



GCE

Mathematics (MEI)

Advanced Subsidiary GCE

Unit **4761**: Mechanics 1

Mark Scheme for June 2011

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All Examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

Mark schemes should be read in conjunction with the published question papers and the Report on the Examination.

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comment

You should expect to follow through from one part to another unless the scheme says otherwise but not follow through within a part unless the scheme specifies this.

Each script must be viewed as a whole at some stage so that

(i) a candidate's writing of letters, digits, symbols on diagrams etc can be better interpreted;

(ii) repeated mistakes can be recognised (e.g. calculator in wrong angle mode throughout – penalty 1 in the script and FT except given answers).

You are advised to 'set height' in *scoris*, particularly for question 7(ii). Questions 5 and 8(v) also spread onto two pages.

Q 1		mark	notes
	$v^2 = 11^2 + 2 \times (-9.8) \times 2.4$ $v = 8.6$ so 8.6 m s^{-1} .	M1 A1 A1	Use of $v^2 = u^2 + 2as$ or complete sequence of correct <i>suvat</i> . Accept sign errors in substitution. All correct cao [Award all marks if 8.6 seen WWW] Do not condone ± 8.6 .
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Q 2	mark	comment
<p>either</p> <p>for u first: $8 = \frac{1}{2}(u + 2.25) \times 32$</p> <p>$u = -1.75$ so 1.75 m s^{-1}</p> <p>$2.25 = -1.75 + 32a$</p> <p>$a = 0.125$ so 0.125 m s^{-2}</p> <p>Directions of u and a are defined</p>	<p>M1</p> <p>A1</p> <p>M1</p> <p>F1</p> <p>F1</p> <p>5</p>	<p>Using $s = \frac{1}{2}(u + v)t$</p> <p>Use of any appropriate <i>suvat</i> with their values and correct signs</p> <p>Sign must be consistent with their u, FT from their value of u</p> <p>Establish directions of both u and a in terms of A and B. May be shown by a diagram, eg showing A and B and a line between them together with an arrow to show the positive direction. Without a diagram, the wording must be absolutely clear: eg do not accept left/right, forwards/backwards without a diagram or more explanation. Dependent on both M marks.</p>
<p>Or</p> <p>for a first: $8 = 2.25 \times 32 - \frac{1}{2} \times a \times 32^2$</p> <p>$a = 0.125$ so 0.125 m s^{-2}</p> <p>$2.25 = u + 32 \times 0.125$</p> <p>$u = -1.75$ so 1.75 m s^{-1}</p> <p>Directions of u and a are defined</p>	<p>M1</p> <p>A1</p> <p>M1</p> <p>F1</p> <p>F1</p> <p>5</p>	<p>Using $s = vt - \frac{1}{2}at^2$</p> <p>Use of any appropriate <i>suvat</i> with their values and correct signs</p> <p>Sign must be consistent with their a, FT from their value of a</p> <p>Establish directions of both u and a in terms of A and B. May be shown by a diagram, eg showing A and B and a line between them together with an arrow to show the positive direction. Without a diagram, the wording must be absolutely clear: eg do not accept left/right, forwards/backwards without a diagram or more explanation. Dependent on both M marks.</p>
<p>Or using simultaneous equations</p> <p>Set up one relevant equation with a and u.</p> <p>Set up second relevant equation with a and u.</p> <p>Solving to find $u = -1.75$ so 1.75 m s^{-1}</p> <p>Solving to find $a = 0.125$ so 0.125 m s^{-2}</p> <p>Directions of u and a are defined</p>	<p>M1</p> <p>M1</p> <p>A1</p> <p>F1</p> <p>F1</p> <p>5</p>	<p>Using one of $v = u + at$, $s = ut + \frac{1}{2}at^2$ and $v^2 = u^2 + 2as$</p> <p>Using another of $v = u + at$, $s = ut + \frac{1}{2}at^2$ and $v^2 = u^2 + 2as$</p> <p>FT from their value of u or a, whichever found first</p> <p>Establish directions of both u and a in terms of A and B. May be shown by a diagram, eg showing A and B and a line between them together with an arrow to show the positive direction. Without a diagram, the wording must be absolutely clear: eg do not accept left/right, forwards/backwards without a diagram or more explanation. Dependent on both M marks.</p>
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Q 3		mark	Notes
(i)	$-6 = -2 \times 3$ so $y = 3 \times 3 = 9$ and $z = -4 \times 3 = -12$	M1 A1 2	May be implied Both correct [Award 2 for both correct answers seen WW]
(ii)	$\begin{pmatrix} -2 \\ 3 \\ -4 \end{pmatrix} + \begin{pmatrix} 3 \\ -5 \\ -1 \end{pmatrix} = 5\mathbf{a}$ $\mathbf{a} = \begin{pmatrix} 0.2 \\ -0.4 \\ -1 \end{pmatrix} \text{ so accn is } \begin{pmatrix} 0.2 \\ -0.4 \\ -1 \end{pmatrix} \text{ m s}^{-2}$ Magnitude is $\sqrt{0.2^2 + (-0.4)^2 + (-1)^2}$ $= 1.09544\dots$ so 1.10 m s^{-2} , (3 s. f.)	M1 B1 A1 M1 F1 5 7	Use of Newton's 2 nd Law in vector form for all 3 cpts of attempted resultant Treat use of wrong vectors as MR. Correct LHS The acceleration may be written as a magnitude in a given direction. FT their values. Condone missing brackets. Condone no – signs. Accept 1.1. Accept surd form. Must come from a vector with 3 non-zero components for a

