

# Mark Scheme (Results)

Summer 2014

Pearson Edexcel International GCSE Mathematics A (4MA0/3H) Paper 3H

Pearson Edexcel Level 1/Level 2 Certificate Mathematics A (KMA0/3H) Paper 3H

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# **General Marking Guidance**

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme.

Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.

- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- When examiners are in doubt regarding the application of the mark scheme to a candidate's response, the team leader must be consulted.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.
- Types of mark
  - o M marks: method marks
  - o A marks: accuracy marks
  - B marks: unconditional accuracy marks (independent of M marks)
- Abbreviations
  - o cao correct answer only
  - o ft follow through
  - isw ignore subsequent working
  - o SC special case
  - o oe or equivalent (and appropriate)
  - o dep dependent
  - o indep independent
  - eeoo each error or omission
  - o awrt answer which rounds to

#### • No working

If no working is shown then correct answers normally score full marks If no working is shown then incorrect (even though nearly correct) answers score no marks.

#### • With working

If there is a wrong answer indicated on the answer line always check the working in the body of the script (and on any diagrams), and award any marks appropriate from the mark scheme.

If it is clear from the working that the "correct" answer has been obtained from incorrect working, award 0 marks.

Any case of suspected misread loses A (and B) marks on that part, but can gain the M marks.

If working is crossed out and still legible, then it should be given any appropriate marks, as long as it has not been replaced by alternative work.

If there is a choice of methods shown, then no marks should be awarded, unless the answer on the answer line makes clear the method that has been used.

If there is no answer on the answer line then check the working for an obvious answer.

#### Ignoring subsequent work

It is appropriate to ignore subsequent work when the additional work does not change the answer in a way that is inappropriate for the question: eg. Incorrect cancelling of a fraction that would otherwise be correct.

It is not appropriate to ignore subsequent work when the additional work essentially makes the answer incorrect eg algebra.

Transcription errors occur when candidates present a correct answer in working, and write it incorrectly on the answer line; mark the correct answer.

#### • Parts of questions

Unless allowed by the mark scheme part of the question CANNOT be awarded in another.

Apart from Questions 2, 14(a)(i), 14(a)(ii), 18, 19 and 23 (where the mark scheme states otherwise), the correct answer, unless clearly obtained by an incorrect method, should be taken to imply a correct method.

Question	Working	Answer	Mark		Notes
<b>1.</b> (a)	89.7 ÷ 8.41	10.66(053284)	2	M1 A1	for 89.7 or 8.41 (Accept if first 3 sig figs correct) Accept if first four sig figs correct.
(b)		10.7	1	B1ft	ft if (a) $> 3$ sig figs
					Total 3 marks

Question	Working	Answer	Mark	Notes
2.	$\frac{4}{9} \times \frac{6}{5}$ oe	24		M1 or $\frac{0.8}{1.5}$
		$\frac{24}{45}$ oe	2	A1 dep on M1. Accept $\frac{8}{15}$ if clear cancelling seen
	Alternative: $\frac{8n}{18n} \div \frac{15n}{18n}$			M1 $\frac{8n}{18n} \div \frac{15n}{18n}$
	for any integer n	$\frac{8}{15}$ oe	2	A1 dep on M1. Answer must come directly from their method eg $\frac{16}{36} \div \frac{30}{36}$ must be followed by $\frac{16}{30}$ for M1A1
				Total 2 marks

Question	Working	Answer	Mark	Notes
<b>3.</b> (a)		Reflection		B1 Accept, for example, reflect, reflected
		(in line) $x = -2$		B1
			2	Multiple transformations score B0B0
(b)		Shape in correct position		B2 Vertices at $(1, -1)(7, -1)(7, -4)(4, -4)(4, -2)(1, -2)$
				Condone omission of inner square and/or no shading and/or
				label C
				If not B2 then B1 for correct orientation but wrong position
			2	or rotation 90° anticlockwise about $(0,0)$
				Total 4 marks

Apart from Questions 2, 14(a)(i), 14(a)(ii), 18, 19 and 23 (where the mark scheme states otherwise), the correct answer, unless clearly obtained by an incorrect method, should be taken to imply a correct method.

