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A2 GCE

4754/01B

MATHEMATICS (MEI)

**Applications of Advanced
Mathematics (C4)**

Paper B: Comprehension

INSERT

FRIDAY 24 JUNE 2016 – Morning

**DURATION: Up to 1 hour
plus your additional time allowance**

MODIFIED ENLARGED

INFORMATION FOR CANDIDATES

This Insert contains the text for use with the questions.

The diagrams are provided in a separate booklet.

Any blank pages are indicated.

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PHOTOMONTAGES

INTRODUCTION

When a new building or structure is proposed, planning permission has to be obtained from the authorities. It is common practice to present an image of what the new building or structure is expected to look like. The image is often an artist's impression but it may also be a photomontage. 5

Photomontages are commonly used to support applications to develop wind farms and this context is used in this article. Electricity at a wind farm is generated by wind turbines. A wind turbine is illustrated in Fig. 1 in the diagram booklet. This diagram also explains the meanings of the terms used throughout the article. 10 15

A photomontage is based on a photograph taken from a particular place. The photograph shows the background before any building work has started. An image of the proposed structure is then superimposed on this. The image may be a photograph or a computer drawing and must be in the right place and to the right scale. Fig. 2 in the diagram booklet is typical of many photomontages that have been used for planning applications. 20

The type of wind turbine in Fig. 2 has blade tip height 99.5 m and hub height 64.5 m. So the blades are 35 m long. 25

THE IMPRESSION GIVEN BY PHOTOMONTAGES

The purpose of a photomontage is to provide an accurate representation of how the proposed development would appear in reality. A photomontage in which the development is the wrong size, either too large or too small, is misleading. 30

After a wind farm has been built, local people have sometimes complained that the turbines looked larger than they did in the photomontages. This article looks at three possible explanations. 35

THE ANGLE OF ELEVATION

The turbine in Fig. 2 has a blade tip height of 99.5 metres and the photomontage shows the view from a place 548 metres away. So it is possible to work out the angle of elevation of the highest point. This is the angle α in Fig. 3 in the diagram booklet. To simplify the calculations it is assumed that the observer's eye is at the same level as the base of the turbine. 40 45

The information with the photomontage also gives the recommended viewing distance as 51.4 centimetres; this is about an arm's length. So you might expect that, seen from this distance, the turbine in the photomontage should have the same angle of elevation of α if it is to appear the right size to a viewer. This is illustrated in Fig. 4 in the diagram booklet. 50 55

From the triangles in Figs 3 and 4, you can deduce that the height of the turbine in the photomontage should be 9.3 cm, to 2 significant figures. However, if you measure it in Fig. 2, you obtain the much smaller figure of about 5.9 cm. How can this discrepancy be explained?

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SEEING ONLY PART OF A WIND TURBINE

One possible explanation is that not all of the turbine is being seen.

Wind turbines are often positioned near the tops of hills where the wind is strongest, so you might expect the whole turbine to be visible from nearby. However, that is often not the case. The view may be obstructed as illustrated in Fig. 5 in the diagram booklet. In this case, an observer at point A would only ever see the tips of the blades.

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So a photomontage has to take account of the lie of the land between the observer and the wind turbine. The choice of the observer's position can have a substantial effect on the appearance of the wind turbine. Might this have happened in Fig. 2?

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One of the blades in Fig. 2 is upright; its length on the photomontage is about 2.35 cm. As the dimensions of the turbine are known (given on lines 26 and 27), it is possible to work out that the height of the full turbine would be about 6.7 cm on the photomontage. However, as the height seen is only 5.9 cm, this means that about 0.8 cm of the tower must be hidden from view in the photomontage. So someone at the point of observation would not see the bottom 12 m of the turbine.

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So the obscuring effect of the land explains some of the discrepancy. However, even though the revised figure of 6.7 cm, is closer than 5.9 cm, it is still much less than the 9.3 cm that is needed for the angle of elevation to be correct. 90

So other possible causes need to be considered.

