

## **Mathematics (MEI)**

Advanced GCE

Unit **4762**: Mechanics 2

### **Mark Scheme for June 2012**

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All examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

Mark schemes should be read in conjunction with the published question papers and the report on the examination.

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## Annotations and abbreviations

Annotation in scores	Meaning
✓ and ✗	
BOD	Benefit of doubt
FT	Follow through
ISW	Ignore subsequent working
M0, M1	Method mark awarded 0, 1
A0, A1	Accuracy mark awarded 0, 1
B0, B1	Independent mark awarded 0, 1
SC	Special case
^	Omission sign
MR	Misread
Highlighting	

Other abbreviations in mark scheme	Meaning
E1	Mark for explaining
U1	Mark for correct units
G1	Mark for a correct feature on a graph
M1 dep*	Method mark dependent on a previous mark, indicated by *
cao	Correct answer only
oe	Or equivalent
rot	Rounded or truncated
soi	Seen or implied
www	Without wrong working

**Subject-specific Marking Instructions**

- a Annotations should be used whenever appropriate during your marking.

**The A, M and B annotations must be used on your standardisation scripts for responses that are not awarded either 0 or full marks.**  
It is vital that you annotate standardisation scripts fully to show how the marks have been awarded.

For subsequent marking you must make it clear how you have arrived at the mark you have awarded.

- b An element of professional judgement is required in the marking of any written paper. Remember that the mark scheme is designed to assist in marking incorrect solutions. Correct *solutions* leading to correct answers are awarded full marks but work must not be judged on the answer alone, and answers that are given in the question, especially, must be validly obtained; key steps in the working must always be looked at and anything unfamiliar must be investigated thoroughly.

Correct but unfamiliar or unexpected methods are often signalled by a correct result following an *apparently* incorrect method. Such work must be carefully assessed. When a candidate adopts a method which does not correspond to the mark scheme, award marks according to the spirit of the basic scheme; if you are in any doubt whatsoever (especially if several marks or candidates are involved) you should contact your Team Leader.

- c The following types of marks are available.

**M**

A suitable method has been selected and *applied* in a manner which shows that the method is essentially understood. Method marks are not usually lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, eg by substituting the relevant quantities into the formula. In some cases the nature of the errors allowed for the award of an M mark may be specified.

**A**

Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated Method mark is earned (or implied). Therefore M0 A1 cannot ever be awarded.

**B**

Mark for a correct result or statement independent of Method marks.

**E**

A given result is to be established or a result has to be explained. This usually requires more working or explanation than the establishment of an unknown result.

Unless otherwise indicated, marks once gained cannot subsequently be lost, eg wrong working following a correct form of answer is ignored. Sometimes this is reinforced in the mark scheme by the abbreviation isw. However, this would not apply to a case where a candidate passes through the correct answer as part of a wrong argument.

- d When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. (The notation 'dep \*' is used to indicate that a particular mark is dependent on an earlier, asterisked, mark in the scheme.) Of course, in practice it may happen that when a candidate has once gone wrong in a part of a question, the work from there on is worthless so that no more marks can sensibly be given. On the other hand, when two or more steps are successfully run together by the candidate, the earlier marks are implied and full credit must be given.
- e The abbreviation ft implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A and B marks are given for correct work only — differences in notation are of course permitted. A (accuracy) marks are not given for answers obtained from incorrect working. When A or B marks are awarded for work at an intermediate stage of a solution, there may be various alternatives that are equally acceptable. In such cases, exactly what is acceptable will be detailed in the mark scheme rationale. If this is not the case please consult your Team Leader.

Sometimes the answer to one part of a question is used in a later part of the same question. In this case, A marks will often be 'follow through'. In such cases you must ensure that you refer back to the answer of the previous part question even if this is not shown within the image zone. You may find it easier to mark follow through questions candidate-by-candidate rather than question-by-question.

- f Unless units are specifically requested, there is no penalty for wrong or missing units as long as the answer is numerically correct and expressed either in SI or in the units of the question. (eg lengths will be assumed to be in metres unless in a particular question all the lengths are in km, when this would be assumed to be the unspecified unit.)

We are usually quite flexible about the accuracy to which the final answer is expressed and we do not penalise over-specification.

