



**FREE-STANDING MATHEMATICS QUALIFICATION
ADVANCED LEVEL**

Additional Mathematics

6993

Candidates answer on the Answer Booklet

OCR Supplied Materials:

- 16 page Answer Booklet
- Graph paper

Other Materials Required:

None

Tuesday 15 June 2010

Morning

Duration: 2 hours



* 6 9 9 3 *

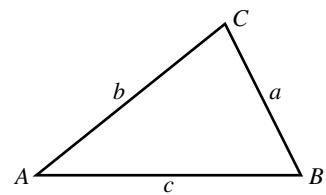
INSTRUCTIONS TO CANDIDATES

- Write your name clearly in capital letters, your Centre Number and Candidate Number in the spaces provided on the Answer Booklet.
- Use black ink. Pencil may be used for graphs and diagrams only.
- Read each question carefully and make sure that you know what you have to do before starting your answer.
- Answer **all** the questions.
- You are permitted to use a scientific or graphical calculator in this paper.
- You are not allowed a formulae booklet in this paper.
- Final answers should be given correct to three significant figures where appropriate.

INFORMATION FOR CANDIDATES

- The number of marks is given in brackets [] at the end of each question or part question.
- You are advised that an answer may receive **no marks** unless you show sufficient detail of the working to indicate that a correct method is being used.
- The total number of marks for this paper is **100**.
- This document consists of **8** pages. Any blank pages are indicated.

Formulae Sheet: 6993 Additional Mathematics

In any triangle ABC **Cosine rule** $a^2 = b^2 + c^2 - 2bc \cos A$ **Binomial expansion**When n is a positive integer

$$(a + b)^n = a^n + \binom{n}{1} a^{n-1} b + \binom{n}{2} a^{n-2} b^2 + \dots + \binom{n}{r} a^{n-r} b^r + \dots + b^n$$

where

$$\binom{n}{r} = {}^n C_r = \frac{n!}{r!(n-r)!}$$

Section A

- 1 Solve the inequality $3 - x < 4(x - 1)$. [3]
- 2 Expand $(1 - x)^{12}$ in ascending powers of x up to the term in x^3 , and simplify your answer. [3]
- 3 The function $f(x)$ is defined by $f(x) = x^3 - 5x^2 + 2x + 8$.
- (i) Find the remainder when $f(x)$ is divided by $(x + 1)$. [2]
 - (ii) Solve the equation $f(x) = 0$. [3]
- 4 In a game 4 fair dice are thrown.
- Calculate the probability that
- (i) no six is thrown, [2]
 - (ii) at least 2 sixes are thrown. [4]
- 5 The curve $y = x^3 - 3x^2 - 9x + 7$ has two turning points, one of which is where $x = 3$.
- (i) Find the coordinates of the other turning point and determine whether it is a maximum or minimum point. [5]
 - (ii) Sketch the curve. [1]
- 6 An aeroplane touches down at a point A on a runway, travelling at 90 m s^{-1} . It then decelerates uniformly until it reaches a speed of 6 m s^{-1} at a point B on the runway, 2016 m from A.
- (i) Find the deceleration. [3]
 - (ii) Find the time taken to travel from A to B. [2]

- 7 It is required to solve the equation $\sin \theta \cos \theta = \frac{1}{4}$.

(i) Show that $\frac{\sin \theta}{\cos \theta} + \frac{\cos \theta}{\sin \theta} = \frac{1}{\sin \theta \cos \theta}$. [1]

(ii) Hence show that the equation $\sin \theta \cos \theta = \frac{1}{4}$ is equivalent to $\tan \theta + \frac{1}{\tan \theta} = 4$. [2]

(iii) By expressing this equation as a quadratic equation in t , where $t = \tan \theta$, find the two values of θ , in the range $0^\circ \leq \theta \leq 180^\circ$, that satisfy the equation. [4]

- 8 A train moves between two stations, taking 5 minutes for the journey.

The velocity of the train may be modelled by the equation $v = 60(t^4 - 10t^3 + 25t^2)$ where v is measured in metres per minute and t is measured in minutes.

Calculate the distance between the two stations. [5]

- 9 The diameter of a circle is PQ, where P and Q are the points (1, 3) and (15, 1) respectively.

(i) Find the centre of the circle. [2]

(ii) Show that the radius of the circle is $5\sqrt{2}$. [2]

(iii) Hence find the equation of the circle in the form $x^2 + y^2 + ax + by + c = 0$. [2]

- 10 John and Paul are carrying out an experiment.

The table shows their results for x and y .

x	0	2	3	4
y	4	0	0.25	0

Paul proposes that the relationship should be modelled by $y = k(x - 2)(x - 4)$. This is shown in Fig. 10.

