

OCR

Oxford Cambridge and RSA

Level 3 Cambridge Technical in Engineering

05822/05823/05824/05825 /05873

Unit 23: Applied mathematics for engineering

Wednesday 18 January 2017 – Afternoon

Time allowed: 2 hours

You must have:

- the formula booklet for Level 3 Cambridge Technical in Engineering (inserted)
- a ruler (cm/mm)
- a scientific calculator

First Name					Last Name				
Centre Number					Candidate Number				
Date of Birth									

INSTRUCTIONS

- Use black ink. You may use an HB pencil for graphs and diagrams.
- Complete the boxes above with your name, centre number, candidate number and date of birth.
- Answer **all** the questions.
- Write your answer to each question in the space provided.
- Additional paper may be used if required but you must clearly show your candidate number centre number and question number(s).
- The acceleration due to gravity is denoted by $g \text{ m s}^{-2}$. Unless otherwise instructed, when a numerical value is needed, use $g = 9.8$.

INFORMATION

- The total mark for this paper is **80**.
- The marks for each question are shown in brackets [].
- Where appropriate, your answers should be supported with working. Marks may be given for a correct method even if the answer is incorrect.
- An answer may receive no marks unless you show sufficient detail of the working to indicate that a correct method is being used.
- Final answers should be given to a degree of accuracy appropriate to the context.
- This document consists of **16** pages.

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Question No	Mark
1	/11
2	/11
3	/14
4	/12
5	/11
6	/12
7	/9
Total	/80

Answer **all** questions.

- 1** For this question you may refer to the constant acceleration formulae in section 6.4 of the formula booklet provided.

A new car is being tested for braking distance on a test track. The car is travelling at a speed of $v \text{ m s}^{-1}$ when the brakes are applied and the car comes to rest after 3 s. The distance, $s \text{ m}$, that the car travels in $t \text{ s}$ after the brakes are applied is recorded. Recordings are made at 0.5 s intervals and the results are shown in Table 1.

Time t (s)	Distance travelled s (m)
0	0
0.5	13.75
1	25
1.5	33.75
2	40
2.5	43.75
3	45

Table 1

- (a) On the grid below, draw a graph of s against t for $0 \leq t \leq 3$.



[3]

- (b) The car decelerates uniformly. The distance the car travels may be modelled by the following equation.

$$s = At^2 + Bt \quad \text{for } 0 \leq t \leq 3$$

- (i) Use information from Table 1 to calculate the values of A and B .

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 [3]

- (ii) Calculate the time taken for the car to travel the first 30 m after the brakes are applied.

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 [3]

- (iii) Calculate the speed of the car when $t = 0$.

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 [1]

- (iv) Calculate the deceleration of the car.

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 [1]

- 3 Fig. 3 shows a concrete block of mass m kg supported at rest in equilibrium by two ropes, A and B. Rope A has tension T_1 N and Rope B has tension T_2 N. The angle between the two ropes is α° and the angle between Rope B and the horizontal is α° where $0 < \alpha < 90$.

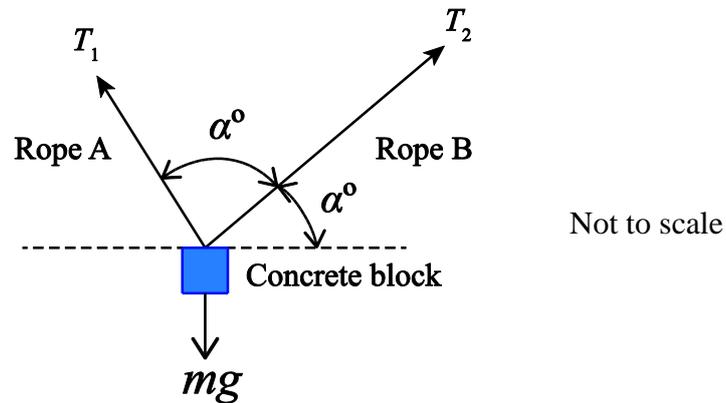


Fig. 3

- (a) Express the tensions T_1 and T_2 as vectors \vec{T}_1 and \vec{T}_2 in component form, expressing each component in terms of α and T_1 or T_2 as appropriate.

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..... [4]

- (b) Sketch a vector diagram showing the relationship between the resultant vector $\vec{R} = \vec{T}_1 + \vec{T}_2$ and the vectors \vec{T}_1 and \vec{T}_2 .

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- 5 A domestic storage heater produces heat over a 10-hour period. During this time the instantaneous power, P kW, produced is modelled by the equation

$$P = 4he^{-\frac{h}{2}},$$

where h is the time, measured in hours, from when the heating system is turned on.

- (a) Calculate the time at which the instantaneous power produced is a maximum.

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- (b) Calculate $\frac{1}{10} \int_0^{10} 4he^{-\frac{h}{2}} dh$ to find the average power produced during the 10-hour period.

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(b) You are given following values.

$$\omega = 10^4 \quad R = 1 \quad L = 10^{-2} \quad C = 10^{-5}$$

(i) Express Z_t in the form $a + jb$ where a and b are real values.

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(ii) Express Z_t in the form $r(\cos \theta + j\sin \theta)$ where r is a real value and θ is an angle in degrees.

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(c) Comment on whether or not the model appears to provide a realistic description of the speed of the flywheel as it is slowing down.

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..... [2]

END OF QUESTION PAPER

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