

## **Mathematics (MEI)**

Advanced GCE

Unit **4763**: Mechanics 3

# **Mark Scheme for January 2013**

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This mark scheme is published as an aid to teachers and students, to indicate the requirements of the examination. It shows the basis on which marks were awarded by examiners. It does not indicate the details of the discussions which took place at an examiners' meeting before marking commenced.

All examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

Mark schemes should be read in conjunction with the published question papers and the report on the examination.

OCR will not enter into any discussion or correspondence in connection with this mark scheme.

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## Annotations and abbreviations

Annotation in scores	Meaning
✓ and ✗	
BOD	Benefit of doubt
FT	Follow through
ISW	Ignore subsequent working
M0, M1	Method mark awarded 0, 1
A0, A1	Accuracy mark awarded 0, 1
B0, B1	Independent mark awarded 0, 1
SC	Special case
^	Omission sign
MR	Misread
Highlighting	

Other abbreviations in mark scheme	Meaning
E1	Mark for explaining
U1	Mark for correct units
G1	Mark for a correct feature on a graph
M1 dep*	Method mark dependent on a previous mark, indicated by *
cao	Correct answer only
oe	Or equivalent
rot	Rounded or truncated
soi	Seen or implied
www	Without wrong working

**Subject-specific Marking Instructions for GCE Mathematics (MEI) Mechanics strand**

a. Annotations should be used whenever appropriate during your marking.

**The A, M and B annotations must be used on your standardisation scripts for responses that are not awarded either 0 or full marks.** It is vital that you annotate standardisation scripts fully to show how the marks have been awarded.

For subsequent marking you must make it clear how you have arrived at the mark you have awarded.

b. An element of professional judgement is required in the marking of any written paper. Remember that the mark scheme is designed to assist in marking incorrect solutions. Correct *solutions* leading to correct answers are awarded full marks but work must not be judged on the answer alone, and answers that are given in the question, especially, must be validly obtained; key steps in the working must always be looked at and anything unfamiliar must be investigated thoroughly.

Correct but unfamiliar or unexpected methods are often signalled by a correct result following an *apparently* incorrect method. Such work must be carefully assessed. When a candidate adopts a method which does not correspond to the mark scheme, award marks according to the spirit of the basic scheme; if you are in any doubt whatsoever (especially if several marks or candidates are involved) you should contact your Team Leader.

c. The following types of marks are available.

**M**

A suitable method has been selected and *applied* in a manner which shows that the method is essentially understood. Method marks are not usually lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, eg by substituting the relevant quantities into the formula. In some cases the nature of the errors allowed for the award of an M mark may be specified.

**A**

Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated Method mark is earned (or implied). Therefore M0 A1 cannot ever be awarded.

**B**

Mark for a correct result or statement independent of Method marks.

**E**

A given result is to be established or a result has to be explained. This usually requires more working or explanation than the establishment of an unknown result.

Unless otherwise indicated, marks once gained cannot subsequently be lost, eg wrong working following a correct form of answer is ignored. Sometimes this is reinforced in the mark scheme by the abbreviation isw. However, this would not apply to a case where a candidate passes through the correct answer as part of a wrong argument.

- d. When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. (The notation 'dep \*' is used to indicate that a particular mark is dependent on an earlier, asterisked, mark in the scheme.) Of course, in practice it may happen that when a candidate has once gone wrong in a part of a question, the work from there on is worthless so that no more marks can sensibly be given. On the other hand, when two or more steps are successfully run together by the candidate, the earlier marks are implied and full credit must be given.
- e. The abbreviation ft implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A and B marks are given for correct work only – differences in notation are of course permitted. A (accuracy) marks are not given for answers obtained from incorrect working. When A or B marks are awarded for work at an intermediate stage of a solution, there may be various alternatives that are equally acceptable. In such cases, exactly what is acceptable will be detailed in the mark scheme rationale. If this is not the case please consult your Team Leader.

Sometimes the answer to one part of a question is used in a later part of the same question. In this case, A marks will often be 'follow through'. In such cases you must ensure that you refer back to the answer of the previous part question even if this is not shown within the image zone. You may find it easier to mark follow through questions candidate-by-candidate rather than question-by-question.

- f. Unless units are specifically requested, there is no penalty for wrong or missing units as long as the answer is numerically correct and expressed either in SI or in the units of the question. (eg lengths will be assumed to be in metres unless in a particular question all the lengths are in km, when this would be assumed to be the unspecified unit.)

We are usually quite flexible about the accuracy to which the final answer is expressed and we do not penalise over-specification.

**When a value is given in the paper**

Only accept an answer correct to at least as many significant figures as the given value. This rule should be applied to each case.