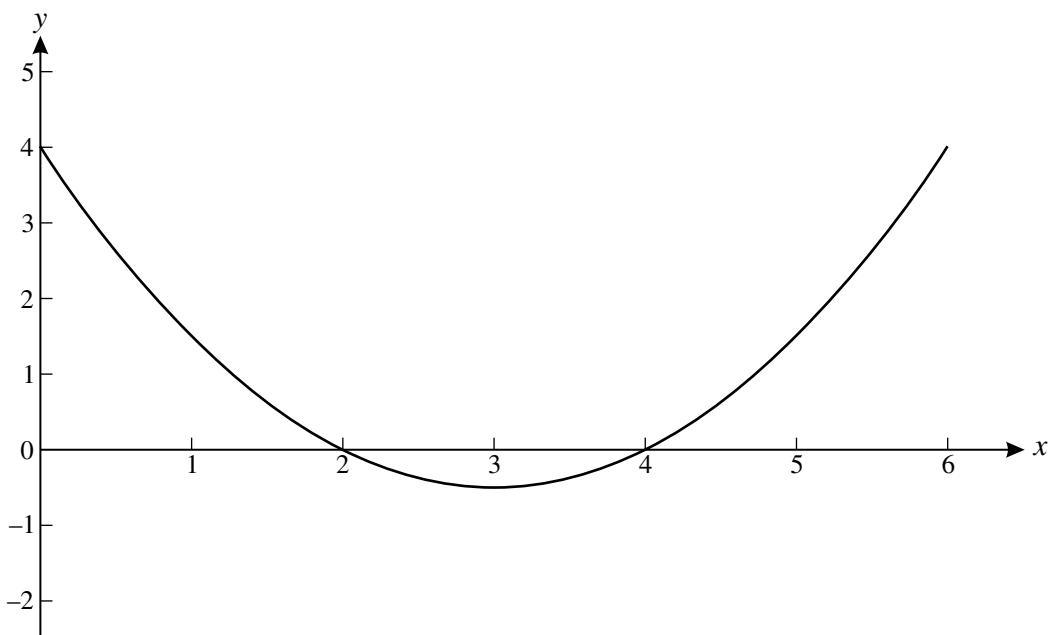


Fig. 10

- (i) Find the value of k for which the points $(0, 4)$, $(2, 0)$ and $(4, 0)$ satisfy this equation. [2]

John proposes a different model, using $y = c(x - 2)^2(x - 4)$.

- (ii) Find the value of c for which the points $(0, 4)$, $(2, 0)$ and $(4, 0)$ satisfy this equation. [2]

- (iii) Which is the better model for John and Paul's results? Give a reason for your answer. [2]

Section B

- 11 Michael is at a point A and the base of a church tower is at a point F, as shown in Fig. 11. He measures the bearing of the tower to be 060° . Michael walks 100 metres due North to the point B from where he measures the bearing of F to be 110° . The triangle ABF is in the horizontal plane.

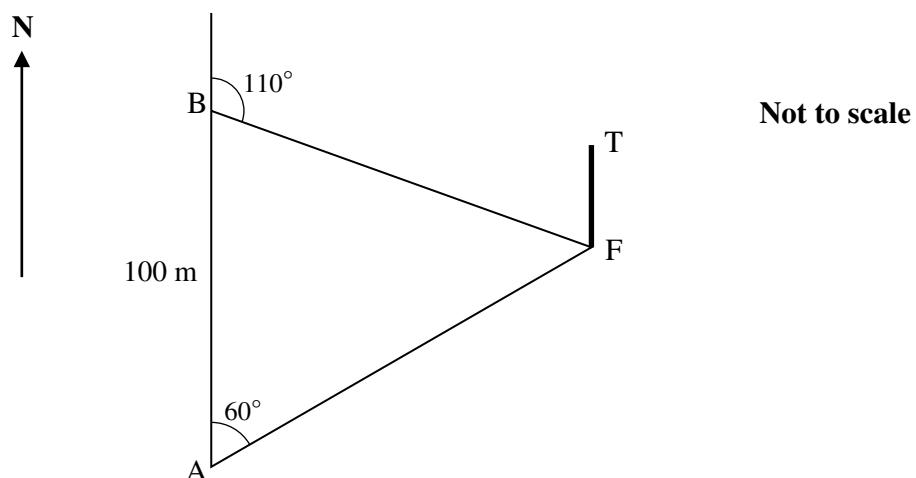


Fig. 11

- (i) Show that $AF = 122.7$ m, correct to 4 significant figures, and find BF. [5]

Michael finds that the angle of elevation of the top of the tower, T, from A is 10° .

- (ii) Find the height of the tower. [2]

C is the point on AB that is nearest to F.

- (iii) Find CF and the angle of elevation from C to the top of the tower, correct to 1 decimal place. [5]

12 Fig. 12 shows the shape AOB that is to be made from card.

B is the point (5, 0) and OB is part of the curve with equation $y = 0.3x^2 - 1.5x$.

