

# **Mathematics (MEI)**

Advanced Subsidiary GCE

Unit **4776**: Numerical Methods

## **Mark Scheme for January 2011**

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4776

## Mark Scheme

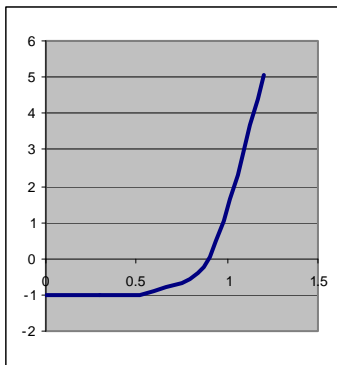
January 2011

Question			Answer	Marks	Guidance																																																
4	(i)		Max poss loss: 365 (or 366) times 0.01 pence: = 3.65 (or 3.66) pence Arises if each daily amount would round up but gets chopped down Average loss 1.825 (or 1.83) pence, because average is half of max.	B1 E1 B1 E1 [4]																																																	
	(ii)		£150 000 divided by 1.825 pence: about 8.2 million (8 million) accounts	M1 A1 [2]																																																	
5			<table><tr><td><math>x</math></td><td><math>P(x)</math></td><td><math>\Delta P(x)</math></td><td><math>\Delta^2 P(x)</math></td><td><math>\Delta^3 P(x)</math></td><td></td></tr><tr><td><i>-1</i></td><td><i>-11</i></td><td></td><td></td><td></td><td>(i) bold:</td></tr><tr><td><b>1</b></td><td><b>-10</b></td><td><i>1</i></td><td></td><td></td><td>Diff table</td></tr><tr><td><b>3</b></td><td><b>3</b></td><td><b>13</b></td><td><i>12</i></td><td></td><td>3rd diffs constant</td></tr><tr><td><b>5</b></td><td><b>44</b></td><td><b>41</b></td><td><b>28</b></td><td><i>16</i></td><td>so cubic</td></tr><tr><td><b>7</b></td><td><b>129</b></td><td><b>85</b></td><td><b>44</b></td><td><b>16</b></td><td>(ii) italic:</td></tr><tr><td><b>9</b></td><td><b>274</b></td><td><b>145</b></td><td><b>60</b></td><td><b>16</b></td><td>working forwards</td></tr><tr><td><i>11</i></td><td><i>495</i></td><td><i>221</i></td><td><i>76</i></td><td><i>16</i></td><td>working backwards</td></tr></table>	$x$	$P(x)$	$\Delta P(x)$	$\Delta^2 P(x)$	$\Delta^3 P(x)$		<i>-1</i>	<i>-11</i>				(i) bold:	<b>1</b>	<b>-10</b>	<i>1</i>			Diff table	<b>3</b>	<b>3</b>	<b>13</b>	<i>12</i>		3rd diffs constant	<b>5</b>	<b>44</b>	<b>41</b>	<b>28</b>	<i>16</i>	so cubic	<b>7</b>	<b>129</b>	<b>85</b>	<b>44</b>	<b>16</b>	(ii) italic:	<b>9</b>	<b>274</b>	<b>145</b>	<b>60</b>	<b>16</b>	working forwards	<i>11</i>	<i>495</i>	<i>221</i>	<i>76</i>	<i>16</i>	working backwards	M1 A1 E1 B1  M1 A1 M1 A1 [4] + [4]	
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6	(i)		<table><tr><td><math>x</math></td><td><math>f</math></td><td><math>g</math></td><td><math>h</math></td><td>abs err <math>g</math></td><td>rel err <math>g</math></td><td>abs err <math>h</math></td><td>rel err <math>h</math></td></tr><tr><td>0.2</td><td>0.013351</td><td>0.013333</td><td>0.013423</td><td>0.0000179</td><td>-0.0013424</td><td>0.0000716</td><td>0.0053600</td></tr><tr><td>0.1</td><td>0.003334</td><td>0.003333</td><td>0.003339</td><td>0.0000011</td><td>-0.0003339</td><td>0.0000045</td><td>0.0013350</td></tr><tr><td></td><td>A1</td><td>A1</td><td>A1</td><td>A1</td><td>A1</td><td>A1</td><td>A1</td></tr></table>	$x$	$f$	$g$	$h$	abs err $g$	rel err $g$	abs err $h$	rel err $h$	0.2	0.013351	0.013333	0.013423	0.0000179	-0.0013424	0.0000716	0.0053600	0.1	0.003334	0.003333	0.003339	0.0000011	-0.0003339	0.0000045	0.0013350		A1	A1	A1	A1	A1	A1	A1	abs M1  rel M1  [9]	$f, g, h$ values may be implied																
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	(ii)		Errors in $g$ and $h$ are of opposite sign; $g$ is about 4 times as accurate as $h$ . <table><tr><td><math>x</math></td><td><math>f</math></td><td><math>(4g + h)/5</math></td><td>abs err</td><td>rel err</td></tr><tr><td>0.2</td><td>0.013351</td><td>0.013351</td><td>-2.5E-08</td><td>-1.9E-06</td></tr><tr><td>0.1</td><td>0.003334</td><td>0.003334</td><td>-4E-10</td><td>-1.2E-07</td></tr><tr><td></td><td></td><td>A1</td><td>A1</td><td>A1</td></tr></table>	$x$	$f$	$(4g + h)/5$	abs err	rel err	0.2	0.013351	0.013351	-2.5E-08	-1.9E-06	0.1	0.003334	0.003334	-4E-10	-1.2E-07			A1	A1	A1	E1 E1  M1  [6]																													
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	(iii)		$x / \sin x \approx 1.000\,000\,002 \approx 1$ $g(10^{-4}) = 3.33 \times 10^{-9}$ Subtraction of nearly equal quantities	B1 B1 E1 [3]																																																	