Question	Working	Answer	Mark	Notes
<b>4.</b> (a)		$56 d^2$	1	B1 cao
(b)		12 <i>e</i> – 20	1	B1 Accept $-20 + 12e$
(c)		f (f – 2)	2	B2 Accept $(f \pm 0) (f - 2)$ oe If not B2 then B1 for factors when expanded and simplified give 2 terms, 1 of which is correct except B0 for $(f + a)(f - a)$
(d)	$2^3 + 6 \times 2 \text{ or } 8 + 12$	20	2	M1 A1 cao
				Total 6 marks

Question	Working	Answer	Mark	Notes		
5.	$\sin 38 = \frac{PQ}{12.2}$ or $\cos(90 - 38) = \frac{PQ}{12.2}$ oe			M1	12.2cos38 (9.61) and 12.2 <sup>2</sup> – "9.61" <sup>2</sup> (= 56.4)	correct statement of sine rule eg $\frac{PQ}{sin38} = \frac{12.2}{sin90}$
	("PQ" =) $12.2 \text{ x} \sin 38 \text{ or } 12.2 \cos(90 - 38) \text{ oe}$			M1	√"56.4"	correct expression for PQ eg (PQ) = $\frac{12.2sin38}{sin90}$
		7.51	3	A1 a	awrt 7.51	
						Total 3 marks

Question	Working	Answer	Mark	Notes
6.	One bearing line at $260^{\circ} (\pm 2^{\circ})$ or one 9.6 cm line ( $\pm 2$ mm) from A	Intersection of 2 lines in boundary of overlay	2	M1 A1 Condone omission of <i>D</i> label Correct position of <i>D</i> within tolerance without any lines scores M1A1.
				Total 2 marks

Question	Working	Answer	Mark	Notes	
<b>7.</b> (a) (i)		${p, r, a}$	1	B1	Withhold marks for repeats
(ii)		$\{p, a, r, i, s, b, u, d, e, t\}$	1	B1	Withhold marks for repeats
(b)		E 1.4		D1	
	no	letters common to Prague and Lisbon	1	B1	<ul> <li>dep on E in box</li> <li>Accept general reasons.</li> <li>e.g. "no letters common to sets A and E"</li> <li>or "they share no common letters"</li> <li>or "no intersection (between A and E)"</li> <li>or "no letters the same"</li> <li>or "no letter in A are in E".</li> </ul>
					Total 3 marks

Question	Working	Answer	Mark	Notes
<b>8.</b> (a)		Correct line drawn		B2 Must be a single straight line passing through at least 3 of
				(0,4) (2,3) (4,2) (6,1) (8,0) (10,-1)
				If not B2 then B1 for a single straight line with a negative
			2	gradient passing through either $(0,4)$ or $(8,0)$
				or at least 3 of (0,4) (2,3) (4,2) (6,1) (8,0) (10,-1) plotted or
				calculated
(b)		x = 2 drawn		B1
		y = 1 drawn		B1
		Correct region identified		B1 Ignore extra lines
			3	Accept R shaded or R' shaded.
				Condone omission of label R
				Total 5 marks

Question	Working	Answer	Mark	Notes
9.	0.5 x 10 x 12 (= 60) or 13 x 8 (= 104) or 8 x 10 (= 80)			M1 One correct face
	0.5 x 10 x 12 (= 60) and 0.5 x 10 x 12 (= 60) and 13 x 8 (= 104) and 13 x 8 (= 104) and 8 x 10 (= 80) or 2 x "60" and 2 x "104" and "80"			M1 dep on M1 above (exactly 5 correct faces )
		408		A1
				Award M0A0 for 0.5 x 10 x $12 \times 8$ and
			3	M0A0 for 0.5 x 10 x 12 = 60 followed by $60 \times 8$ , etc
				Total 3 marks

Question	Working	Answer		Mark	Notes				
10.	64 x 4 (=256) 70 x 5 (=350) "350" – "256"	94 or 94% or 94 / 100	94 or 94% or 94 / 100 or 94 out of 100			dep on M2 94 embedded in w unless contradicte	0.64 × 400 (= 256) 0.7 × 500 (= 350) "350" – "256" orking but not on answ d.	$0.64 \times 4 (= 2.56) \\ 0.7 \times 5 (= 3.5) \\ (3.5 - 2.56) \times 100$ er line gets M3A0	
	Alternative (i): List of 4 numbers addi List of 5 numbers addi list of 5 is identical to 1 eg 94,50,50,56,100 and	ng to 350 list of 4 but also contains 94	94 or 94% etc (as above)		M1 M1 M1 A1	dep on M2 permitted answ	vers as listed for A1 abo	we	
	Alternative (ii): 70 - 64 (=6) (70 - 64) X 4 (=24) 70 + 24		94 or 94% etc (as above)		M1 M1 M1 A1	dep on M2 permitted answ	vers as listed for A1 abo		
								Total 4 marks	