#### **When a value is given in the paper**

Only accept an answer correct to at least as many significant figures as the given value. This rule should be applied to each case.

#### **When a value is not given in the paper**

Accept any answer that agrees with the correct value to 2 s.f.

ft should be used so that only one mark is lost for each distinct accuracy error, except for errors due to premature approximation which should be penalised only once in the examination.

There is no penalty for using a wrong value for g. E marks will be lost except when results agree to the accuracy required in the question.

## g Rules for replaced work

If a candidate attempts a question more than once, and indicates which attempt he/she wishes to be marked, then examiners should do as the candidate requests.

If there are two or more attempts at a question which have not been crossed out, examiners should mark what appears to be the last (complete) attempt and ignore the others.

NB Follow these maths-specific instructions rather than those in the assessor handbook.

h For a *genuine* misreading (of numbers or symbols) which is such that the object and the difficulty of the question remain unaltered, mark according to the scheme but following through from the candidate's data. A penalty is then applied; 1 mark is generally appropriate, though this may differ for some units. This is achieved by withholding one A mark in the question.

Marks designated as cao may be awarded as long as there are no other errors. E marks are lost unless, by chance, the given results are established by equivalent working.

'Fresh starts' will not affect an earlier decision about a misread.

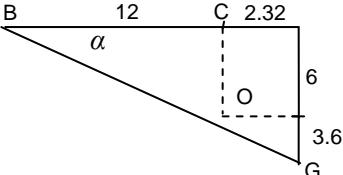
Note that a miscopy of the candidate's own working is not a misread but an accuracy error.

## i If a graphical calculator is used, some answers may be obtained with little or no working visible. Allow full marks for correct answers (provided, of course, that there is nothing in the wording of the question specifying that analytical methods are required). Where an answer is wrong but there is some evidence of method, allow appropriate method marks. Wrong answers with no supporting method score zero. If in doubt, consult your Team Leader.

## j If in any case the scheme operates with considerable unfairness consult your Team Leader.

Question		Answer	Marks	Guidance
1	(a) (i)	KE change: $\frac{1}{2} \times 0.6 \times (7.5^2 - 5.5^2)$ = 7.8 J GPE change: $0.6 \times 9.8 \times 1.5 = 8.82$ J	M1 A1 B1 [3]	Difference of two KE terms  Allow -8.82J
1	(a) (ii)	$W$ is work done against resistance $7.8 = 8.82 - W$ so $W = 1.02$ J	M1 A1 [2]	W-E all terms. Allow sign errors FT (i) only. Also FT only if mod (their KE) < mod (their PE) -1.02 gets M1A0; 16.62 gets M1A0
1	(a) (iii)	Average resistance is $F$ so $F \times 1.5 = 1.02$ so $F = 0.68$ Power is $0.68 \times 5.5$ = 3.74 so 3.74 W	M1 A1 M1 A1 [4]	Use of $WD = Fs$ OR find $a = 8.667$ and use $F = 0.6g - 0.6 \times 8.667$ May be implied. FT (ii) Use of $P = Fv$ any calculated F cao
1	(b) (i)	$R = mg \cos 40$ $F_{\max} = mg \sin 40$ $F_{\max} = \mu R$ so $\mu = \frac{mg \sin 40}{mg \cos 40} = \tan 40$	B1 B1 M1 E1 [4]	Seen or implied Seen or implied Use of $F = \mu R$ : substitute $F$ and $R$  This is the minimum amount of working needed to earn the E1 Must see explicit evidence of method Note: $g$ omitted, treat as MR
1	(b) (ii)	<b>EITHER</b>  $\tan 40 \times 0.8 \times 9.8 \times \cos 20$ $\times 3 (= 18.545)$  $(+) 0.8 \times 9.8$ $\times 3 \sin 20 (= 8.044)$  $= 26.5897\dots$ so 26.6 J (3 s.f.)	B1 M1 B1 M1 A1	Use of $F_{\max} = \mu R$ with $\tan 40$ and $\cos 20$ Use of $WD = Fs$ NOTE: This mark may be awarded here or for use in PE term Use of $mgh$ Allow $\sin \leftrightarrow \cos$ interchange  Two relevant terms added Cao Allow 26.7 Allow 27 Omission of $g$ can get B0M1B1M1A0