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Q 4		mark	Comment
(i)		B1 B1 2	Any one force in correct direction correctly labelled with arrow or all forces with correct directions and arrows. A force may be replaced by its components if labelled correctly eg $mg\cos 20^\circ$, $mg\sin 20^\circ$. All correct (Accept words for labels and weight as W , mg , 147 (N)) No extra or duplicate forces. Do not allow force and its components unless components are clearly distinguished, eg by broken lines.
(ii)	Either Up the plane $P\cos 20^\circ - 15 \times 9.8 \times \sin 20^\circ = 0$ $P = 53.50362\dots$ so 53.5 (3 s. f.)	M1 A1 A1 3	Attempt to resolve at least one force up plane. Accept mass not weight. No extra forces. If other directions used, all forces must be present but see below for resolving vertically and horizontally. Accept only error as consistent $s \leftrightarrow c$. Cao
	Or Vertically and horizontally $R\cos 20^\circ = 15g$, $R\sin 20^\circ = P$ Eliminate R $P = \frac{15g}{\cos 20^\circ} \times \sin 20^\circ$ $P = 53.5$ (3.s.f.)	M1 A1 A1 3	Attempt to resolve all forces both horizontally and vertically and attempt to combine into a single equation. No extra forces. Accept $s \leftrightarrow c$. Accept mass not weight. Accept only error as consistent $s \leftrightarrow c$. Cao
	Or Triangle of forces Triangle drawn and labelled $\frac{P}{15g} = \tan 20^\circ$ $P = 53.5$ (3.s.f.)	M1 A1 A1 3	All sides must be labelled and in correct orientation; three forces only; condone no arrows Oe Cao
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Q 5		mark	notes
	<p>Usual notation either consider height: Attempt to substitute for u and a in $s = ut + \frac{1}{2}at^2$ $y = 30 \sin 35^\circ t - 4.9t^2$ Need $y = 0$ for time of flight T giving $T = \frac{30 \sin 35^\circ}{4.9}$ ($= 3.511692\dots$)</p>	<p>M1 A1 B1 A1</p>	<p>Accept: g as $g, \pm 9.8, \pm 9.81, \pm 10; u = 30; s \leftrightarrow c$. Derivation need not be shown cao. Any form. May not be explicit.</p>
	<p>Or Consider time to top Attempt to substitute for u and a in $v = u + at$ $v = 30 \sin 35^\circ - 9.8t$ Need $v = 0$ and to double for time of flight T giving $T = \frac{30 \sin 35^\circ}{4.9}$ ($= 3.511692\dots$)</p>	<p>M1 A1 B1 A1</p>	<p>Accept: g as $g, \pm 9.8, \pm 9.81, \pm 10; u = 30; s \leftrightarrow c$. Derivation need not be shown cao. Any form. May not be explicit.</p>
	<p>then $x = 30 \cos 35^\circ T$ so $x = 30 \cos 35^\circ \times \frac{30 \sin 35^\circ}{4.9}$ ($= 86.29830\dots$) Required time for sound is $x/343$ Total time is $3.511692\dots + 0.251598\dots = 3.76329\dots$ so 3.76 s (3 s. f.)</p>	<p>M1 F1 M1 A1</p>	<p>Accept $s \leftrightarrow c$ if consistent with above FT for their time Condone consistent $s \leftrightarrow c$ error (which could lead to correct answer here). FT from their x cao following fully correct working throughout question.</p>
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Q6		mark	notes
(i)	<p>Either using <i>suvat</i>:</p> <p>Use of $\mathbf{v} = \mathbf{u} + t\mathbf{a}$ $\mathbf{v} = 4\mathbf{i} - 2t\mathbf{j}$ Use of $\mathbf{r} = (\mathbf{r}_0 +) t\mathbf{u} + \frac{1}{2} t^2\mathbf{a}$ $+ 3\mathbf{j}$ $\mathbf{r} = 4t\mathbf{i} + (3 - t^2)\mathbf{j}$</p>	<p>M1 A1 M1 B1 A1 5</p>	<p>Column vectors may be used throughout; lose 1 mark once if \mathbf{j} components put at top or if fraction line included. . Notation used must be clear.</p> <p>substitution required. Must be vectors.</p> <p>substitution required. \mathbf{r}_0 not required. Must be vectors. May be seen on either side of a meaningful equation for \mathbf{r} Accept $\mathbf{r} = 3\mathbf{j} + 4t\mathbf{i} - \frac{1}{2} \times 2 \times t^2 \mathbf{j}$ oe written in a correct notation. Isw, providing not reduced to scalar: (see 12c in marking instructions)</p>
	<p>Or using integration:</p> <p>$\mathbf{v} = \int \mathbf{a} dt$ $\mathbf{v} = 4\mathbf{i} - 2t\mathbf{j}$ $\mathbf{r} = \int \mathbf{v} dt$ $+ 3\mathbf{j}$ $\mathbf{r} = 4t\mathbf{i} + (3 - t^2)\mathbf{j}$</p>	<p>M1 A1 M1 B1 A1 5</p>	<p>Attempt at integration. Condone no '+c'. Must be vectors. cao</p> <p>Integrate their \mathbf{v} but must contain 2 components. Must be vectors. May be seen on either side of a meaningful equation for \mathbf{r} Accept $\mathbf{r} = 3\mathbf{j} + 4t\mathbf{i} - \frac{1}{2} \times 2 \times t^2 \mathbf{j}$ oe written in a correct notation. Isw, providing not reduced to scalar: (see 12e in marking instructions)</p>
		5	
(ii)	<p>$\mathbf{v}(2.5) = 4\mathbf{i} - 5\mathbf{j}$ Angle is $(90+) \arctan \frac{5}{4}$ $= 141.34019\dots$ so 141° (3 s. f.)</p>	<p>B1 M1 A1 3</p>	<p>FT their \mathbf{v} Award for arctan attempted oe. FT their values. Allow argument to be $\pm (\text{their } i \text{ cpt})/(\text{their } j \text{ cpt})$ or $\pm (\text{their } j \text{ cpt})/(\text{their } i \text{ cpt})$. Allow this mark if bearing of position vector attempted. cao</p>
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Q7		mark	notes
(i)	$\frac{-20}{2} = -10$ -10 m s^{-2}	M1 A1 2	Use of a suitable triangle to attempt at $\Delta v / \Delta t$ for suitable interval. Accept wrong sign. cao. Allow both marks if correct answer seen.
(ii) (A) (B)	Signed area under graph $\frac{1}{2} \times 2 \times 20 = 20$	M1 A1	Using the relevant area or other complete method
	either using areas Signed area $2 \leq t \leq 5$ is $\frac{1}{2} \times ((5-2) + (4.5-2.4)) \times (-4) = -10.2$ Signed area $5 \leq t \leq 6$ is $\frac{1}{2} \times 1 \times 8 = 4$ Total displacement is 13.8 m	B1 B1 B1	Allow + 10.2. cao but FT from their 20 in part (A)
	or using <i>suvat</i> From $t = 0$ to $t = 2.4$: 19.2 From $t = 4.5$ to $t = 6$: 3.0 From $t = 2.4$ to $t = 4.5$: -8.4 Total : 13.8	B1 B1 B1	Both required and both must be correct.
		5	
(iii)	$a = 4t - 14$ $a(0.5) = -12$ so -12 m s^{-2}	M1 A1 A1 3	Differentiate. Do not award for division by t .
(iv)	Model A gives -4 m s^{-1} For model B we need v when $a = 0$ $v\left(\frac{7}{2}\right) = -4.5$ so model B is 0.5 m s^{-1} less	B1 M1 A1 F1 4	May be implied by other working Using (iii) or an argument based on symmetry or sketch graph that $a = 0$ when $t = 3.5$ Accept values without more or less

