td></tr> <tr><td>x<sub>21</sub></td><td>3.000000</td><td>0.000000</td></tr> <tr><td>x<sub>22</sub></td><td>0.000000</td><td>6.000000</td></tr> <tr><td>x<sub>23</sub></td><td>7.000000</td><td>0.000000</td></tr> <tr><td>y<sub>11</sub></td><td>0.000000</td><td>0.000000</td></tr> <tr><td>y<sub>12</sub></td><td>4.000000</td><td>0.000000</td></tr> <tr><td>y<sub>13</sub></td><td>0.000000</td><td>8.000000</td></tr> <tr><td>y<sub>14</sub></td><td>3.000000</td><td>0.000000</td></tr> <tr><td>y<sub>21</sub></td><td>0.000000</td><td>1.000000</td></tr> <tr><td>y<sub>22</sub></td><td>0.000000</td><td>3.000000</td></tr> <tr><td>y<sub>23</sub></td><td>6.000000</td><td>0.000000</td></tr> <tr><td>y<sub>24</sub></td><td>0.000000</td><td>3.000000</td></tr> <tr><td>y<sub>31</sub></td><td>7.000000</td><td>0.000000</td></tr> <tr><td>y<sub>32</sub></td><td>0.000000</td><td>3.000000</td></tr> <tr><td>y<sub>33</sub></td><td>0.000000</td><td>3.000000</td></tr> <tr><td>y<sub>34</sub></td><td>0.000000</td><td>6.000000</td></tr> </tbody> </table>	Variable	Value	Reduced Cost	x <sub>11</sub>	4.000000	0.000000	x <sub>12</sub>	6.000000	0.000000	x <sub>13</sub>	0.000000	2.000000	x <sub>21</sub>	3.000000	0.000000	x <sub>22</sub>	0.000000	6.000000	x <sub>23</sub>	7.000000	0.000000	y <sub>11</sub>	0.000000	0.000000	y <sub>12</sub>	4.000000	0.000000	y <sub>13</sub>	0.000000	8.000000	y <sub>14</sub>	3.000000	0.000000	y <sub>21</sub>	0.000000	1.000000	y <sub>22</sub>	0.000000	3.000000	y <sub>23</sub>	6.000000	0.000000	y <sub>24</sub>	0.000000	3.000000	y <sub>31</sub>	7.000000	0.000000	y <sub>32</sub>	0.000000	3.000000	y <sub>33</sub>	0.000000	3.000000	y <sub>34</sub>	0.000000	6.000000	B1
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	Suboptimising does not give the optimum	B1 cao																																																									

4.

(i)	e.g. = lookup(rand(),A1:A3,B1:B3) with <table style="margin-left: 40px;"> <tr><td></td><td style="text-align: center;">A</td><td style="text-align: center;">B</td></tr> <tr><td style="text-align: center;">1</td><td style="text-align: center;">0</td><td style="text-align: center;">0</td></tr> <tr><td style="text-align: center;">2</td><td style="text-align: center;">0.1</td><td style="text-align: center;">1</td></tr> <tr><td style="text-align: center;">3</td><td style="text-align: center;">0.6</td><td style="text-align: center;">2</td></tr> </table>		A	B	1	0	0	2	0.1	1	3	0.6	2	M1 A1
	A	B												
1	0	0												
2	0.1	1												
3	0.6	2												
(ii)	Many approaches possible, but all must allow for 3 applications of part (i) Offspring from generation 0 Conditional offspring from generation 1(s) Output	B2 B1 B1 M1A1 M1A1 B1												
(iii)	Theoretical probabilities (Galton-Watson branching): <table style="margin-left: 40px;"> <tr><td style="text-align: center;">0</td><td style="text-align: center;">1</td><td style="text-align: center;">2</td><td style="text-align: center;">3</td><td style="text-align: center;">4</td></tr> <tr><td style="text-align: center;">0.154</td><td style="text-align: center;">0.29</td><td style="text-align: center;">0.332</td><td style="text-align: center;">0.16</td><td style="text-align: center;">0.064</td></tr> </table>	0	1	2	3	4	0.154	0.29	0.332	0.16	0.064	M1 A1		
0	1	2	3	4										
0.154	0.29	0.332	0.16	0.064										
(iv)	Two independent runs. Sum the numbers in the two second generations. (or nested "IF"s) 0, 1, 2, 3, 4, 5, 6, 7, 8	B1 B1 (M1 A1) B1												

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