

OXFORD CAMBRIDGE AND RSA EXAMINATIONS
FSMQ

6993

ADVANCED LEVEL

Additional Mathematics

QUESTION PAPER

WEDNESDAY 30 MAY 2012: Afternoon

DURATION: 2 hours

plus your additional time allowance

MODIFIED ENLARGED

Candidates answer on the Printed Answer Book or any suitable paper provided by the centre.

OCR SUPPLIED MATERIALS:

Printed Answer Book 6993

OTHER MATERIALS REQUIRED:

Scientific or graphical calculator

READ INSTRUCTIONS OVERLEAF

INSTRUCTIONS TO CANDIDATES

These instructions are the same on the Printed Answer Book and the Question Paper.

- **The Question Paper will be found in the centre of the Printed Answer Book.**
- **Write your name, centre number and candidate number in the spaces provided on the Printed Answer Book. Please write clearly and in capital letters.**
- **WRITE YOUR ANSWER TO EACH QUESTION IN THE SPACE PROVIDED IN THE PRINTED ANSWER BOOK.** Additional paper may be used if necessary but you must clearly show your candidate number, centre number and question number(s).
- **Use black ink. HB pencil may be used for graphs and diagrams only.**
- **Answer ALL the questions.**
- **Read each question carefully. Make sure you know what you have to do before starting your answer.**
- **You are permitted to use a scientific or graphical calculator in this paper.**
- **Final answers should be given correct to three significant figures where appropriate.**

INFORMATION FOR CANDIDATES

This information is the same on the Printed Answer Book and the Question Paper.

- **The number of marks is given in brackets [] at the end of each question or part question on the Question Paper.**
- **You are advised that an answer may receive NO MARKS unless you show sufficient detail of the working to indicate that a correct method is being used.**
- **The total number of marks for this paper is 100.**

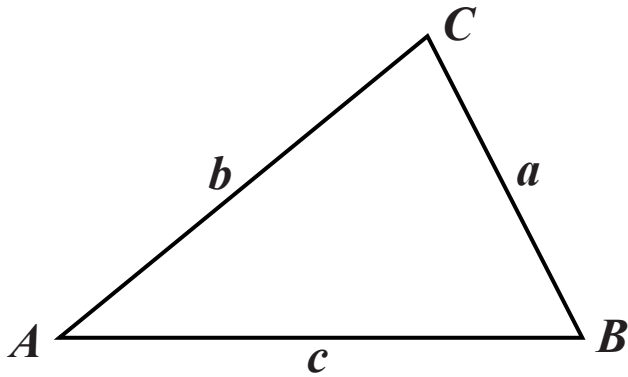
INSTRUCTION TO EXAMS OFFICER/INVIGILATOR

- **Do not send this Question Paper for marking; it should be retained in the centre or recycled. Please contact OCR Copyright should you wish to re-use this document.**

FORMULAE SHEET: 6993 ADDITIONAL MATHEMATICS

IN ANY TRIANGLE ABC

COSINE RULE $a^2 = b^2 + c^2 - 2bc \cos A$



BINOMIAL EXPANSION

When n is a positive integer

$$(a + b)^n = a^n + \binom{n}{1} a^{n-1}b + \binom{n}{2} a^{n-2}b^2 + \dots + \binom{n}{r} a^{n-r}b^r + \dots + b^n$$

where

$$\binom{n}{r} = {}^nC_r = \frac{n!}{r!(n-r)!}$$

SECTION A

- 1 (i) Find the range of values of x satisfying $x^2 - 4x + 3 \leq 0$. [3]
- (ii) Show this range on the number line provided. [1]
- 2 A die has 6 faces numbered one to six. The die is biased so that when it is thrown the probability of obtaining a six is $\frac{1}{5}$.
- The die is thrown 5 times.
- Find the probability of obtaining
- (i) at least 1 six, [2]
- (ii) exactly 3 sixes. [4]
- 3 The function $f(x) = x^3 + ax + 6$ is such that when $f(x)$ is divided by $(x - 3)$ the remainder is 12.
- (i) Show that the value of a is -7 . [2]
- (ii) Factorise $f(x)$. [3]

- 4 A car moves from rest with constant acceleration on a straight road. When the car passes a point A it is travelling at 10 m s^{-1} and when it passes a point B further along the road it is travelling at 16 m s^{-1} .**

The car takes 10 seconds to travel from A to B.