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Question			Answer	Marks	Guidance																
7	(i)		<p><math>f(0) = -1</math><math>f(1) = 1</math> (hence root) <math>f'(x) = 7x^6 + 5x^4</math> which is zero only at <math>x = 0</math>. Convincing argument that this is not a turning point No turning points implies no other roots.</p> 	<p>B1 M1 A1 B1 E1</p> <p>G2</p> <p>[7]</p>																	
	(ii)		<p>NR iteration: <math>x_{r+1} = x_r - (x_r^7 + x_r^5 - 1) / (7x_r^6 + 5x_r^4)</math></p> <table><tr><td><math>r</math></td><td>0</td><td>1</td><td>2</td></tr><tr><td><math>x_r</math></td><td>0.6</td><td>1.51756</td><td>1.289164</td></tr></table> <p>On graph: tangent at 0.6, intersection at 1.5, ordinate &amp; tangent, intersection at 1.3</p>	$r$	0	1	2	$x_r$	0.6	1.51756	1.289164	<p>B1</p> <p>A1 A1 G4</p> <p>[7]</p>									
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	(iii)		<table><tr><td><math>r</math></td><td>0</td><td>1</td><td>2</td></tr><tr><td><math>x_r</math></td><td>0.3</td><td>22.1703</td><td>19.00128</td></tr></table> <p>Comment: e.g. converging but initially very slow (or difficult to tell with only 2 iter'ns)</p> <table><tr><td><math>r</math></td><td>0</td><td>1</td><td>2</td></tr><tr><td><math>x_r</math></td><td>0.9</td><td>0.890174</td><td>0.889891</td></tr></table> <p>Comment: e.g. almost converged, root very close to 0.89</p>	$r$	0	1	2	$x_r$	0.3	22.1703	19.00128	$r$	0	1	2	$x_r$	0.9	0.890174	0.889891	<p>A1 E1</p> <p>A1 E1</p> <p>[4]</p>	
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