



GCE
Mathematics (MEI)

Unit **4772**: Decision Mathematics 2

Advanced GCE

Mark Scheme for June 2017

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All examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

Mark schemes should be read in conjunction with the published question papers and the report on the examination.

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Annotations and abbreviations

Annotation in score	Meaning
✓ and ✗	
BOD	Benefit of doubt
FT	Follow through
ISW	Ignore subsequent working
M0, M1	Method mark awarded 0, 1
A0, A1	Accuracy mark awarded 0, 1
B0, B1	Independent mark awarded 0, 1
SC	Special case
^	Omission sign
MR	Misread
Highlighting	
Other abbreviations in mark scheme	Meaning
E1	Mark for explaining
U1	Mark for correct units
G1	Mark for a correct feature on a graph
M1 dep*	Method mark dependent on a previous mark, indicated by *
cao	Correct answer only
oe	Or equivalent
rot	Rounded or truncated
soi	Seen or implied
www	Without wrong working

Question		Answer												Marks	Guidance																																																																																																																							
1	(a)	<p>e.g. A workable definition of a liar is one who does not always tell the truth.</p> <p>If Epimenides was telling the truth, then all Cretans were liars (which is unlikely since there were perhaps some 200000 inhabitants in Crete in 400 BC). This does not contradict the implication that he is a liar, given the above.</p> <p>If Epimenides was lying then not all Cretans are liars, which is also not a contradiction.</p> <p>(Note the liar paradox, “I am lying”, refers to one statement only.)</p>												B1	Sensible consideration of meaning																																																																																																																							
	(b)	<p>If Epimenides was telling the truth, then all Cretans were liars (which is unlikely since there were perhaps some 200000 inhabitants in Crete in 400 BC). This does not contradict the implication that he is a liar, given the above.</p> <p>If Epimenides was lying then not all Cretans are liars, which is also not a contradiction.</p> <p>(Note the liar paradox, “I am lying”, refers to one statement only.)</p> <table border="1" data-bbox="336 587 1325 1032"> <tr> <td>a</td><td>\wedge</td><td>(b)</td><td>\vee</td><td>c)</td><td></td><td>(a)</td><td>\wedge</td><td>b)</td><td>\vee</td><td>(a)</td><td>\wedge</td><td>c)</td></tr> <tr> <td>0</td><td>0</td><td>0</td><td>0</td><td>0</td><td></td><td>0</td><td>0</td><td>0</td><td>0</td><td>0</td><td>0</td><td>0</td></tr> <tr> <td>0</td><td>0</td><td>0</td><td>1</td><td>1</td><td></td><td>0</td><td>0</td><td>0</td><td>0</td><td>0</td><td>0</td><td>1</td></tr> <tr> <td>0</td><td>0</td><td>1</td><td>1</td><td>0</td><td></td><td>0</td><td>0</td><td>1</td><td>0</td><td>0</td><td>0</td><td>0</td></tr> <tr> <td>0</td><td>0</td><td>1</td><td>1</td><td>1</td><td></td><td>0</td><td>0</td><td>1</td><td>0</td><td>0</td><td>0</td><td>1</td></tr> <tr> <td>1</td><td>0</td><td>0</td><td>0</td><td>0</td><td></td><td>1</td><td>0</td><td>0</td><td>0</td><td>1</td><td>0</td><td>0</td></tr> <tr> <td>1</td><td>1</td><td>0</td><td>1</td><td>1</td><td></td><td>1</td><td>0</td><td>0</td><td>1</td><td>1</td><td>1</td><td>1</td></tr> <tr> <td>1</td><td>1</td><td>1</td><td>1</td><td>0</td><td></td><td>1</td><td>1</td><td>1</td><td>1</td><td>1</td><td>0</td><td>0</td></tr> <tr> <td>1</td><td>1</td><td>1</td><td>1</td><td>1</td><td></td><td>1</td><td>1</td><td>1</td><td>1</td><td>1</td><td>1</td><td>1</td></tr> </table>														a	\wedge	(b)	\vee	c)		(a)	\wedge	b)	\vee	(a)	\wedge	c)	0	0	0	0	0		0	0	0	0	0	0	0	0	0	0	1	1		0	0	0	0	0	0	1	0	0	1	1	0		0	0	1	0	0	0	0	0	0	1	1	1		0	0	1	0	0	0	1	1	0	0	0	0		1	0	0	0	1	0	0	1	1	0	1	1		1	0	0	1	1	1	1	1	1	1	1	0		1	1	1	1	1	0	0	1	1	1	1	1		1	1	1	1	1	1	1	M1	8 rows
a	\wedge	(b)	\vee	c)		(a)	\wedge	b)	\vee	(a)	\wedge	c)																																																																																																																										
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Question		Answer	Marks	Guidance
2	(i)& (ii)	<p>Travel with the charter airline</p>	M1 M1 A1 A1 M1 A1 M1 A1 M1 A1 M1 A1 B1 B1	decision node at first branch chance nodes at second branches 3 terminal nodes twice 4 terminal nodes once one cost OK all costs OK one “no delay” prob OK all probs OK one chance computation OK all chance computations OK £333 quoted or in decision box decision

	(iii)	Utilities are 18.26, 18.11, 18.24 respectively, so travel with the budget airline. Common errors ... 12.38, 15.70 and 14.57 ... allowed on ft. Common errors ... 13.53, 9.86, 11.49 ... allowed on ft	M1 A1	one of 18.11 or 18.24 all correct, plus decision
	(iv)	EMV = £333 - £313 = £20 (Computation of £313 uses probabilities of 0.87, 0.1 and 0.03) Common error ... budget becomes £233. for B1 only.	B1 B1	computation of £313 ✓ subtraction from £333 cao

