



GCE

Mathematics (MEI)

Unit **4777**: Numerical Computation

Advanced GCE

Mark Scheme for June 2015

OCR (Oxford Cambridge and RSA) is a leading UK awarding body, providing a wide range of qualifications to meet the needs of candidates of all ages and abilities. OCR qualifications include AS/A Levels, Diplomas, GCSEs, Cambridge Nationals, Cambridge Technicals, Functional Skills, Key Skills, Entry Level qualifications, NVQs and vocational qualifications in areas such as IT, business, languages, teaching/training, administration and secretarial skills.

It is also responsible for developing new specifications to meet national requirements and the needs of students and teachers. OCR is a not-for-profit organisation; any surplus made is invested back into the establishment to help towards the development of qualifications and support, which keep pace with the changing needs of today's society.

This mark scheme is published as an aid to teachers and students, to indicate the requirements of the examination. It shows the basis on which marks were awarded by examiners. It does not indicate the details of the discussions which took place at an examiners' meeting before marking commenced.

All examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

Mark schemes should be read in conjunction with the published question papers and the report on the examination.

OCR will not enter into any discussion or correspondence in connection with this mark scheme.

© OCR 2015

1. Annotations

Annotation in scoris	Meaning
✓ and ✕	
BOD	Benefit of doubt
FT	Follow through
ISW	Ignore subsequent working
M0, M1	Method mark awarded 0, 1
A0, A1	Accuracy mark awarded 0, 1
B0, B1	Independent mark awarded 0, 1
SC	Special case
^	Omission sign
MR	Misread
Highlighting	
Other abbreviations in mark scheme	Meaning
E1	Mark for explaining
U1	Mark for correct units
G1	Mark for a correct feature on a graph
M1 dep*	Method mark dependent on a previous mark, indicated by *
cao	Correct answer only
oe	Or equivalent
rot	Rounded or truncated
soi	Seen or implied
www	Without wrong working

2. Subject-specific Marking Instructions for GCE Mathematics (MEI) Pure strand

- a. Annotations should be used whenever appropriate during your marking.

The A, M and B annotations must be used on your standardisation scripts for responses that are not awarded either 0 or full marks. It is vital that you annotate standardisation scripts fully to show how the marks have been awarded.

For subsequent marking you must make it clear how you have arrived at the mark you have awarded.

- b. An element of professional judgement is required in the marking of any written paper. Remember that the mark scheme is designed to assist in marking incorrect solutions. Correct *solutions* leading to correct answers are awarded full marks but work must not be judged on the answer alone, and answers that are given in the question, especially, must be validly obtained; key steps in the working must always be looked at and anything unfamiliar must be investigated thoroughly.

Correct but unfamiliar or unexpected methods are often signalled by a correct result following an *apparently* incorrect method. Such work must be carefully assessed. When a candidate adopts a method which does not correspond to the mark scheme, award marks according to the spirit of the basic scheme; if you are in any doubt whatsoever (especially if several marks or candidates are involved) you should contact your Team Leader.

- c. The following types of marks are available.

M

A suitable method has been selected and *applied* in a manner which shows that the method is essentially understood. Method marks are not usually lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, eg by substituting the relevant quantities into the formula. In some cases the nature of the errors allowed for the award of an M mark may be specified.

A

Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated Method mark is earned (or implied). Therefore M0 A1 cannot ever be awarded.

B

Mark for a correct result or statement independent of Method marks.

E

A given result is to be established or a result has to be explained. This usually requires more working or explanation than the establishment of an unknown result.

Unless otherwise indicated, marks once gained cannot subsequently be lost, eg wrong working following a correct form of answer is ignored. Sometimes this is reinforced in the mark scheme by the abbreviation isw. However, this would not apply to a case where a candidate passes through the correct answer as part of a wrong argument.