Find

- the distance AB,**
- the constant acceleration. [4]**

- 5 (i) Show that the equation $3\cos^2 \theta = \sin \theta + 1$ can be written as $3\sin^2 \theta + \sin \theta - 2 = 0$. [2]**

- (ii) Solve this equation to find values of θ in the range $0^\circ < \theta < 360^\circ$ that satisfy**

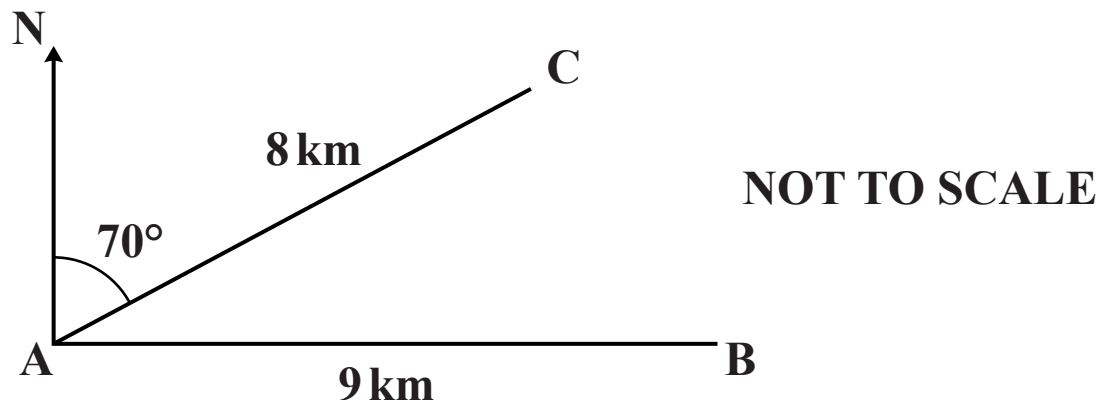
$$3\cos^2 \theta = \sin \theta + 1 . \quad [4]$$

- 6 The equation of a curve is $y = 2x^3 - 9x^2 + 12x$.**

- (i) Show that the curve has a stationary point where $x = 2$. [4]**

- (ii) Determine whether the stationary value where $x = 2$ is a maximum or minimum. [2]**

- 7 A yachtsman wishes to sail from a port, A, to another port, B, which is 9 km due East of A. Because of the wind he is unable to sail directly East and sails 8 km on a bearing of 070° to point C. This is shown on the following diagram.

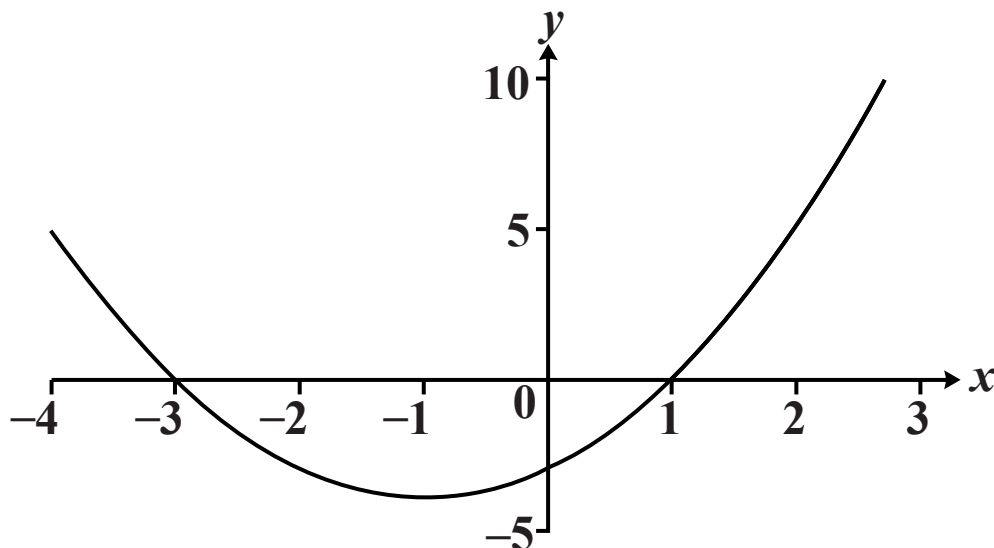


Calculate

- (i) the distance he is now from port B, [3]
- (ii) the angle ABC and hence the bearing on which he must sail to reach port B from point C, correct to the nearest degree. [4]

- 8 (i) Show that $\int_0^2 (x^2 + 2x - 3) dx = \frac{2}{3}$. [3]**

The diagram below shows part of the curve $y = x^2 + 2x - 3$.



