



GCE

Mathematics (MEI)

Unit **4773**: Decision Mathematics Computation

Advanced GCE

Mark Scheme for June 2018

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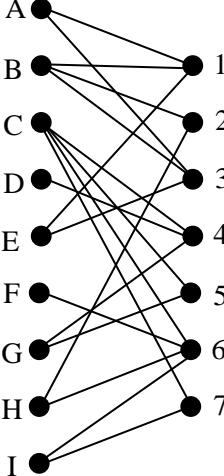
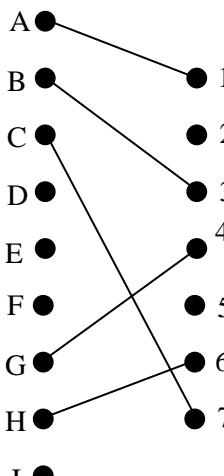
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This mark scheme is published as an aid to teachers and students, to indicate the requirements of the examination. It shows the basis on which marks were awarded by examiners. It does not indicate the details of the discussions which took place at an examiners' meeting before marking commenced.

All examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

Mark schemes should be read in conjunction with the published question papers and the report on the examination.

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Question		Answer	Marks	Guidance
1	(i)		M1 A1	A and I correct
	(ii)	 <p> Breakthrough paths found: <ul style="list-style-type: none"> A — 1 — E breakthrough B — 3 — E breakthrough 2 — H — 6 — C — 7 — F breakthrough 5 — C — 7 — I breakthrough 5 — G — 4 — D breakthrough </p>	B1 M1 A1 B1 M1 A1 M1 A1 B1	bipartite an alternating path from 2 E1, B2, A3 or A1, B2, E3 or A1, H2, B3 (with F6) an alternating path from 5 G4, C5, H6, I7 or D4, G5, H6, C7

Question	Answer	Marks	Guidance																
(iii)	Max $4A1 + 4A3 + 4B1 + 3B2 + 4B3 + 5C4 + 5C5 + 5C6 + 5C7 + 4D4 + 3E1 + 3E3 + 4F6 + 4G4 + 4G5 + 2H2 + 3H6 + 5I6 + 4I7$ st $A1 + A3 \leq 1$ $B1 + B2 + B3 \leq 1$ $C4 + C5 + C6 + C7 \leq 1$ $D4 \leq 1$ $E1 + E3 \leq 1$ $F6 \leq 1$ $G4 + G5 \leq 1$ $H2 + H6 \leq 1$ $I6 + I7 \leq 1$ $A1 + B1 + E1 \leq 1$ $B2 + H2 \leq 1$ $A3 + B3 + E3 \leq 1$ $C4 + D4 + G4 \leq 1$ $C5 + G5 \leq 1$ $C6 + H6 + F6 + I6 \leq 1$ $C7 + I7 \leq 1$ end	B1 M1 A1 M1 A1	objective player constraints “ $<$ ” is correct (throughout) position constraints allow (grudgingly) “ $=$ ” Penalise -1 for setting it up as an IP.																
(iv)	running successfully <table border="1"> <tr> <td>Position</td> <td>1</td> <td>2</td> <td>3</td> <td>4</td> <td>5</td> <td>6</td> <td>7</td> </tr> <tr> <td>Player</td> <td>B</td> <td>H</td> <td>A</td> <td>D</td> <td>G</td> <td>I</td> <td>C</td> </tr> </table> Total manager score = 28.	Position	1	2	3	4	5	6	7	Player	B	H	A	D	G	I	C	B1 B1 B1 B1	positions 1, 2 and 3 positions 4, 5, 6 and 7
Position	1	2	3	4	5	6	7												
Player	B	H	A	D	G	I	C												

Question		Answer												Marks	Guidance																																																															
2	(i)	eg												B1	λ and β OK																																																															
		λ	β	time	$f(t)$	$s(t)$	$10-f(t)-s(t)$	$P(+)$	$P(-)$	+	-	$f(t+1)$	$s(t+1)$	B1	time																																																															
		0.04	0.2	0	2	8	0	0.64	0.4	1	0	3	7	B1	f, s and <i>recovered</i> above updated																																																															
				1	3	7	0	0.84	0.6	1	-1	3	6	B1	probabilities																																																															
														B1	use of absolute addresses																																																															
														B1	“IF” statements																																																															
														B1	computation of $f(t+1)$ and $s(t+1)$																																																															
	(ii)	running												B1																																																																
		time t and $s(t)$ noted												B1																																																																
	(iii)	eg																																																																												
		<table border="1"> <tr> <td>Run</td><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td><td>7</td><td>8</td><td>9</td><td>10</td><td>11</td><td>12</td><td>13</td><td>14</td><td>15</td><td>16</td><td>17</td><td>18</td><td>19</td><td>20</td></tr> <tr> <td>t</td><td>37</td><td>33</td><td>16</td><td>3</td><td>12</td><td>15</td><td>18</td><td>17</td><td>15</td><td>27</td><td>24</td><td>16</td><td>25</td><td>18</td><td>19</td><td>23</td><td>8</td><td>17</td><td>34</td><td>16</td></tr> <tr> <td>$s(t)$</td><td>3</td><td>0</td><td>2</td><td>8</td><td>3</td><td>2</td><td>0</td><td>0</td><td>4</td><td>1</td><td>0</td><td>1</td><td>1</td><td>1</td><td>1</td><td>1</td><td>7</td><td>4</td><td>0</td><td>4</td></tr> </table>	Run	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	t	37	33	16	3	12	15	18	17	15	27	24	16	25	18	19	23	8	17	34	16	$s(t)$	3	0	2	8	3	2	0	0	4	1	0	1	1	1	1	1	7	4	0	4													
Run	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20																																																										
t	37	33	16	3	12	15	18	17	15	27	24	16	25	18	19	23	8	17	34	16																																																										
$s(t)$	3	0	2	8	3	2	0	0	4	1	0	1	1	1	1	1	7	4	0	4																																																										
		t is time to infection dying out – usually within 24 hours, but occasionally longer																																																																												
		$s(t)$ is the number who survive without being infected – usually few but occasionally more																																																																												
	(iv)	less time												B1																																																																
		more survivors												B1																																																																
	(v)	t in minutes												B1	Implies more runs, but “more runs” scores zero																																																															