- d. When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. (The notation 'dep *' is used to indicate that a particular mark is dependent on an earlier, asterisked, mark in the scheme.) Of course, in practice it may happen that when a candidate has once gone wrong in a part of a question, the work from there on is worthless so that no more marks can sensibly be given. On the other hand, when two or more steps are successfully run together by the candidate, the earlier marks are implied and full credit must be given.
- e. The abbreviation ft implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A and B marks are given for correct work only — differences in notation are of course permitted. A (accuracy) marks are not given for answers obtained from incorrect working. When A or B marks are awarded for work at an intermediate stage of a solution, there may be various alternatives that are equally acceptable. In such cases, exactly what is acceptable will be detailed in the mark scheme rationale. If this is not the case please consult your Team Leader.

Sometimes the answer to one part of a question is used in a later part of the same question. In this case, A marks will often be 'follow through'. In such cases you must ensure that you refer back to the answer of the previous part question even if this is not shown within the image zone. You may find it easier to mark follow through questions candidate-by-candidate rather than question-by-question.

- f. Wrong or missing units in an answer should not lead to the loss of a mark unless the scheme specifically indicates otherwise. Candidates are expected to give numerical answers to an appropriate degree of accuracy, with 3 significant figures often being the norm. Small variations in the degree of accuracy to which an answer is given (e.g. 2 or 4 significant figures where 3 is expected) should not normally be penalised, while answers which are grossly over- or under-specified should normally result in the loss of a mark. The situation regarding any particular cases where the accuracy of the answer may be a marking issue should be detailed in the mark scheme rationale. If in doubt, contact your Team Leader.

g. Rules for replaced work

If a candidate attempts a question more than once, and indicates which attempt he/she wishes to be marked, then examiners should do as the candidate requests.

If there are two or more attempts at a question which have not been crossed out, examiners should mark what appears to be the last (complete) attempt and ignore the others.

NB Follow these maths-specific instructions rather than those in the assessor handbook.

h. For a *genuine* misreading (of numbers or symbols) which is such that the object and the difficulty of the question remain unaltered, mark according to the scheme but following through from the candidate's data. A penalty is then applied; 1 mark is generally appropriate, though this may differ for some units. This is achieved by withholding one A mark in the question.

Note that a miscopy of the candidate's own working is not a misread but an accuracy error.