PRINTED SIZE

Another possible explanation relates to the size of paper on which the photomontage is printed. 95

All of the pages that this article are printed on are A4 size; they are 210 mm wide and 297 mm high, to the nearest mm. When two A4 sheets are laid side by side, the resulting size is 420 mm \times 297 mm. This is A3 size and is illustrated in Fig. 6 in the diagram booklet. 100

In the same way, two A3 sheets laid side by side make an A2 sheet, and so on up to A0. The area of an A0 sheet is exactly 1 m². For all the A sizes, the ratio *short side: long side* is 1 : $\sqrt{2}$. Because the ratio is the same, every A-sized sheet of paper is similar to every other sheet. 105

It follows that a photomontage printed on an A3 sheet would be an exact enlargement of one printed on an A4 sheet, with a scale factor of $\sqrt{2}$ or 1.41, to 3 significant figures. Thus if the photomontage in Fig. 2 were printed on A3 paper, the height of the turbine would be 6.7 \times 1.41 or about 9.45 cm. Given the approximate nature of the measurements, this is very close to 9.3 cm. 110 115

So an explanation of the discrepancy is that the photomontage should have been printed on an A3 sheet, rather than on A4. However, it is not clear that this is actually the right explanation.

It is common practice to give the viewing distance at the bottom of a photomontage, as in Fig. 2, but not the recommended printing size. Many people view photomontages on their computers and print them out. A standard printer produces an A4 image and this is also about the size that it appears on many computer monitors. So those people who view photomontages on-screen or from their print-outs would expect the turbines to be smaller than they will appear when they are actually constructed.

However, complaints have also come from some people who only saw the photomontages at public meetings where they were presented at A3 size. These people have also said that the turbines looked too small in the photomontages they were shown.

VISUALISATION

There are professional people, such as architects and artists, whose expertise includes 'visualisation'. They say that arguments about the printed size and viewing distance miss the point, which is that it does not matter whether the size of the photomontage is large or small, as your brain will convert it into an image inside your head. What matters is whether the image in your head from looking at a photomontage is the same as the image from looking at the real thing.

Fig. 7 and Fig. 8 in the diagram booklet show two views from the same place. Fig. 8 is a rectangular window that has been taken from within Fig. 7 and then enlarged to the same size. It follows that 150

Fig. 8 has a narrower field of view than Fig. 7

objects look larger in Fig. 8 than in Fig. 7.

The key question is which of these two views is the better representation of what a typical person would actually see from that place. 155

Different fields of view are obtained when photographs are taken with lenses of different focal length. Fig. 9 in the diagram booklet illustrates the relationship between the focal length and the included angle in the field of view of the photograph. A shorter focal length would give a larger included angle and so a wider field of view. 160

So photographs taken using a camera with a longer focal length lens have a narrower field of view, resulting in distant objects looking larger. 165

The question of what is the best focal length was investigated in a study by Stirling University for the Highland Council in 2011 to 2012. Participants were taken to places near existing wind farms and were given 7 photomontages. These used photographs that had been taken with lenses with a range of focal lengths from 50 mm to 110 mm. They were asked to select the one that best represented what they saw. 170

In total 362 people took part and their responses are given in Table 10. 175

TABLE 10

Focal length (mm)	50	60	70	80	90	100	110
Number of preferences	16	50	85	85	72	37	17

As a result of the study, it was recommended that a focal length of 75 mm should be used. This contrasts with the previous common practice of using a focal length of 50 mm.

Fig. 8 is the picture that would have been obtained using a 75 mm lens, which is consistent with this recommendation. If this is enlarged to the same size as Fig. 2, and allowance is made for the part of the tower that is obscured, the height of the turbine would be close to 9.3 cm. So the angle of elevation when an A4 print-out was viewed at arm's length would be about right. 180 185

The wide spread of the data in Table 10 indicates that people see things differently. However, for a very large majority of viewers (over 95% of participants in the study) a photomontage based on a photograph taken with a 50 mm lens will under-represent the height of a wind turbine. 190

Consequently, of the three explanations considered in this article, the use of an unsuitable camera lens has been accepted as the most plausible. 195

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