**When a value is not given in the paper**

Accept any answer that agrees with the correct value to 2 s.f.

ft should be used so that only one mark is lost for each distinct error made in the accuracy to which working is done or an answer given.

Refer cases to your Team Leader where the same type of error (eg errors due to premature approximation leading to error) has been made in different questions or parts of questions.

There are some mistakes that might be repeated throughout a paper. If a candidate makes such a mistake, (eg uses a calculator in wrong angle mode) then you will need to check the candidate's script for repetitions of the mistake and consult your Team Leader about what penalty should be given.

There is no penalty for using a wrong value for  $g$ . E marks will be lost except when results agree to the accuracy required in the question.

g. Rules for replaced work

If a candidate attempts a question more than once, and indicates which attempt he/she wishes to be marked, then examiners should do as the candidate requests.

If there are two or more attempts at a question which have not been crossed out, examiners should mark what appears to be the last (complete) attempt and ignore the others.

NB Follow these maths-specific instructions rather than those in the assessor handbook.

h. For a *genuine* misreading (of numbers or symbols) which is such that the object and the difficulty of the question remain unaltered, mark according to the scheme but following through from the candidate's data. A penalty is then applied; 1 mark is generally appropriate, though this may differ for some units. This is achieved by withholding one A mark in the question.

Marks designated as cao may be awarded as long as there are no other errors. E marks are lost unless, by chance, the given results are established by equivalent working.

'Fresh starts' will not affect an earlier decision about a misread.

Note that a miscopy of the candidate's own working is not a misread but an accuracy error.

i. If a graphical calculator is used, some answers may be obtained with little or no working visible. Allow full marks for correct answers (provided, of course, that there is nothing in the wording of the question specifying that analytical methods are required). Where an answer is wrong but there is some evidence of method, allow appropriate method marks. Wrong answers with no supporting method score zero. If in doubt, consult your Team Leader.

j. If in any case the scheme operates with considerable unfairness consult your Team Leader.

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## Mark Scheme

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Question		Answer	Marks	Guidance	
1	(a)	$A\omega = 5.1$ $4.5^2 = \omega^2(A^2 - 6^2)$ $4.5^2 = 5.1^2 - 36\omega^2$ $\omega = 0.4$ Period $(\frac{2\pi}{\omega})$ is $5\pi = 15.7$ s (3 sf) Amplitude ( $A$ ) is 12.75 m	B1 M1 A1 M1 A1 A1 <b>[6]</b>	Using $v^2 = \omega^2(A^2 - x^2)$ Eliminating $A$ or $\omega$  Allow $5\pi$	
1	(b)	(i)	$[F] = MLT^{-2}$ $[G] = \left[ \frac{Fd^2}{m_1 m_2} \right] = \frac{MLT^{-2}L^2}{M^2}$ $= M^{-1}L^3T^{-2}$	B1 M1 A1 <b>[3]</b>	Obtaining dimensions of $G$
1	(b)	(ii)	$T^{-1} = (M^{-1}L^3T^{-2})^\alpha M^\beta L^\gamma$ $\alpha = \frac{1}{2}$ $-\alpha + \beta = 0$ $\beta = \frac{1}{2}$ $3\alpha + \gamma = 0$ $\gamma = -\frac{3}{2}$	B1 M1 A1 M1 A1 <b>[5]</b>	Considering powers of $M$ Considering powers of $L$  <i>All marks FT from wrong [G] if comparable. No FT within part (ii).</i>

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Question		Answer	Marks	Guidance	
1	(b) (iii)	$\omega = 2.0 \times 10^{-6} \times \left( \frac{4.86 \times 10^{14}}{2500} \right)^{\frac{1}{2}} \times \left( \frac{30000}{50} \right)^{-\frac{3}{2}}$	M1M1 A1	For $\left( \frac{4.86 \times 10^{14}}{2500} \right)^{\frac{1}{2}}$ and $\left( \frac{30000}{50} \right)^{\frac{3}{2}}$ Correct equation for $\omega$	Requires $\beta \neq 0, \gamma \neq 0$ <i>FT if comparable</i>
	OR	$2.0 \times 10^{-6} = k \times G^{\frac{1}{2}} \times 2500^{\frac{1}{2}} \times 50^{-\frac{3}{2}}$ $kG^{\frac{1}{2}} = 1.414 \times 10^{-5}$ $\omega = 1.414 \times 10^{-5} \times (4.86 \times 10^{14})^{\frac{1}{2}} \times 30000^{-\frac{3}{2}}$		M1 Requires $\beta \neq 0$ or $\gamma \neq 0$ M1 Requires $\beta \neq 0$ and $\gamma \neq 0$ A1 Correct equation for $\omega$	Condone the use of any value for $G$ (including $G=1$ ) <i>FT if comparable</i>
		Angular speed is $6.0 \times 10^{-5} \text{ rad s}^{-1}$	A1 [4]	CAO	
2	(a) (i)	$\frac{1}{2}mv^2 - \frac{1}{2}m(1.2)^2 = mg(0.8 - 0.8 \cos \frac{1}{6}\pi)$ $v^2 = 3.5407$ Radial component $\left( \frac{v^2}{0.8} \right)$ is $4.43 \text{ ms}^{-2}$ (3 sf) $(\pm)mg \sin \frac{1}{6}\pi = ma_T$ Tangential component is $4.9 \text{ ms}^{-2}$	M1 A1 A1 M1 A1 [5]	Equation involving initial KE, final KE and attempt at PE  Allow M1 for $\cos \frac{1}{6}\pi$ used instead of $\sin \frac{1}{6}\pi$ ; but M0 for $a_T = mg \sin \frac{1}{6}\pi$ Allow $\frac{1}{2}g$	