- (ii) Marc claims that the total area between the curve, the x -axis and the lines $x = 0$ and $x = 2$ is $\frac{2}{3}$.**

Explain why he is wrong. [1]

- (iii) Calculate the total area between the curve, the x -axis and the lines $x = 0$ and $x = 2$. [3]**

- 9 The height above the ground of a seat on a fairground big wheel is h metres. At time t MINUTES after the wheel starts, h is given by**

$$h = 7 - 5\cos(480t)^\circ.$$

- (i) Write down the initial height above the ground of the seat (when $t = 0$). [1]**
- (ii) Find the greatest height reached by the seat. [2]**
- (iii) Calculate the time of the first occasion when the seat is 9 metres above the ground. Give your answer correct to the nearest second. [4]**

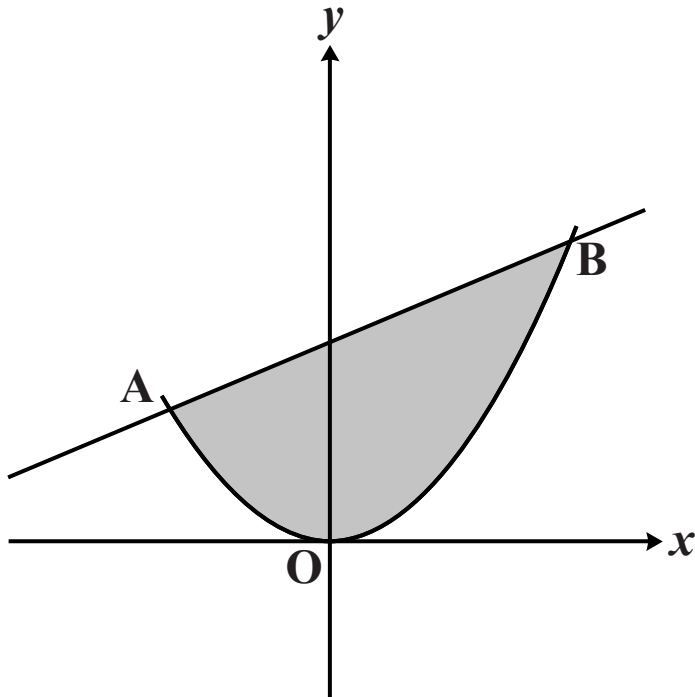
SECTION B

10 A (1, 10), B (8, 9) and C (7, 2) are three points.

- (i) Find the coordinates of the midpoint, M, of AC. [1]**
- (ii) Find the equation of the circle with AC as diameter. [4]**
- (iii) Show that B lies on this circle. [1]**
- (iv) Prove that AM and BM are perpendicular. [3]**
- (v) BD is a diameter of this circle. Find the coordinates of D. [3]**

- 11 The shaded region in the diagram below shows a wooden shape.**

The curve has equation $y = \frac{1}{2}x^2$ and the coordinates of A are $(-2, 2)$.



The line AB is the normal to the curve at the point A.

- (i) Find the equation of the line AB. [5]**
- (ii) Find the coordinates of the point B where the line AB meets the curve again. [3]**
- (iii) Find the shaded area. [4]**

- 12 The Highway Code gives a table of shortest stopping distances (d feet) for a vehicle travelling at v miles per hour.**

The formula used for this table is given by

$$d = av^2 + bv .$$

Two entries in the table are given below.

v mph	d feet
30	75
60	240

- (i) By forming and solving a pair of simultaneous equations in a and b , show that the formula is**

$$d = \frac{v^2}{20} + v. \quad [5]$$

- (ii) Find the difference between the stopping distances for a car travelling at 65 mph and a car travelling at 70 mph.** [3]

- (iii) Many drivers maintain a distance of 50 feet or less when driving on a motorway.**

Use the formula in part (i) to find the speed at which the shortest stopping distance is 50 feet. [4]

- 13 (i) Find the coefficients a , b and c in the expansion

$$(2 + h)^3 = 8 + ah + bh^2 + ch^3 . \quad [3]$$

- (ii) The graph of the equation $y = x^3$ passes through the points P and Q which have x -coordinates 2 and $2 + h$ respectively.

Show that the gradient of the chord PQ is $\frac{(2 + h)^3 - 8}{h}$. [3]

- (iii) Express $\frac{(2 + h)^3 - 8}{h}$ as a quadratic function of h . [2]

- (iv) As the value of h decreases, the point Q gets closer and closer to the point P on the curve. As h gets closer to 0 the chord PQ gets closer to being the tangent to the curve at P.

Deduce the value of the gradient of the tangent at P. [1]

- (v) Kareen uses the same method to deduce the value of the gradient of the tangent at the point (2, 16) on the curve $y = x^4$.

The first three lines of her working are given below and in the answer booklet.

Take P to be the point (2, 16)

Take Q to be the point (2 + h, (2 + h)⁴)

The gradient of the chord PQ is given by

$$\frac{(2+h)^4 - 16}{h} =$$

Complete Kareen's working.

[3]

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