Question		Answer	Marks	Guidance
		<b>OR</b> $\tan 40 \times 0.8 \times 9.8 \times \cos 20 (= 6.182)$ $(+) 0.8 \times 9.8 \times \sin 20 (= 2.68)$ $(= 8.8632444\dots)$ WD is $3 \times 8.8632444\dots$ $= 26.5897\dots$ so 26.6 J (3 s.f.)	B1 B1 M1 M1 A1 <b>[5]</b>	Use of $F_{\max} = \mu R$ with $\tan 40$ and $\cos 20$ Allow $\sin \leftrightarrow \cos$ interchange Two relevant forces added Use of $WD = Fs$ (for at least one of forces) cao Omission of $g$ can get B0B1M1M1A0
<b>2</b>	(i)	a.c. moments about B $10T_C - 15 \times 2 = 0$ so $T_C = 3$ . Tension at C is 3 N $\uparrow T_C + T_B - 15 = 0$ so $T_B = 12$ . Tension at B is 12 N	M1 A1 M1 F1 <b>[4]</b>	Moments with all forces present, no extra forces. May take moments again
<b>2</b>	(ii)	a.c. moments about A $25T \sin 30 - 15 \times 17 = 0$ so $T = 20.4$ At A Let force $\uparrow$ be $Y$ N $\uparrow Y + T \sin 30 - 15 = 0$ so $Y = 4.8$ $\rightarrow X = T \cos 30 = 17.6669\dots$ N $\sqrt{4.8^2 + (T \cos 30)^2}$ $= 18.3073755\dots$ so 18.3 N (3 s.f.)	M1 A1 B1 B1 M1 A1 <b>[6]</b>	Attempt at moments with resolution; allow $\cos \leftrightarrow \sin$ error. All forces present, no extra forces cao FT (can take moments about C) FT Need not be evaluated cao
<b>2</b>	(iii)	Let force be $P$ . a.c. moments about D. $8 \times 15 - 12 \times P = 0$ so $P = 10$ on point of tipping Using $F_{\max} = \mu R$ on point of slipping with $R = 15$ gives $F_{\max} = 0.65 \times 15 = 9.75$ so slips first	M1 A1 M1 B1 A1 E1 <b>[6]</b>	Moments about D with all forces present, no extra forces cao cao cao and WWW

Question			Answer	Marks	Guidance
3	(a)	(i)	$300 \begin{pmatrix} \bar{x} \\ \bar{y} \end{pmatrix} = 72 \begin{pmatrix} -6 \\ 3 \end{pmatrix} + 192 \begin{pmatrix} 4 \\ -6 \end{pmatrix} + 36 \begin{pmatrix} 10 \\ -4 \end{pmatrix}$ $\begin{pmatrix} \bar{x} \\ \bar{y} \end{pmatrix} = \begin{pmatrix} 696 \\ -1080 \end{pmatrix}$ so $\bar{x} = 2.32$ $\bar{y} = -3.6$	B1 M1 B1 A1 A1 <b>[5]</b>	Correctly identifying the position of the c.m. of triangle EFH (10, -4) A systematic method for at least 1 cpt <i>Either</i> all x or all y values correct <i>or</i> 2 vector terms correct <i>or</i> allow one common error in both components, e.g. one wrong mass, misunderstanding of c.m. of triangle Allow FT for either if only error is common to both
3	(a)	(ii)	 centre of mass is at G $\tan \alpha = \frac{9.6}{14.32}$ so $\alpha = 33.8376\dots$ so $33.8^\circ$ (3 s.f.)	M1* B1 M1dep* A1 <b>[4]</b>	Identifying correct angle. May be implied At least 1 relevant distance found. FT (i) Use of $\arctan \frac{9.6}{14.32}$ or $\arctan \frac{14.32}{9.6}$ o.e. cao or $180^\circ - 33.8^\circ$
3	(b)	(i)	Marking given tension and thrust Marking all other forces internal to rods acting on A, B and C (as T or C)	B1 B1 <b>[2]</b>	Each labelled with magnitude and correct direction Need ALL forces at A, B and C. Need pairs of arrows on AB, AC and BC