Question			Answer	Marks	Guidance
3	(a)	(i)	Auxiliary ... $\lambda^2 - 0.8\lambda - 0.2 = 0$, so $\lambda = 1$ or -0.2 Gives $A + B(-0.2) = 7$ and $A + B(-0.2)^2 = 8$ So $A = 47/6$ and $B = 25/6$ giving $T_n = 47/6 + (25/6)(-1/5)^n$	B1 B1 B1 B1 B1 B1 B1 B1	
		(ii)	a 0.8 7 1 7 b 0.2 8 2 8 c 0 7.8 3 7.8 7.84 4 7.84 7.832 5 7.832 7.8336 6 7.8336 7.83328 7 7.83328 7.833344 8 7.833344 7.833331 9 7.833331 7.833334 10 7.833334 7.833333 11 7.833333 ... and then repeated to line 20.	M1 A1 B1	RR - use of absolute addressing or equivalent formula
		(iii)	$7\frac{5}{6}$	B1	

Question	Answer	Marks	Guidance
(iv)	a 0.8 b 0.2 c 0.1 7 8 7.9 8.02 8.096 8.1808 8.26384 8.347232 8.4305536 8.51388928 8.597222144 8.680555571 8.763888886 8.847222223 8.930555555 9.013888889 9.097222222 9.180555556 9.263888889 9.347222222 Differences converge to 1/12	B1	
(v)	eg $T_n = (643/72) + (n - 15)/12$	B1	
(vi)	$a = 0.6$ $b = 0.4$ $c = 0.2$	B1B1B 1	2/3 for solutions from simultaneous eqns

Question	Answer	Marks	Guidance
4 (i)		M1 A1	geometry and two correct weights
(ii)	<p>eg</p> <p>The demand at B is not satisfied.</p> <p>Cut $\{S, A, D, C, F, E\} / \{B, T\}$ has capacity of 70.</p>	B1 B1 B1	B not satisfied max flow/min cut

Question	Answer	Marks	Guidance
(iii)	Max SA+SD (or BT + ET) st SA<40 SD<40 BT<50 ET<30 AB<20 AC<30 DC<20 DF<30 CB<20 CF<50 FC<50 FE<60 BE<70 SA-AC-AB=0 SD-DC-DF=0 AC+DC+FC-CF-CB=0 DF+CF-FC-FE=0 AB+CB-BE-BT=0 BE+FE-ET=0 end	B1 B1 B1 B1 B1 B1 B1 B1 B1 B1 B1 B1 B1 M1 A1	objective one-way capacities two-way capacities balancing at A, D, B and E balancing at C and F

Question		Answer	Marks	Guidance																										
(iv)		<p>Objective value: 70.00000</p> <p>Variable Value</p> <table> <tbody> <tr><td>SA</td><td>30.00000</td></tr> <tr><td>SD</td><td>40.00000</td></tr> <tr><td>BT</td><td>40.00000</td></tr> <tr><td>ET</td><td>30.00000</td></tr> <tr><td>AB</td><td>20.00000</td></tr> <tr><td>AC</td><td>10.00000</td></tr> <tr><td>DC</td><td>20.00000</td></tr> <tr><td>DF</td><td>20.00000</td></tr> <tr><td>CB</td><td>20.00000</td></tr> <tr><td>CF</td><td>50.00000</td></tr> <tr><td>FC</td><td>40.00000</td></tr> <tr><td>FE</td><td>30.00000</td></tr> <tr><td>BE</td><td>0.000000</td></tr> </tbody> </table> <p>CF=50 and FC=40 means CF=10</p>	SA	30.00000	SD	40.00000	BT	40.00000	ET	30.00000	AB	20.00000	AC	10.00000	DC	20.00000	DF	20.00000	CB	20.00000	CF	50.00000	FC	40.00000	FE	30.00000	BE	0.000000	<p>B1</p> <p>B1</p> <p>B1</p>	<p>running</p> <p>rest</p>
SA	30.00000																													
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(v)		Objective value: 80.00000 Variable Value SA 40.00000 SD 40.00000 BT 30.00000 ET 50.00000 AB 20.00000 AC 20.00000 DC 20.00000 DF 20.00000 CB 20.00000 CF 50.00000 FC 30.00000 FE 40.00000 BE 10.00000 CF=50 and FC=30 means CF=20													B1	modification																																																				
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