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(v)	<p>Displacement is $\int_0^6 (2t^2 - 14t + 20) \, dt$</p> $= \left[\frac{2t^3}{3} - 7t^2 + 20t \right]_0^6$ <p>= 12 so 12 m.</p>	<p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>4</p>	<p>Do not penalise poor notation</p> <p>Limits not required.</p> <p>Limits not required. Accept 2 terms correct.</p> <p>Substitute limits cao. Accept bottom limit not substituted.</p>
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Q 8		mark	notes
(i)	25 N	B1 1	Condone no units. Do not accept -25 N.
(ii)	50 cos 25 = 45.31538... so 45.3 N (3 s. f.)	M1 A1 2	Attempt to resolve 50 N. Accept $s \leftrightarrow c$. No extra forces. cao but accept - 45.3.
(iii)	Resolving vertically $R + 50 \sin 25 - 8 \times 9.8 = 0$ $R = 57.26908...$ so 57.3 N (3 s. f.)	M1 A1 A1 3	All relevant forces with resolution of 50 N. No extras. Accept $s \leftrightarrow c$. All correct.
(iv)	Newton's 2 nd Law in direction DC $50 \cos 25 - 20 = 18a$ $a = 1.4064105...$ so 1.41 m s ⁻² (3 s. f.)	M1 A1 A1 3	Newton's 2nd Law with $m = 18$. Accept $F = mga$. Attempt at resolving 50 N. Allow 20 N omitted and $s \leftrightarrow c$. No extra forces. Allow only sign error and $s \leftrightarrow c$. cao
Q8	continued		
(v)	Resolution of weight down the slope	B1	$mg \sin 5^\circ$ where $m = 8$ or 10 or 18, wherever first seen
	either Newton's 2 nd Law down slope overall $18 \times 9.8 \times \sin 5 - 20 = 18a$ $a = -0.2569...$ Newton's 2 nd Law down slope. Force in rod can be taken as tension or thrust. Taking it as tension T gives For D: $10 \times 9.8 \times \sin 5 - 15 - T = 10a$ (For C: $8 \times 9.8 \times \sin 5 - 5 + T = 8a$) $T = -3.888...$ = - 3.89 N (3 s. f.) The force is a thrust	M1 A1 M1 F1 A1 A1	$F = ma$. Must have 20 N and $m = 18$. Allow weight not resolved and use of mass. Accept $s \leftrightarrow c$ and sign errors (including inconsistency between the 15 N and the 5 N). cao $F = ma$. Must consider the motion of either C or D and include: component of weight, resistance and T . No extra forces. Condone sign errors and $s \leftrightarrow c$. Do not condone inconsistent value of mass. FT only applies to a , and only if direction is consistent. '+ T ' if T taken as a thrust '- T ' if T taken as a thrust If T taken as thrust, then $T = +3.89$. Dependent on T correct

