

## Wednesday 3 June 2015 – Morning

### FSMQ ADVANCED LEVEL

6993/01 Additional Mathematics

### QUESTION PAPER

Candidates answer on the Printed Answer Book.

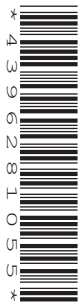
**OCR supplied materials:**

- Printed Answer Book 6993/01

**Other materials required:**

- Scientific or graphical calculator

**Duration:** 2 hours



### INSTRUCTIONS TO CANDIDATES

These instructions are the same on the Printed Answer Book and the Question Paper.

- The Question Paper will be found inside the Printed Answer Book.
- Write your name, centre number and candidate number in the spaces provided on the Printed Answer Book. Please write clearly and in capital letters.
- **Write your answer to each question in the space provided in the Printed Answer Book.** Additional paper may be used if necessary but you must clearly show your candidate number, centre number and question number(s).
- Use black ink. HB pencil may be used for graphs and diagrams only.
- Answer **all** the questions.
- Read each question carefully. Make sure you know what you have to do before starting your answer.
- Do **not** write in the bar codes.
- You are permitted to use a scientific or graphical calculator in this paper.
- Final answers should be given correct to three significant figures where appropriate.

### INFORMATION FOR CANDIDATES

This information is the same on the Printed Answer Book and the Question Paper.

- The number of marks is given in brackets [ ] at the end of each question or part question on the Question Paper.
- You are advised that an answer may receive **no marks** unless you show sufficient detail of the working to indicate that a correct method is being used.
- The total number of marks for this paper is **100**.
- The Printed Answer Book consists of **20** pages. The Question Paper consists of **8** pages. Any blank pages are indicated.

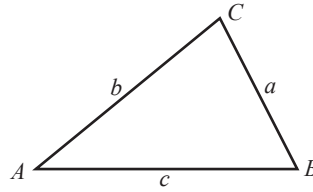
### INSTRUCTION TO EXAMS OFFICER/INVIGILATOR

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## Formulae Sheet: 6993 Additional Mathematics

In any triangle  $ABC$

**Cosine rule**  $a^2 = b^2 + c^2 - 2bc \cos A$



**Binomial expansion**

When  $n$  is a positive integer

$$(a + b)^n = a^n + \binom{n}{1} a^{n-1}b + \binom{n}{2} a^{n-2}b^2 + \dots + \binom{n}{r} a^{n-r}b^r + \dots + b^n$$

where

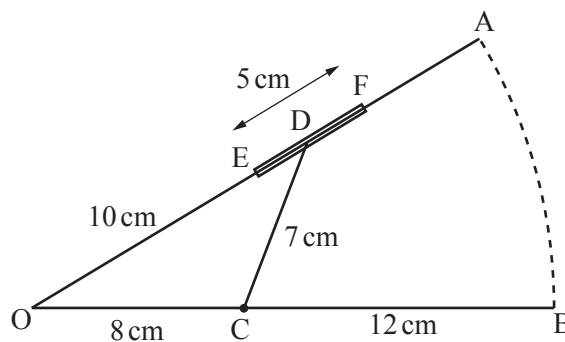
$$\binom{n}{r} = {}^nC_r = \frac{n!}{r!(n-r)!}$$

## Section A

- 1 Find the equation of the line which is perpendicular to the line  $2x + 3y = 5$  and which passes through the point  $(3, 4)$ . [3]
- 2 (i) Find  $\alpha$  in the range  $0^\circ \leq \alpha \leq 180^\circ$  such that  $\tan \alpha = -1.5$ . [2]  
(ii) Find  $\beta$  in the range  $0^\circ \leq \beta \leq 180^\circ$  such that  $\sin \beta = 0.2$ . [2]
- 3 Find the equation of the tangent to the curve  $y = x^3 + 3x - 5$  at the point  $(2, 9)$ . [5]
- 4 (i) Find  $\int_1^2 (x^2 + 2x + 3) dx$ . [4]  
(ii) Interpret your answer geometrically. [1]
- 5 A train accelerates from rest from a point O such that at  $t$  seconds the displacement,  $s$  metres from O, is given by the formula  $s = \frac{3}{2}t^2 - 2t + 3$ .  
(i) Show by calculus that the acceleration is constant. [3]  
(ii) Find the velocity after 5 seconds. [2]
- 6 You are given that  $n$  is a positive integer and  $(n - 1), n, (n + 1)$  are three consecutive integers.  
In each of the following cases form an equation in  $n$  and solve it.  
(i) The three integers add up to 99. [2]  
(ii) When the product of the first integer and third integer is added to 5 times the second integer the sum is 203. [4]

- 7 (i) Solve algebraically the simultaneous equations  $y = 3 + 5x - x^2$  and  $y = x + 7$ . [4]
- (ii) Interpret your answer geometrically. [1]
- 8 The cubic polynomial  $f(x) = x^3 + ax + 6$ , where  $a$  is a constant, has a factor of  $(x + 3)$ .
- (i) Find the value of  $a$ . [2]
- (ii) Hence or otherwise, solve the equation  $f(x) = 0$  for this value of  $a$ . [4]
- 9 The equation of the circle  $C$  is  $x^2 + y^2 - 8x + 2y - 19 = 0$ .
- (i) Express the equation of  $C$  in the form  $(x - a)^2 + (y - b)^2 = r^2$ . [4]
- (ii) Hence or otherwise, use an algebraic method to decide whether the point  $(8, 3)$  lies inside, outside or on the circumference of the circle. [2]  
Show all your working.
- 10 Fig. 10 shows a partly open window  $OA$ , viewed from above. The window is hinged at  $O$ . When the window is closed, the end  $A$  is at point  $B$ . The window is kept open by a rod  $CD$ , where  $C$  is a fixed point on the line  $OB$ . The point  $D$  slides along a fixed bar  $EF$ . When the window is closed,  $D$  is at  $F$ . When the window is fully open,  $D$  is at  $E$ .

