



# Level 3 Certificate

## Mathematics for Engineering

OCR Level 3 Certificate

H860/02 Paper 2

## Mark Scheme for June 2011

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Any enquiries about publications should be addressed to:

OCR Publications  
PO Box 5050  
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NOTTINGHAM  
NG15 0DL

Telephone: 0870 770 6622  
Facsimile: 01223 552610  
E-mail: [publications@ocr.org.uk](mailto:publications@ocr.org.uk)

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<b>1 a i</b>	Force = $0.01 \text{ Mg} \cos(0)$ $= 0.01 \times 1500 \times 9.8 \times 1 = 147\text{N}$	1 <b>1</b>	
<b>1 a ii</b>	Initial speed = 0, Final speed = 20, Time = 12 Acceleration $a = 20/12$ Force = $Ma = 1500 \times 5/3 = 2500$ Total force = $2500 + 147 = 2647 \text{ N}$	1 1 <b>2</b>	Allow FT from a i  Accept 20/12 and 2500 for 2 marks
<b>1 a iii</b>	For slope of 1 in 20, $\theta = \tan^{-1}(1/20) = 0.049958 \text{ radians } (2.8624^\circ)$ $F_r = 0.01 \times 1500 \times 9.8 \times \cos(0.049958) = 146.816594$ $F_i = 1500 \times 9.8 \times \sin(0.049958) = 734.082969$ Total force = $880.899563 \text{ N}$	1 1 1 <b>3</b>	Accept reasonable rounding Accept ECF from slope Accept ECF from slope 1 mark for each force or 2 marks for total
<b>1 b</b>	$u = 20$ $a = 1.5$ $v^2 = 20^2 + 2as = 400 + 2 \times 1.5 \times 300 = 1300$ $v = \sqrt{1300} = 36.06 \text{ m s}^{-1}$	1 1 <b>2</b>	Allow 1 mark for $v^2 = 2 \times 1.5 \times 300 = 900$ and $v = 30$
<b>1 c</b>	$F_r + F_i = 880.899563$ Total force = 2000 Remaining force = $2000 - 880.899563 = 1119.100437$ $F = Ma$ ; $a = F/M = 1119.100437/1500 = 0.7460669 \text{ m s}^{-2}$	1 1 <b>2</b>	Allow FT from a iii Accept reasonable rounding Remaining force = $2000 - 881.51 = 1118.49$ $F = Ma$ ; $a = F/M = 1118.49/1500 = 0.7456 \text{ m s}^{-2}$
<b>2 a i</b>	$F_d = 0.5 \times 1.2 \times 0.4 \times 2.5 \times v^2 = 0.6 \times 24^2 = 345.6 \text{ N}$ $F_r = 1500 \times 9.8 \times 0.01 = 147$ Total force = $345.6 + 147 = 492.6$ Torque at wheel = $492.6 \times 0.3 = 147.78$ Torque at motor = $147.78/4.5 = 32.84 \text{ Nm}$	1 1 1 1 <b>4</b>	Allow FT from 1 a i Allow 1 mark for $t_w = F \times 0.3$ seen Allow 1 mark for $t_m = t_w/4.5$ seen

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<b>2 a ii</b>	Speed = 24 Wheel radius = 0.3 Rotational speed of wheel = $24/0.3 = 80 \text{ rad s}^{-1}$ Rotational speed of motor = $80 \times 4.5 = 360 \text{ rad s}^{-1}$	1 1 <b>2</b>	Accept $24/(2\pi \times 0.3) \approx 12.73 \text{ revs s}^{-1}$ Accept $12.73 \times 4.5 \approx 57.29 \text{ revs s}^{-1}$
<b>2 a iii</b>	Current $i = (\text{rotational speed} \times \text{torque})/(120\eta)$ $i = (360 \times 32.84)/(120 \times 0.9) = 109.4667 \text{ A} \approx 110 \text{ A}$	1 <b>1</b>	Allow FT in both cases
<b>2 b i</b>	$F = 0.6 v^2 + 147 = 250 \text{ N}$ $v = \sqrt{(250 - 147)/0.6} = 13.1022 \text{ m s}^{-1}$	1 1 <b>2</b>	Allow FT in both cases
<b>2 b ii</b>	Terminal velocity reached when $a \rightarrow 0$ ( $F_a = 0$ ) Total force = $0.6v^2 + 147 \cos(5^\circ) + 1500 \times 9.8 \times \sin(5^\circ) = 1600$ $= 0.6v^2 + 146.4406 + 1281.1894$ $v = \sqrt{((1600 - 146.4406 - 1281.1894)/0.6)} = 16.9494 \text{ m s}^{-1}$	1 1 1 <b>3</b>	
<b>3</b>	Total force, $F = v^2 + 150$ Power = $(v^2 + 150)v$ Using $i = \text{power}/V$ $i = (v^2 + 150)v/120$ <hr/> Alternatively: Torque at wheel = $(v^2 + 150) \times l$ ( $l = \text{wheel radius}$ ) Torque at the motor = $(v^2 + 150) \times l/r$ ( $r = \text{gear ratio}$ ) Rotational speed of wheel = $v/l$ (rads/s) Rotational speed of motor = $v \times r/l$ Current required $i = (\text{rotational motor speed} \times \text{motor torque})/\text{voltage}$ $= (v \times r/l) \times ((v^2 + 150) \times l/r) / 120 = v \times (v^2 + 150)/120$ <hr/>	1  1	Allow 1 mark for use of Power = $F \times v$

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	<p>Battery time available =  <math>10000/i = (10000 \times 120)/(v \times (v^2 + 150)) \text{ min}</math>  Journey time = <math>(100 \times 10^3)/(60 \times v) \text{ min}</math>  For journey completion:  <math>(100 \times 10^3)/(60 \times v) \leq (10000 \times 120)/(v \times (v^2 + 150))</math>  <math>v^2 + 150 \leq (10000 \times 120 \times 60)/(100 \times 10^3)</math>  <math>v^2 \leq 570</math>  <math>v \leq 23.87</math></p> <p>Maximum speed = <math>23.87 \text{ m s}^{-1}</math></p>	<p>1</p> <p>1</p> <p>1</p> <p>1</p> <p>6</p>	
<b>4 a</b>	<p>Total force opposing motion = <math>F_d + F_r</math>  <math>F_d = \frac{1}{2} \times 1.2 \times 5/9 \times 3 \times v^2 = v^2</math>  <math>F_r = 9.8 \times 1200 \times 0.012755 = 150</math></p> <p>Driving force = 550  Total force = <math>550 - v^2 - 150 = 400 - v^2</math></p> <p>Force = Mass <math>\times</math> acceleration = <math>1200 \frac{dv}{dt} = 400 - v^2</math></p> <p><math>1200 \frac{dv}{dt} + v^2 = 400</math></p>	<p>1</p> <p>1</p> <p>1</p> <p>1</p> <p>4</p>	<p><math>\rho = 1.2</math> was not given explicitly in this question  so accept any reasonable attempt showing  <math>0.8333\rho v^2</math></p>

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**OCR (Oxford Cambridge and RSA Examinations)**  
**1 Hills Road**  
**Cambridge**  
**CB1 2EU**

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