Question			Answer	Marks	Guidance																			
1	(i)		$-1 < g'(\alpha) < 1$ Correct algebra to obtain given expression Derivative of RHS is $(1 - \lambda) + \lambda g'(x)$ Set this to zero at $x = \alpha$ to obtain $\lambda = 1 / (1 - g'(\alpha))$ In practice use $\lambda = 1 / (1 - g'(x_0))$	B1 M1 B1 B1 E1 [5]	Accept λ being re-set at each it'n																			
1	(ii)		<table><tr><td></td><td>x</td><td>2 tan x</td><td>1/(x - 1.5)</td></tr><tr><td>1.5 + 0.001</td><td>1.501</td><td>28.60826</td><td>< 1000</td></tr><tr><td>pi/2 - 0.001</td><td>1.569796</td><td>1999.999</td><td>> 14.3274</td></tr></table> E.g. <table><tr><td>1.525</td><td>1.520838</td><td>1.529145</td><td>1.512573</td><td>1.545655</td><td>1.479738</td></tr></table> Explain: oscillating with increasing amplitude (Or exhibit differences and ratios of differences)		x	2 tan x	1/(x - 1.5)	1.5 + 0.001	1.501	28.60826	< 1000	pi/2 - 0.001	1.569796	1999.999	> 14.3274	1.525	1.520838	1.529145	1.512573	1.545655	1.479738	M1A1 M1A1A1 E1 [6]	Other approaches possible	
	x	2 tan x	1/(x - 1.5)																					
1.5 + 0.001	1.501	28.60826	< 1000																					
pi/2 - 0.001	1.569796	1999.999	> 14.3274																					
1.525	1.520838	1.529145	1.512573	1.545655	1.479738																			
1	(iii)		E.g. <table><tr><td>1.525</td><td>1.522919</td><td>1.523955</td><td>1.523439</td><td>1.523696</td><td>1.523568</td></tr><tr><td>1.523632</td><td>1.523600</td><td>1.523616</td><td>1.523608</td><td>1.523612</td><td>1.523610</td></tr></table> Root is 1.52361 to 5 dp	1.525	1.522919	1.523955	1.523439	1.523696	1.523568	1.523632	1.523600	1.523616	1.523608	1.523612	1.523610	M1A1A1 A1 [4]								
1.525	1.522919	1.523955	1.523439	1.523696	1.523568																			
1.523632	1.523600	1.523616	1.523608	1.523612	1.523610																			
1	(iv)		$\lambda = 0.33$ (2dp) gives fastest convergence: <table><tr><td>1.525</td><td>1.523627</td><td>1.523611</td><td>1.523610</td><td>1.523610</td><td>1.523610</td></tr></table> Accept $\lambda = 0.34$: <table><tr><td>1.525</td><td>1.523585</td><td>1.523611</td><td>1.523610</td><td>1.523610</td><td>1.523610</td></tr></table>	1.525	1.523627	1.523611	1.523610	1.523610	1.523610	1.525	1.523585	1.523611	1.523610	1.523610	1.523610	M1A1 A1 [3]	Evidence of trials Answer							
1.525	1.523627	1.523611	1.523610	1.523610	1.523610																			
1.525	1.523585	1.523611	1.523610	1.523610	1.523610																			
1	(v)		<table><tr><td>k</td><td>root</td></tr><tr><td>0.5</td><td>1.547200</td></tr><tr><td>1</td><td>1.535406</td></tr><tr><td>1.5</td><td>1.528329</td></tr><tr><td>2</td><td>1.523610</td></tr><tr><td>2.5</td><td>1.520240</td></tr><tr><td>3</td><td>1.517712</td></tr></table>	k	root	0.5	1.547200	1	1.535406	1.5	1.528329	2	1.523610	2.5	1.520240	3	1.517712	M1 A1 A1 A1	Any method of solution is permitted 2 roots 4 roots 6 roots					
k	root																							
0.5	1.547200																							
1	1.535406																							
1.5	1.528329																							
2	1.523610																							
2.5	1.520240																							
3	1.517712																							

Question			Answer	Marks	Guidance																																																											
				G2 [6]																																																												
				[24]																																																												
2	(i)		$T_n - I = A_2 h^2 + A_4 h^4 + A_6 h^6 + \dots$ $T_{2n} - I = A_2 (h/2)^2 + A_4 (h/2)^4 + A_6 (h/2)^6 + \dots$ $4(T_{2n} - I) - (T_n - I) = b_4 h^4 + b_6 h^6 + \dots$ $4T_{2n} - T_n - 3I = b_4 h^4 + b_6 h^6 + \dots$ $(4T_{2n} - T_n)/3 - I = B_4 h^4 + B_6 h^6 + \dots$ $(T_n^* = (4T_{2n} - T_n)/3 \text{ has error of order } h^4 \text{ as given})$ $T_n^{**} = (16T_{2n}^* - T_n^*)/15 \text{ has error of order } h^6$	B1 B1 B1 B1 B1 B1 [6]																																																												
2	(ii)		<table border="1"> <thead> <tr> <th>h</th><th>x</th><th>f(x)</th><th>M</th><th>T</th><th>T*</th><th>T**</th></tr> </thead> <tbody> <tr> <td rowspan="3">0.5</td><td>1.5</td><td>2.063628</td><td></td><td></td><td></td><td></td></tr> <tr> <td>2</td><td>2.693273</td><td></td><td>1.189225</td><td></td><td></td></tr> <tr> <td>1.75</td><td>2.362378</td><td>1.181189</td><td>1.185207</td><td>1.183868</td><td></td></tr> <tr> <td rowspan="2">0.25</td><td>1.625</td><td>2.209413</td><td></td><td></td><td></td><td></td></tr> <tr> <td>1.875</td><td>2.523383</td><td>1.183199</td><td>1.184203</td><td>1.183868</td><td>1.183869</td></tr> <tr> <td rowspan="3">0.125</td><td>1.5625</td><td>2.135678</td><td></td><td></td><td></td><td></td></tr> <tr> <td>1.6875</td><td>2.284944</td><td></td><td></td><td></td><td></td></tr> <tr> <td>1.8125</td><td>2.441823</td><td></td><td></td><td></td><td></td></tr> </tbody> </table>	h	x	f(x)	M	T	T*	T**	0.5	1.5	2.063628					2	2.693273		1.189225			1.75	2.362378	1.181189	1.185207	1.183868		0.25	1.625	2.209413					1.875	2.523383	1.183199	1.184203	1.183868	1.183869	0.125	1.5625	2.135678					1.6875	2.284944					1.8125	2.441823					M1A1 M1A1 M1A1	T values T* values T** values	
h	x	f(x)	M	T	T*	T**																																																										
0.5	1.5	2.063628																																																														
	2	2.693273		1.189225																																																												
	1.75	2.362378	1.181189	1.185207	1.183868																																																											
0.25	1.625	2.209413																																																														
	1.875	2.523383	1.183199	1.184203	1.183868	1.183869																																																										
0.125	1.5625	2.135678																																																														
	1.6875	2.284944																																																														
	1.8125	2.441823																																																														