Question		Answer	Marks	Guidance
3	(b) (ii)	<p>Equilibrium at A <math>\uparrow</math></p> $T_{AB} \cos 30 - 18 = 0$ $T_{AB} = 12\sqrt{3}$ . Force in AB: $12\sqrt{3}$ N (T) <p>A <math>\leftarrow</math></p> $T_{AC} + T_{AB} \cos 60 + 5 = 0$ $T_{AC} = -(5 + 6\sqrt{3})$ . <p>Force in AC: <math>(5 + 6\sqrt{3})</math> N (C)</p> <p>At B in direction AB</p> $T_{BR} \cos 60 - T_{AB} = 0$ <p>so <math>T_{BR} = 24\sqrt{3}</math></p> <p>At B in direction BC</p> $T_{BC} - T_{BR} \cos 30 = 0$ $T_{BC} = 36$ . Force in BC: 36 N (T)	M1 A1 M1 F1 M1 F1 A1 [7]	Equilibrium at one pin-joint 20.8 Sign consistent with tension on their diagram -15.39 FT their $T_{AB}$ Allow FT Other methods are possible, but award this M1 only for a complete method that would lead to $T_{BC}$ cao WWW T/C all correct
4	(i)	$26t = 3 \times 13$ $t = 1.5$ so 1.5 s	M1 A1 [2]	Use of $Ft = m(v - u)$ or N2L to find $a$ ( $= 26/3$ ) and use $v = u + at$ cao
4	(ii)	PCLM $10 \times 0 + 3 \times 13 = 10v_Q + 3v_P$ $39 = 10v_Q + 3v_P$ NEL $\frac{v_Q - v_P}{0 - 13} = -e$ $v_Q - v_P = 13e$ $v_Q = 3(1 + e)$ $v_P = 3 - 10e$	M1 A1 M1 A1 M1 B1 E1 [7]	Use of PCLM Any form Use of NEL. Allow sign errors but not inversion Any form Eliminating one of $v_Q$ or $v_P$ OR allow substitution of given result in one equation and check both answers in other equation cao; aef Properly shown

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## Mark Scheme

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Question		Answer	Marks	Guidance
4	(iii)	Need $v_P < 0$ so $3 - 10e < 0$ Hence $\frac{3}{10} < e \leq 1$	M1 A1 [2]	Accept $\leq$ cao (Allow $e \leq 1$ omitted) Correct answer www gets 2/2
4	(iv)	When $e > \frac{3}{10}$ , its speed is $10e - 3$ We require $(10e - 3) > 3(1 + e)$ so $7e > 6$ and so $\frac{6}{7} < e \leq 1$	M1 M1 A1 A1 [4]	FT their $v_Q$ SC1 for $(3 - 10e) > \pm 3(1 + e)$ FT their $v_Q$ cao. Allow $e > \frac{6}{7}$ (0.857) Correct answer www gets 4/4
4	(v)	<b>Either</b> $v_Q = 4.5$ and $v_P = -2$ When they collide the speed of Q is $-4.5$ and of P is 2 PCLM $10 \times -4.5 + 3 \times 2 = 13V$ so $V = -3$ and velocity is $-3 \text{ m s}^{-1}$	M1 M1 M1 A1 [4]	Substitute $e = 0.5$ ; FT their $v_Q$ Change signs of their velocities Use of PCLM Allow sign errors cao; OR $3 \text{ m s}^{-1}$ to the right or use argument about final LM is $-ve$ of original LM
		<b>Or</b> $10(-3(1+e)) + 3(10e - 3) = 13V$ $-39 = 13V$ so $V = -3$ and velocity is $-3 \text{ m s}^{-1}$	M1 M1 M1 A1 [4]	Use of PCLM; Allow sign errors ; FT their $v_Q$ Change signs of their velocities Simplify cao; OR $3 \text{ m s}^{-1}$ to the right
4	(vi)	$3(-3 - 2) = -15 \text{ N s}$	B1 [1]	FT $3(\text{their}(v) - 2)$ Using $10(-3 + 4.5) = 15$ gets B0 until it leads to correct answer

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