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Question		Answer	Marks	Guidance
2	(a) (ii)	$\frac{1}{2}mv^2 - \frac{1}{2}m(1.2)^2 = mg(0.8 - 0.8\cos\theta)$ $mg\cos\theta - R = \frac{mv^2}{0.8}$ <p>Leaves surface when <math>R = 0</math></p> $v^2 - 1.44 = 2 \times 9.8 \times 0.8 \left(1 - \frac{v^2}{7.84}\right)$ <p>Speed is <math>2.39 \text{ ms}^{-1}</math></p>	M1 M1 A1 M1 M1 A1 [6]	Equation involving initial KE, final KE and attempt at PE in general position Equation involving resolved component of weight and $v^2 / r$ $R$ may be omitted May be implied Obtaining equation in $v$ or $\theta$ <i>Dependent on previous MIMIMI</i> e.g. Implied by $mg\cos\theta = \frac{mv^2}{0.8}$ $\cos\theta = \frac{107}{147} = 0.728$ $\theta = 0.756 \text{ rad or } 43.3^\circ$
2	(b)	$T_R \sin\alpha + T_S \sin\beta = mg$ $0.8T_R + 0.28T_S = 0.9 \times 9.8 \quad (= 8.82)$ $T_R \cos\alpha + T_S \cos\beta = m \frac{v^2}{r}$ $0.6T_R + 0.96T_S = 0.9 \times \frac{5^2}{2.4} \quad (= 9.375)$ <p>Tension in string RQ is 9.737 N  Tension in string SQ is 3.68 N</p>	M1 A1 M1 A1 M1 A1 A1 [7]	Resolving vertically (three terms) Allow $\sin 53.1^\circ$ , etc Horizontal equation of motion Obtaining $T_R$ or $T_S$ <i>Dependent on previous MIMI</i>

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Question		Answer	Marks	Guidance	
3	(i)	Length of each string is 7.8 m $T = \frac{728}{6.4}(7.8 - 6.4)$ Tension is 159.25 N	B1  M1  A1 [3]	Using Hooke's law	Must use extension
3	(ii)	$2T \cos \theta = mg$ $2 \times 159.25 \times \frac{5}{13} = m \times 9.8$ $m = \frac{122.5}{9.8} = 12.5 \text{ kg}$	M1  A1  E1  [3]	Resolving vertically  FT  <i>Working must lead to 12.5 to 3 sf</i>	$\theta = \hat{XPM} = 67.4^\circ$
3	(iii)	New length of each string is 7.5 m $T = \frac{728}{6.4}(7.5 - 6.4) (= 125.125)$ $mg - 2T \cos \theta = ma$ $12.5 \times 9.8 - 2 \times 125.125 \times 0.28 = 12.5a$ Acceleration is $4.19 \text{ m s}^{-2}$ downwards (3 sf)	M1  A1  M1  A1  A1  [5]	Hooke's law with new extension  Vertical equation of motion (3 terms) FT for incorrect $T$  <i>Some indication of downwards required</i>	
3	(iv)	At maximum speed, acceleration is zero Acceleration is zero in equilibrium position	B1  [1]	Mention of zero acceleration	<i>Reference to <math>v^2 = \omega^2(A^2 - x^2)</math>, SHM, etc, will usually be B0</i>