Question			Answer				Marks	Guidance																				
			1.9375	2.607166	1.183701	1.183952	1.183869	1.183869	Iterating enough																			
		0.0625	1.53125	2.099449																								
			1.59375	2.172328																								
			1.65625	2.246947																								
			1.71875	2.323416																								
			1.78125	2.401842																								
			1.84375	2.482332																								
			1.90625	2.564990																								
			1.96875	2.649922	1.183827	1.183889	1.183869	1.183869																				
		Integral is 1.183869 to 6 dp						A1	Correct answer																			
		<table><tr><td>T</td><td>diffs</td><td>ratios</td></tr><tr><td>1.189225</td><td></td><td></td></tr><tr><td>1.185207</td><td>-0.0040182</td><td></td></tr><tr><td>1.184203</td><td>-0.0010039</td><td>0.249846</td></tr><tr><td>1.183952</td><td>-0.0002509</td><td>0.249959</td></tr><tr><td>1.183889</td><td>-6.273E-05</td><td>0.249989</td></tr></table>						T		diffs	ratios	1.189225			1.185207	-0.0040182		1.184203	-0.0010039	0.249846	1.183952	-0.0002509	0.249959	1.183889	-6.273E-05	0.249989	B1	
T	diffs	ratios																										
1.189225																												
1.185207	-0.0040182																											
1.184203	-0.0010039	0.249846																										
1.183952	-0.0002509	0.249959																										
1.183889	-6.273E-05	0.249989																										
		<table><tr><td>T*</td><td>diffs</td><td>Ratios</td></tr><tr><td>1.183868</td><td></td><td></td></tr><tr><td>1.183868</td><td>8.2563E-07</td><td></td></tr><tr><td>1.183869</td><td>5.5446E-08</td><td>0.067156</td></tr><tr><td>1.183869</td><td>3.5297E-09</td><td>0.063661</td></tr></table>						T*		diffs	Ratios	1.183868			1.183868	8.2563E-07		1.183869	5.5446E-08	0.067156	1.183869	3.5297E-09	0.063661	B1				
T*	diffs	Ratios																										
1.183868																												
1.183868	8.2563E-07																											
1.183869	5.5446E-08	0.067156																										
1.183869	3.5297E-09	0.063661																										
		<table><tr><td>T**</td><td>diffs</td><td>Ratios</td></tr><tr><td>1.183869</td><td></td><td></td></tr><tr><td>1.183869</td><td>4.1002E-09</td><td></td></tr><tr><td>1.183869</td><td>6.8675E-11</td><td>0.016749</td></tr></table>						T**	diffs	Ratios	1.183869			1.183869	4.1002E-09		1.183869	6.8675E-11	0.016749	B1								
T**	diffs	Ratios																										
1.183869																												
1.183869	4.1002E-09																											
1.183869	6.8675E-11	0.016749																										
		Ratios 1/4, 1/16, 1/64 as theory indicates						E1																				