Question	Working	Answer		Mark		Notes
<b>11.</b> (a)			$60 < v \le 70$	1	B1	Accept 60 – 70 or 60 to 70 or 60 $\rightarrow$ 70
(b)					M1	for $\frac{56}{a}$ with a > 56 or $\frac{b}{180}$ with b < 180 or 0.31 or 31%
						$ \begin{array}{c} a & 180 \\ 0f & \frac{4+52}{4+52+60+34+18+12} \end{array} \end{array} $
			$\frac{56}{180}$ oe		A1	Accept answer written as an equivalent fraction, (eg $\frac{14}{45}$ ), or
			100			0.311 (accept if first 3 SF correct) or 31.1% (accept if
				2		first 3 SF correct)
				Ζ.		M1A0 for 56 : 180 or 14 : 45 oe
(c)		4, 56, 116, 15	0, 168, 180	1	B1	
(d)	All 6 plotted correctly	ро	ints plotted		B1	All 6 points plotted correctly $\pm \frac{1}{2}$ sq
		Curve or lin	e segments		B1	ft curve/line segments from points if 4 or 5 plotted correctly or if all 6 points are plotted consistently within
						each interval of frequency table at the correct heights $(\pm \frac{1}{2}$ sq).
						Accept curve which is not joined to $(40, 0)$
				2		
(e)	vertical line or mark drawn at 84				M1	for 84 indicated on cf graph
	corresponding to speed = 84km	(± <sup>1</sup> ⁄2 sq) on ct graph.	20 – 26 inclusive	2	A1	If M1 scored from 84 indicated on graph, ft from cf graph. If M1 not scored from 84 indicated on graph, ft only from a correct curve / line segments. If their answer comes from their curve $(\pm \frac{1}{2} \text{ sq})$ then award M1A1.
<u> </u>						Total 8 marks

Question	Working	Answer	Mark	Notes		
<b>12.</b> (a)	167.4 – 155 (= 12.4)			M1	167.4 ÷ 155 (= 1.08)	167.4 ÷ 155 (= 1.08)
	"12.4" ÷ 155 (= 0.08)			M1 dep	"1.08" – 1 (= 0.08)	"1.08" × 100 (= 108)
		8		A1 cao		
			3	If build up ap	proach used, award M2A	1 for correct answer,
				otherwise M0	A0.	
(b)	$\frac{125.4}{104.5} \times 100$ oe			M2		
	104.5			M1 f	for $\frac{125.4}{104.5}$ (= 1.2) or 104.5	5% = 125.4
				or 1.	045x = 125.4 oe or 1.2 see	en or 5.4
		120	3	A1		
				If build up ap otherwise M0	proach used, award M2A A0.	1 for correct answer,
		1				Total 6 marks

Question	Working	Answer	Mark	Notes	
13.	$(AC^2 =) 10^2 + 10^2 (=200)$			M1	$(AO^2 = ) 5^2 + 5^2 (= 50)$
	$(AC=) \sqrt{(10^2 + 10^2)} (= 14.1)$			M1 dep	$(AO =) \sqrt{(5^2 + 5^2)} (=7.07)$
	$\pi \times \sqrt{(10^2 + 10^2)}$ oe or 14.1 $\pi$ or $2\pi \times 7.07$			M1 dep	$2 \times \pi \times \sqrt{(5^2 + 5^2)}$
	Alternative method:				
	M1 $\cos 45 = \frac{10}{x} \text{ or } \sin 45 = \frac{10}{x}$			M1	
	M1 dep $(x =) \frac{10}{\cos 45}$ or $(x =) \frac{10}{\sin 45}$ oe $(= 14.1.)$			M1dep	
	M1 dep $\pi \times \frac{10}{\cos 45}$ or $\pi \times \frac{10}{\sin 45}$ oe			M1 dep	
		44.4	4	A1 awrt 44.3 or 44.4	
					Total 4 marks