$OA = OB = 20$  cm,  $OC = 8$  cm,  $CD = 7$  cm,  $EF = 5$  cm,  $OE = 10$  cm



**Fig. 10**

Find

- (i) angle  $EOC$  when the window is fully open, [3]
- (ii) the distance  $OD$  when angle  $EOC$  is  $30^\circ$ . [4]

## Section B

- 11 Two curves,  $S_1$  and  $S_2$  have equations  $y = x^2 - 4x + 7$  and  $y = 6x - x^2 - 1$  respectively. The curves meet at A and at B.

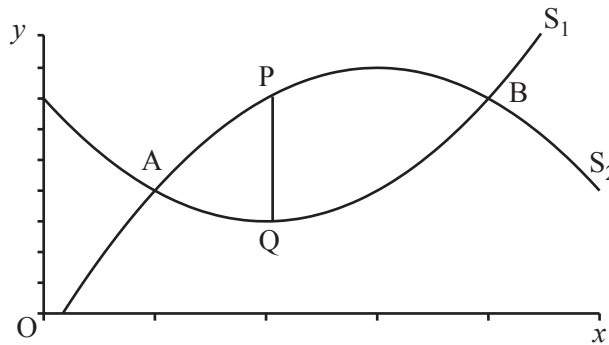


Fig. 11

- (i) Show that the coordinates of A and B are (1, 4) and (4, 7) respectively. [2]

Points P and Q lie on  $S_2$  and  $S_1$  between A and B. P and Q have the same  $x$  coordinate so that PQ is parallel to the  $y$ -axis, as shown in Fig. 11.

- (ii) Find an expression, in its simplest form, for the length PQ as a function of  $x$ . [2]
- (iii) Use calculus to find the greatest length of PQ. [4]
- (iv) Find the area between the two curves. [4]

- 12 A distributor of flower bulbs has a large number of tulip bulbs and daffodil bulbs, mixed in the ratio 1 : 3 respectively. He packs the bulbs in boxes. He puts 10 bulbs, chosen at random, into each box.

- (a) Find the probability that a box, chosen at random, contains

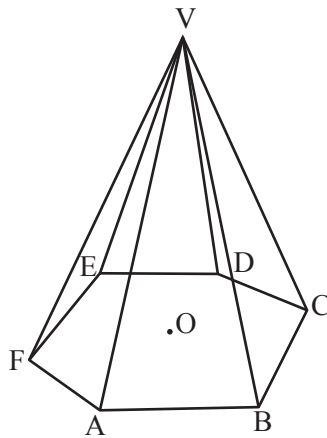
(i) exactly 4 daffodil bulbs, [4]

(ii) at least 1 tulip bulb. [3]

- (b) Two boxes of bulbs are chosen at random.

Find the probability that there is a total of 3 tulip bulbs in the two boxes. [5]

- 13** A gardener marks out a regular hexagon ABCDEF on his horizontal garden. Each side of the hexagon is 0.5 m. The gardener sticks a cane in the ground at each point of the hexagon. He joins the six canes at V where V is vertically above the centre, O, of the hexagon, as shown in Fig. 13. Each cane has a length of 2.4 m from the ground to V.



**Fig. 13**

Calculate, giving your answers to 3 significant figures,

- (i) the vertical height of V above the ground, [3]
- (ii) the angle between each cane and the ground, [2]
- (iii) the angle between the plane VAB and the ground. [4]

The gardener stretches a horizontal wire around the structure to strengthen it. He fixes the wire to each cane at a point 1 m vertically above the ground.

- (iv) Find the length of the wire. [3]

- 14** A company produces bottles of two liquids, X and Y. There are two ingredients, A and B, in each liquid.

The table shows the quantities, in centilitres (cl), of A and B needed for each bottle of liquid.

	A	B
X	4	2
Y	3	5

Each day the company can use 84 cl of A and 90 cl of B.

From this information an analyst writes down the inequality  $4x + 3y \leq 84$ .

- (i)** Explain what  $x$  and  $y$  stand for in this inequality and explain what the inequality models. **[2]**
- (ii)** Use the information given to write down another inequality, other than  $x \geq 0$  and  $y \geq 0$ . **[1]**
- (iii)** On the grid given in the answer booklet, illustrate your two inequalities. Shade the region that is not required. **[3]**
- (iv)** The company needs to produce the same number of bottles of X and of Y each day.

Find the maximum number of bottles of X and of Y that the company can produce. **[2]**

- (v)** On one day the company does not have to produce the same numbers of bottles of X and of Y.

Write down the maximum number of bottles that can be produced and all the combinations that will give this maximum. **[4]**

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