Question			Answer	Marks	Guidance																			
2	(iii)		With $a = 0$ the values obtained and their differences are:	[12]																				
			<table><tr><td>T</td><td>diffs</td><td>Ratios</td></tr><tr><td>2.693273</td><td></td><td></td></tr><tr><td>2.879739</td><td>0.18646558</td><td></td></tr><tr><td>2.982122</td><td>0.10238307</td><td>0.549072</td></tr><tr><td>3.027443</td><td>0.04532125</td><td>0.442664</td></tr><tr><td>3.045738</td><td>0.018295</td><td>0.403674</td></tr></table>	T			diffs	Ratios	2.693273			2.879739	0.18646558		2.982122	0.10238307	0.549072	3.027443	0.04532125	0.442664	3.045738	0.018295	0.403674	B1
			T	diffs			Ratios																	
			2.693273																					
			2.879739	0.18646558																				
			2.982122	0.10238307			0.549072																	
			3.027443	0.04532125			0.442664																	
			3.045738	0.018295			0.403674																	
			<table><tr><td>T*</td><td>diffs</td><td>Ratios</td></tr><tr><td>2.941894</td><td></td><td></td></tr><tr><td>3.016250</td><td>0.07435557</td><td></td></tr><tr><td>3.042550</td><td>0.02630064</td><td>0.353714</td></tr><tr><td>3.051836</td><td>0.00928625</td><td>0.353081</td></tr></table>	T*			diffs	Ratios	2.941894			3.016250	0.07435557		3.042550	0.02630064	0.353714	3.051836	0.00928625	0.353081	B1			
			T*	diffs			Ratios																	
2.941894																								
3.016250	0.07435557																							
3.042550	0.02630064	0.353714																						
3.051836	0.00928625	0.353081																						
<table><tr><td>T**</td><td>diffs</td><td>Ratios</td></tr><tr><td>3.021207</td><td></td><td></td></tr><tr><td>3.044304</td><td>0.02309698</td><td></td></tr><tr><td>3.052456</td><td>0.00815195</td><td>0.352944</td></tr></table>	T**	diffs	Ratios	3.021207			3.044304	0.02309698		3.052456	0.00815195	0.352944	B1											
T**	diffs	Ratios																						
3.021207																								
3.044304	0.02309698																							
3.052456	0.00815195	0.352944																						
Show that the gradient of the curve is infinite at $x = 0$			M1A1																					
Integration methods based on fitting polynomials (T, T*=S etc.)			E1																					
do not approximate infinite gradients well.			[6]																					
			[24]																					