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	<p>or Newton's 2nd Law down slope. Force in rod can be taken as tension or thrust. Taking it as tension T gives</p> <p>For C: $8 \times 9.8 \times \sin 5 - 5 + T = 8a$ For D: $10 \times 9.8 \times \sin 5 - 15 - T = 10a$ $a = -0.2569 \dots T = -3.888 \dots = -3.89 \text{ N (3s.f.)}$</p> <p>The force is a thrust</p>	<p>M1</p> <p>M1</p> <p>A1</p> <p>A1</p> <p>F1</p> <p>A1</p>	<p>$F = ma$. Must consider the motion of C and include: component of weight, resistance and T. No extra forces. Condone sign errors and $s \leftrightarrow c$. Do not condone inconsistent value of mass.</p> <p>$F = ma$. Must consider the motion of D and include: component of weight, resistance and T. No extra forces. Condone sign errors and $s \leftrightarrow c$. Do not condone inconsistent value of mass.</p> <p>Award for either the equation for C or the equation for D correct. '-T' if T taken as a thrust '+T' if T taken as a thrust</p> <p>First of a and T found is correct. If T taken as thrust, then $T = +3.89$. The second of a and T found is FT Dependent on T correct</p>
	<p>then After 2 s: $v = 3 + 2 \times a$ $v = 2.4860303 \dots$ so 2.49 m s^{-1} (3 s. f.)</p>	<p>M1</p> <p>F1</p> <p>9</p>	<p>Allow sign of a not followed. FT their value of a. Allow change to correct sign of a at this stage. FT from magnitude of their a but must be consistent with its direction.</p>
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