The line AB is the normal to the curve at B.

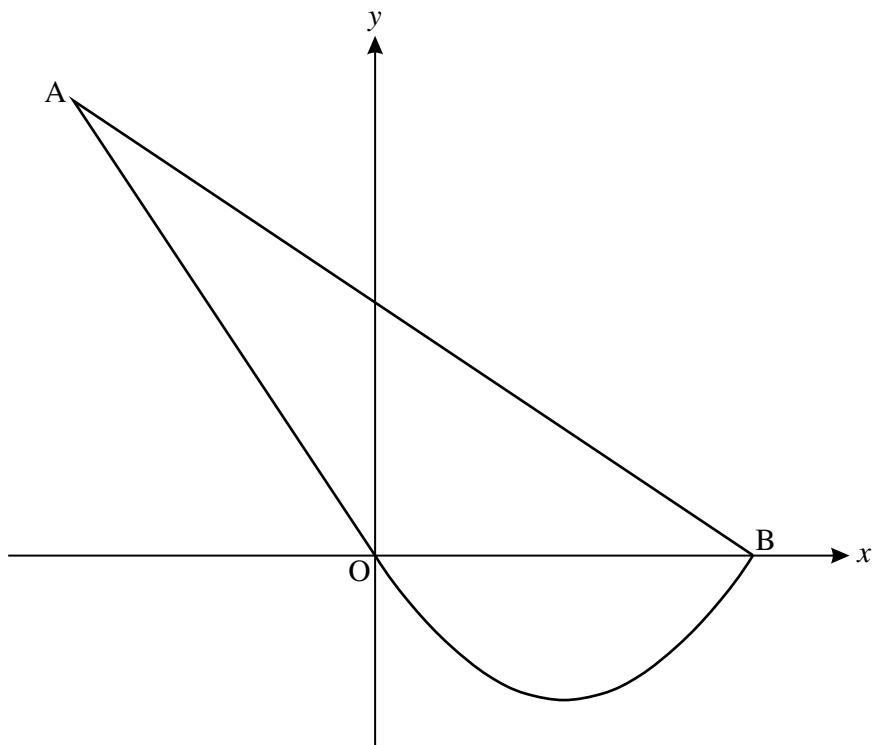


Fig. 12

(i) Find the equation of the line AB. [4]

The equation of the line AO is $2y + 3x = 0$.

(ii) Find the coordinates of the point A. [3]

(iii) Find the area of the shape AOB. [5]

[Questions 13 and 14 are printed overleaf.]

- 13 Ali and Beth make components in a factory. Ali works faster than Beth and makes 3 more components per hour. As a result he takes 2 hours less time than Beth to make 72 components.

Let t hours be the time that Ali takes to make 72 components.

(i) Write expressions for the numbers of components made per hour by Ali and by Beth. [3]

(ii) Hence derive the equation $3t(t + 2) = 144$. [5]

(iii) Solve this equation to find the times that Ali and Beth take to make 72 components. [4]

- 14 A firm has to transport 1500 packages to a site. It has a number of large vans which will transport 200 packages each and a number of small vans which will transport 100 packages each.

Let x be the number of large vans and let y be the number of small vans used.

(i) Write down an inequality based on the number of packages transported. [2]

The firm needs to use at least as many small vans as large vans.

(ii) Write a second inequality. [1]

(iii) Plot these two inequalities on a graph, using 1 cm to represent one van on each axis. Indicate the region for which these inequalities hold. Shade the area that is **not** required. [3]

A large van costs £80 to complete the trip and a small van costs £60 to complete the trip.

(iv) Write down the objective function and hence find from your graph the number of each type of van that will minimise the cost, and work out that cost. [4]

(v) What choice of vans should be made to minimise the cost if the restriction about the large and small vans is removed? Work out the cost in this case. [2]



Copyright Information

OCR is committed to seeking permission to reproduce all third-party content that it uses in its assessment materials. OCR has attempted to identify and contact all copyright holders whose work is used in this paper. To avoid the issue of disclosure of answer-related information to candidates, all copyright acknowledgements are reproduced in the OCR Copyright Acknowledgements Booklet. This is produced for each series of examinations, is given to all schools that receive assessment material and is freely available to download from our public website (www.ocr.org.uk) after the live examination series.

If OCR has unwittingly failed to correctly acknowledge or clear any third-party content in this assessment material, OCR will be happy to correct its mistake at the earliest possible opportunity. For queries or further information please contact the Copyright Team, First Floor, 9 Hills Road, Cambridge CB2 1GE.

OCR is part of the Cambridge Assessment Group; Cambridge Assessment is the brand name of University of Cambridge Local Examinations Syndicate (UCLES), which is itself a department of the University of Cambridge.