Question	Working	Answer		Mark	Notes	
<b>14.</b> (a) (i)	12x + 10y = 180			1	B1	Accept $12x = 180 - 10y$ or $10y = 180 - 12x$
(ii)	$(A =) 4x \times 2y$				M1	$4x \times 2y$ or $8xy$ oe
	$(A =) 4x \times 2(18 - 1.2x)$	proceed to $A = 1$	$44x - 9.6 x^2$		A1	$4x \times 2(18 - 1.2x)$ or $8x(18 - 1.2x)$ or $4x(36 - 2.4x)$ oe
				2		<b>AND</b> proceeding correctly to $A = 144x - 9.6 x^2$
(b)		(dA/dx =)	144 - 19.2x		B2	B1 for 144, B1 for – 19.2 <i>x</i>
				2		Do not isw
(c)	"144 - 19.2x" = 0				M1 ft	Must be a 2 part linear expression
	x = 7.5 (y = 9)					
	$(A =) 144 \times "7.5" - 9.6 \times "7.5^{2"}$ or	( <i>A</i> =) 8 x "7.5" x "9"			M1 dep	
			540	3	A1	
						Total 8 marks

Question	Working	Answer	Mark	Notes	
15.	$3^2$ or 9			M1	3 <sup>2</sup> used or identified as area scale factor
	$3^2 \times 4$			M1	$3^2 \times 4 \text{ or } 9 \times 4 \text{ or } 36 \text{ or } 3^2 \times 4 - 4 \text{ or } (3^2 - 1) \times 4 \text{ or } 8 \times 4$
		32	3	A1	
					Total 3 marks

Question	Working	Answer	Mark	Notes
16.	$(x \times x =) 4 \times 9 (=36)$			M1 for $4 \times 9$ or $36$
	$x = \sqrt{36}$			
		6	2	A1 accept – 6
				Total 2 marks

Question	Working	Answer	Mark	Notes	
17.	$y^2 = \frac{2x+1}{x+1}$			M1	squaring both sides to get a correct equation
	$y^{2} (x - 1) = 2x + 1$ $y^{2} x - y^{2} = 2x + 1$			M1	removing denominator to get a correct equation
	$y^2 x - 2x = y^2 + 1$			M1	correctly gathering $x$ s on one side of a correct equation with non $x$ terms on the other side
		$x = \frac{y^2 + 1}{y^2 - 2}$ oe	4	A1	
					Total 4 marks

Question	Working	Answer	Mark	Notes
18.	$(A =) 0.5 \times (4 + k) \times \sqrt{3} (= 5\sqrt{6})$ oe			M1 $4\sqrt{3} + 0.5(k-4) \times \sqrt{3}$ oe
	$k+4 = \frac{10\sqrt{6}}{\sqrt{3}}$			
	$(k =) 2 \times \frac{5\sqrt{6}}{\sqrt{3}} - 4 \text{ or } (k =) \frac{5\sqrt{6} - 2\sqrt{3}}{0.5\sqrt{3}} \text{ oe}$			M1 correctly isolating k
		$(k =) 10\sqrt{2} - 4$		A1 Accept $2(5\sqrt{2}-2)$ but don't accept $10\sqrt{2}-4$
			3	followed by $5\sqrt{2} - 2$
				Total 3 marks

Question	Working	Answer	Mark	Notes
19.	$2.85 \times 60 \div 4.5$ oe			M2 M1 for 4.5 or 2.85 selected or used. Accept 4.49
				or 2.849
		38		A1 38 must come from correct working, although 38 without
			3	working gets M2A1
				Total 3 marks