Question		Answer	Marks	Guidance
3	(a) (i)	10 (16 if not exploiting symmetry) (6 or 12 if no diagonal)	B1 (B1) (0)	but follow subsequently
	(ii)	50	B1	or 80 or 30 or 60 from above
	(iii)	$(3+3) + (2+2) + (1+1) = 12$	M1A1	$(3+3)$ or $(2+2)$ or $(1+1)$ M1
	(iv)	$12 + 6 + 2 = 20$	M1A1	12 or 6 seen within three parts for M1
	(b) (i)	Min connector has length $18 + 22 + 23 + 29 = 92$ Add back in 27 and 31 giving an lower bound of 150	M1A1 M1A1	M1 for 4 arcs M1 for adding 2 A1 \vee
	(ii)	A 27 C 18 E 29 D 22 B 33 F 31 A ... 160 B 22 D 23 F 31 A 27 C 18 E 45 B ... 166 C 18 E 29 D 22 B 32 A 31 F ... stall	M1 B1 A1	160 and 166 stall ACEDBFA given or indicated
	(iii)	Odd vertices are B, C, D and F. Pairings ... BC – 38 and DF – 23 ... 61 BD – 22 and CF – 58 ... 80 BF – 33 and CD – 47 ... 80 So repeat BC and DF, giving for instance ... A 32 B 38 C 38 B 22 D 29 E 18 C 27 A 41 E 45 B 33 F 23 D 23 F 31 A ... 400	M1 A1 A1 A1 M1 A1 A1	

Question		Answer										Marks	Guidance																																																												
4	(i)	the proportions of each ingredient										B1																																																													
	(ii)	<table border="1"> <thead> <tr> <th>P</th><th>p1</th><th>p2</th><th>p3</th><th>p4</th><th>s1</th><th>s2</th><th>s3</th><th>s4</th><th>RHS</th></tr> </thead> <tbody> <tr><td>1</td><td>-1</td><td>-1</td><td>-1</td><td>-1</td><td>0</td><td>0</td><td>0</td><td>0</td><td>0</td></tr> <tr><td>0</td><td>1</td><td>1</td><td>1</td><td>1</td><td>1</td><td>0</td><td>0</td><td>0</td><td>1</td></tr> <tr><td>0</td><td>2</td><td>5</td><td>30</td><td>100</td><td>0</td><td>1</td><td>0</td><td>0</td><td>26</td></tr> <tr><td>0</td><td>0.05</td><td>1</td><td>2</td><td>0</td><td>0</td><td>0</td><td>1</td><td>0</td><td>1</td></tr> <tr><td>0</td><td>3.5</td><td>2</td><td>0</td><td>0</td><td>0</td><td>0</td><td>0</td><td>1</td><td>2.5</td></tr> </tbody> </table>										P	p1	p2	p3	p4	s1	s2	s3	s4	RHS	1	-1	-1	-1	-1	0	0	0	0	0	0	1	1	1	1	1	0	0	0	1	0	2	5	30	100	0	1	0	0	26	0	0.05	1	2	0	0	0	1	0	1	0	3.5	2	0	0	0	0	0	1	2.5	B1 B4	objective constraints
P	p1	p2	p3	p4	s1	s2	s3	s4	RHS																																																																
1	-1	-1	-1	-1	0	0	0	0	0																																																																
0	1	1	1	1	1	0	0	0	1																																																																
0	2	5	30	100	0	1	0	0	26																																																																
0	0.05	1	2	0	0	0	1	0	1																																																																
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P	p1	p2	p3	p4	s1	s2	s3	s4	RHS																																																																
1	0	$-\frac{3}{7}$	-1	-1	0	0	0	$\frac{5}{7}$	$\frac{5}{7}$																																																																
0	0	$\frac{3}{7}$	1	1	1	0	0	$-\frac{2}{7}$	$\frac{2}{7}$																																																																
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0	1	$\frac{4}{7}$	0	0	0	0	0	$\frac{5}{7}$	$\frac{5}{7}$																																																																
	(iv)	(4, 0.683333, 2.5) and (26, 1, 1.4175)										B1 B1	mark 26.01 and 1.00025 as correct																																																												

(v)		Tableau																		
		A	P	p1	p2	p3	p4	s1	s2	s3	s4	s5	s6	s7	s8	a1	a2	a3	a4	RHS
		1	0	1	1	1	1	0	0	0	0	-1	-1	-1	-1	0	0	0	0	0.85
		0	1	-1	-1	-1	-1	0	0	0	0	0	0	0	0	0	0	0	0	0
		0	0	1	1	1	1	1	0	0	0	0	0	0	0	0	0	0	0	1
		0	0	2	5	30	100	0	1	0	0	0	0	0	0	0	0	0	0	26
		0	0	0.05	1	2	0	0	0	1	0	0	0	0	0	0	0	0	0	1
		0	0	3.5	2	0	0	0	0	0	1	0	0	0	0	0	0	0	0	2.5
		0	0	1	0	0	0	0	0	0	0	-1	0	0	0	1	0	0	0	0.4
		0	0	0	1	0	0	0	0	0	0	0	-1	0	0	0	1	0	0	0.3
		0	0	0	0	1	0	0	0	0	0	0	0	-1	0	0	0	1	0	0.1
		0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	1	0.05
	(vi)	Proportions as given. Concentrations are (25.3, 0.52, 2).																		B1

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