Question			Answer	Marks	Guidance																																										
3	(i)		Use central difference formulae for first and second derivatives. Correct algebra to first given result. Use central difference formula and initial condition on y' to obtain a relationship between y_1 and y_{-1} Eliminate y_{-1} to obtain given expression for y_1	M1A1 M1 A1 M1A1 [6]	Award A marks for convincing algebra only																																										
3	(ii)		Implement the solution Obtain values and look at differences: <table border="1"><thead><tr><th>h</th><th colspan="3">$y(10)$</th></tr></thead><tbody><tr><td>0.1</td><td>11.188803</td><td></td><td></td></tr><tr><td>0.05</td><td>11.179093</td><td>-0.009710</td><td></td></tr><tr><td>0.025</td><td>11.176665</td><td>-0.002428</td><td>0.250090</td></tr><tr><td>0.0125</td><td>11.176058</td><td>-0.000607</td><td>0.250023</td></tr></tbody></table> Method clearly second order (0.25)	h	$y(10)$			0.1	11.188803			0.05	11.179093	-0.009710		0.025	11.176665	-0.002428	0.250090	0.0125	11.176058	-0.000607	0.250023	Set up M3 Values A1,1,1,1 Differences M1A1 Explanation E1	<table border="1"><thead><tr><th>h</th><th>x</th><th>y</th></tr></thead><tbody><tr><td>0.1</td><td>1</td><td>1</td></tr><tr><td>0.1</td><td>1.1</td><td>1.0575</td></tr><tr><td>0.1</td><td>1.2</td><td>1.128698</td></tr><tr><td>0.1</td><td>1.3</td><td>1.212161</td></tr><tr><td>0.1</td><td>1.4</td><td>1.306323</td></tr><tr><td>0.1</td><td>1.5</td><td>1.409503</td></tr></tbody></table>	h	x	y	0.1	1	1	0.1	1.1	1.0575	0.1	1.2	1.128698	0.1	1.3	1.212161	0.1	1.4	1.306323	0.1	1.5	1.409503	
h	$y(10)$																																														
0.1	11.188803																																														
0.05	11.179093	-0.009710																																													
0.025	11.176665	-0.002428	0.250090																																												
0.0125	11.176058	-0.000607	0.250023																																												
h	x	y																																													
0.1	1	1																																													
0.1	1.1	1.0575																																													
0.1	1.2	1.128698																																													
0.1	1.3	1.212161																																													
0.1	1.4	1.306323																																													
0.1	1.5	1.409503																																													
				[10]																																											
3	(iii)		New values and differences: <table border="1"><thead><tr><th>h</th><th colspan="3">$y(10)$</th></tr></thead><tbody><tr><td>0.1</td><td>10.973628</td><td></td><td></td></tr><tr><td>0.05</td><td>11.074228</td><td>0.100600</td><td></td></tr><tr><td>0.025</td><td>11.124915</td><td>0.050687</td><td>0.503851</td></tr><tr><td>0.0125</td><td>11.150354</td><td>0.025439</td><td>0.501875</td></tr></tbody></table> Method now clearly first order (0.5)	h	$y(10)$			0.1	10.973628			0.05	11.074228	0.100600		0.025	11.124915	0.050687	0.503851	0.0125	11.150354	0.025439	0.501875	Modify M1 Values A1,1,1,1 Differences B1 Identify new order A1E1	<table border="1"><thead><tr><th>h</th><th>x</th><th>y</th></tr></thead><tbody><tr><td>0.1</td><td>1</td><td>1</td></tr><tr><td>0.1</td><td>1.1</td><td>1.05</td></tr><tr><td>0.1</td><td>1.2</td><td>1.114417</td></tr><tr><td>0.1</td><td>1.3</td><td>1.191774</td></tr><tr><td>0.1</td><td>1.4</td><td>1.280471</td></tr><tr><td>0.1</td><td>1.5</td><td>1.3788</td></tr></tbody></table>	h	x	y	0.1	1	1	0.1	1.1	1.05	0.1	1.2	1.114417	0.1	1.3	1.191774	0.1	1.4	1.280471	0.1	1.5	1.3788	
h	$y(10)$																																														
0.1	10.973628																																														
0.05	11.074228	0.100600																																													
0.025	11.124915	0.050687	0.503851																																												
0.0125	11.150354	0.025439	0.501875																																												
h	x	y																																													
0.1	1	1																																													
0.1	1.1	1.05																																													
0.1	1.2	1.114417																																													
0.1	1.3	1.191774																																													
0.1	1.4	1.280471																																													
0.1	1.5	1.3788																																													
				[8]																																											
				[24]																																											