Question		Answer	Marks	Guidance
3	(v)	Change of PE is $12.5 \times 9.8 \times 3$ ( $= 367.5$ ) Initial EE is $2 \times \frac{728 \times 0.8^2}{2 \times 6.4}$ ( $= 72.8$ ) Final EE is $2 \times \frac{728 \times 1.4^2}{2 \times 6.4}$ ( $= 222.95$ ) $\frac{1}{2}(12.5)v^2 - 367.5 + 222.95 = 72.8$ Maximum speed is $5.90 \text{ ms}^{-1}$ (3 sf)	B1 B1 B1 M1 A1 A1 <b>[6]</b>	Allow one string (36.4) Allow one string (111.475) Equation involving KE, PE and EE FT from any B0 above All signs must be correct CAO <i>All terms must be non-zero</i>
4	(a)	$V = \int_0^h \pi(y^{\frac{1}{4}})^2 dy$ $= \pi \left[ \frac{2}{3} y^{\frac{3}{2}} \right]_0^h \quad (= \frac{2}{3} \pi h^{\frac{3}{2}})$ $V \bar{y} = \int \pi x^2 y dy = \int_0^h \pi y^{\frac{1}{2}} y dy$ $= \pi \left[ \frac{2}{5} y^{\frac{5}{2}} \right]_0^h \quad (= \frac{2}{5} \pi h^{\frac{5}{2}})$ $\bar{y} = \frac{\frac{2}{5} \pi h^{\frac{5}{2}}}{\frac{2}{3} \pi h^{\frac{3}{2}}} = \frac{3}{5} h$	M1 A1 M1 A1 A1 <b>[5]</b>	For $\int \dots (y^{\frac{1}{4}})^2 dy$ For $\frac{2}{3} y^{\frac{3}{2}}$ For $\int x^2 y dy$ For $\frac{2}{5} y^{\frac{5}{2}}$

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Question		Answer	Marks	Guidance
4	(b) (i)	$A = \int_0^4 (x + \sqrt{x}) dx$ $= \left[ \frac{1}{2}x^2 + \frac{2}{3}x^{\frac{3}{2}} \right]_0^4 \quad (= \frac{40}{3})$ $A\bar{x} = \int xy dx = \int_0^4 x(x + \sqrt{x}) dx$ $= \left[ \frac{1}{3}x^3 + \frac{2}{5}x^{\frac{5}{2}} \right]_0^4 \quad (= \frac{512}{15})$ $\bar{x} = \frac{\frac{512}{15}}{\frac{40}{3}} = \frac{64}{25} = 2.56$ $A\bar{y} = \int \frac{1}{2}y^2 dx = \int_0^4 \frac{1}{2}(x + \sqrt{x})^2 dx$ $= \left[ \frac{1}{6}x^3 + \frac{2}{5}x^{\frac{5}{2}} + \frac{1}{4}x^2 \right]_0^4 \quad (= \frac{412}{15})$ $\bar{y} = \frac{\frac{412}{15}}{\frac{40}{3}} = \frac{103}{50} = 2.06$	M1 A1 M1 A1 E1 M1 A1A1 A1 [9]	For $\int (x + \sqrt{x}) dx$ For $\frac{1}{2}x^2 + \frac{2}{3}x^{\frac{3}{2}}$ For $\int xy dx$ For $\frac{1}{3}x^3 + \frac{2}{5}x^{\frac{5}{2}}$  For $\int \dots y^2 dx$ For $\frac{1}{6}x^3 + \frac{2}{5}x^{\frac{5}{2}} + \frac{1}{4}x^2$  Give A1 for two correct terms

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Question		Answer	Marks	Guidance
4	(b) (ii)	<p>Area of <math>B</math> is <math>24 - \frac{40}{3} = \frac{32}{3}</math></p> $\frac{32}{3} \begin{pmatrix} \bar{x} \\ \bar{y} \end{pmatrix} + \frac{40}{3} \begin{pmatrix} 2.56 \\ 2.06 \end{pmatrix} = 24 \begin{pmatrix} 2 \\ 3 \end{pmatrix}$ $\begin{pmatrix} \bar{x} \\ \bar{y} \end{pmatrix} = \begin{pmatrix} 1.3 \\ 4.175 \end{pmatrix}$	M1 M1 A1 A1	CM of composite body Correct strategy CAO FT requires $0 < \bar{y} < 6$ (One coordinate sufficient) $FT \text{ is } 6.75 - 1.25\bar{y}_A$ <i>No FT from wrong area</i>
	OR	$\int \frac{1}{4} (\sqrt{1+4y} - 1)^2 y \, dy \text{ or } \int x(6-x-\sqrt{x}) \, dx$ $\text{or } \int \frac{1}{32} (\sqrt{1+4y} - 1)^4 \, dy$ $\text{or } \int \frac{1}{2}(6-x-\sqrt{x})(6+x+\sqrt{x}) \, dx$ $\bar{x} = 1.3, \bar{y} = 4.175$	M1 M1 A1A1	For any one of these For one successful integration
		[4]		

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