Question			Answer	Marks	Guidance																															
4	(i)		Gaussian elimination, forward pass, pivots in <i>bold italic</i>	Set up M1 Pivoting M1 First step M1A1 Second B1 Third B1																																
			<table><tr><td>5</td><td>3</td><td>-2</td><td>7</td><td>1</td></tr><tr><td><i>11</i></td><td>-6</td><td>-5</td><td>2</td><td>2</td></tr><tr><td>-4</td><td>3</td><td>3</td><td>4</td><td>2</td></tr><tr><td>6</td><td>2</td><td>-4</td><td>5</td><td>2</td></tr></table>				5	3	-2	7	1	<i>11</i>	-6	-5	2	2	-4	3	3	4	2	6	2	-4	5	2										
			5				3	-2	7	1																										
			<i>11</i>				-6	-5	2	2																										
			-4				3	3	4	2																										
			6				2	-4	5	2																										
			<table><tr><td></td><td><i>5.727273</i></td><td>0.272727</td><td>6.0909091</td><td>0.09090909</td></tr><tr><td></td><td>0.818182</td><td>1.181818</td><td>4.7272727</td><td>2.72727273</td></tr><tr><td></td><td>5.272727</td><td>-1.27273</td><td>3.9090909</td><td>0.90909091</td></tr><tr><td></td><td></td><td>1.142857</td><td>3.8571429</td><td>2.71428571</td></tr><tr><td></td><td></td><td><i>-1.52381</i></td><td>-1.698413</td><td>0.82539683</td></tr><tr><td></td><td></td><td></td><td><i>2.5833333</i></td><td>3.33333333</td></tr></table>					<i>5.727273</i>	0.272727	6.0909091	0.09090909		0.818182	1.181818	4.7272727	2.72727273		5.272727	-1.27273	3.9090909	0.90909091			1.142857	3.8571429	2.71428571			<i>-1.52381</i>	-1.698413	0.82539683				<i>2.5833333</i>	3.33333333
							<i>5.727273</i>	0.272727	6.0909091	0.09090909																										
							0.818182	1.181818	4.7272727	2.72727273																										
							5.272727	-1.27273	3.9090909	0.90909091																										
		1.142857	3.8571429	2.71428571																																
		<i>-1.52381</i>	-1.698413	0.82539683																																
			<i>2.5833333</i>	3.33333333																																
Solutions, obtained from pivotal rows: -1.641129 -1.262097 -1.979839 1.290323 Evidence of substituting solutions back into equations to check. Partial pivoting: selecting the element of largest magnitude in the left most column to eliminate other elements in that column. The pivot acts as a divisor in the calculations; using the largest pivot reduces magnitudes of errors in other terms.																																				
M1 A1 A1 A1 A1 B1 E2 E2																																				
Award E1 for partial understanding Award E1 for partial understanding																																				
[16]																																				
4	(ii)		Magnitude of determinant is product of pivotal elements: -248 Correct sign because there were two pivots not in first row: (-1) ²	M1A1 E1																																
				[3]																																
4	(iii)		Replace RHS with the correct four unit vectors. Obtain solutions and assemble to give the inverse matrix: <table><tr><td>0.754032</td><td>-0.076613</td><td>-0.479839</td><td>-0.641129</td></tr><tr><td>0.471774</td><td>-0.213710</td><td>-0.391129</td><td>-0.262097</td></tr><tr><td>0.963710</td><td>-0.060484</td><td>-0.431452</td><td>-0.979839</td></tr><tr><td>-0.322581</td><td>0.129032</td><td>0.387097</td><td>0.290323</td></tr></table>	0.754032	-0.076613	-0.479839	-0.641129	0.471774	-0.213710	-0.391129	-0.262097	0.963710	-0.060484	-0.431452	-0.979839	-0.322581	0.129032	0.387097	0.290323	M1 Each column A1,1,1,1																
0.754032	-0.076613	-0.479839	-0.641129																																	
0.471774	-0.213710	-0.391129	-0.262097																																	
0.963710	-0.060484	-0.431452	-0.979839																																	
-0.322581	0.129032	0.387097	0.290323																																	
				[5]																																
				[24]																																

OCR (Oxford Cambridge and RSA Examinations)
1 Hills Road
Cambridge
CB1 2EU

OCR Customer Contact Centre

Education and Learning

Telephone: 01223 553998

Facsimile: 01223 552627

Email: general.qualifications@ocr.org.uk

www.ocr.org.uk

For staff training purposes and as part of our quality assurance programme your call may be recorded or monitored

Oxford Cambridge and RSA Examinations
is a Company Limited by Guarantee
Registered in England
Registered Office; 1 Hills Road, Cambridge, CB1 2EU
Registered Company Number: 3484466
OCR is an exempt Charity

OCR (Oxford Cambridge and RSA Examinations)
Head office
Telephone: 01223 552552
Facsimile: 01223 552553

© OCR 2015