Question	Working	Answer		Mark	Notes	
<b>20.</b> (a)	$\frac{4}{9} \times \frac{3}{8} \left(=\frac{12}{72}\right)$				M1	
	9 8 72		$\frac{12}{72}$ or $\frac{1}{6}$ oe	2	A1	accept 0.167 or better
(b)	$\frac{2}{9} \times \frac{3}{8} \ (= \frac{6}{72}) \ \text{oe or} \ \frac{3}{9} \times \frac{2}{8} \ (= \frac{6}{72}) \ \text{o}$ $\text{or} \ \frac{2}{9} \times \frac{4}{8} \ (= \frac{8}{72}) \ \text{o}$	e or $\frac{4}{9} \times \frac{2}{8} (= \frac{8}{72})$ oe			M1	1 correct branch
	$\frac{2}{9} \times \frac{3}{8} + \frac{3}{9} \times \frac{2}{8} + \frac{4}{9} \times \frac{2}{8} + \frac{2}{9} \times \frac{4}{8}  (=\frac{2}{7})$	$(\frac{8}{2})$ oe			M1	4 correct branches with intention to add
			$\frac{7}{18}$ oe	3	A1	accept 0.389 or better.
	Alternative to (b) : with replace	ement			NB: U	Jse of this method can score all available M marks, but
		4 2 2	2 4 2		canno	ot score the Accuracy (A) mark.
	$\frac{2}{9} \times \frac{3}{9} \left(=\frac{6}{81}\right) \text{ oe or } \frac{3}{9} \times \frac{2}{9} \left(=\frac{6}{81}\right) \text{ oe or } \frac{4}{9} \times \frac{2}{9}  \left(=\frac{8}{81}\right) \text{ oe or } \frac{2}{9} \times \frac{4}{9}  \left(=\frac{8}{81}\right) \text{ oe }$					
	$\frac{2}{9} \times \frac{3}{9} + \frac{3}{9} \times \frac{2}{9} + \frac{4}{9} \times \frac{2}{9} + \frac{2}{9} \times \frac{4}{9}  (= \frac{2}{9})$	$\frac{10}{81}$ oe )			N/1	
					M1	
						Total 5 marks

Question	Working	Answer	Mark	Notes	
<b>21.</b> (a)		<u>3</u> 5	1	B1	$\frac{3}{5}$ or 0.6
(b)		(x = ) - 4	1	B1 a	accept $x \neq -4$
(c)		(a = ) 2	1	B1	
(d)	g(1) = 6			M1 -	$\frac{3}{4+5+1}$ or $\frac{3}{4+6}$ or 6 or f(6)
		$\frac{3}{10}$	2	A1 -	$\frac{3}{10}$ or 0.3
(e)	3			M1	
	$\overline{4+5+x}$	$\frac{3}{9+x}$	2	A1 c	cao
					Total 7 marks

Question	Working	Answer	Mark	Notes		
<b>22.</b> (a)	$\frac{8}{\sin 35} = \frac{BC}{\sin(180 - 65)} \text{ or } \frac{\sin 35}{8} = \frac{\sin(180 - 65)}{BC}$			M1	for correct substitution into the	Condone use of 65
	sin35 sin(180 - 65) 8 BC				sine rule	instead of 115
	$("BC" =) \frac{8sin"115"}{sin35}$ oe			M1	dep	
		12.6	3	A1	awrt 12.6	
(b)	0.5 x 8 x "12.6" sin (180 – 115 – 35) oe (= 25.28)			M1ft	0.5 x 8 x "12.6" sin (180 – 115 – 3	5) oe or 25.2 – 25.3
					"12.6" must be from clear final ans	wer from (a) to allow ft
	$65/360 \ge \pi \ge 8^2 (=36.30)$			M1	Accept $\frac{65}{360} \times 201$ or $\frac{104\pi}{9}$ oe or 30	6.3 (correct to the
					first 3 SF)	
	"25.28" + "36.30"			M1	dep on M2	
		61.6	4	A1	61.5 - 61.6	
						Total 7 marks

Question	Working	Answer	Mark	Notes
23.	$\frac{3(x-3)+4(x+2)}{(x+2)(x-3)} \text{ or } \frac{3(x-3)}{(x+2)(x-3)} + \frac{4(x+2)}{(x+2)(x-3)} (=2)$			M1 correct single fraction
	3(x-3) + 4(x+2) = 2(x+2)(x-3)			M1 correct removal of denominator to give a correct
	$7x - 1 = 2(x^2 - x - 6)$ oe			equation
	$2x^2 - 9x - 11 \ (= 0)$			A1 correct 3 part quadratic (eg $2x^2 - 9x - 11$ (= 0) or $2x^2 - 9x = 11$ or $2x^2 = 9x + 11$ oe)
	(2x-11)(x+1) (=0)			M1 for $(2x - 11)(x + 1)$ (=0) or
				a fully correct substitution into the quadratic formula
				$eg = \frac{-9 \pm \sqrt{(-9)^2 - 4 \times 2 \times -11}}{2 \times 2}$ condone no brackets around -9
				or $\frac{9 \pm \sqrt{169}}{4}$
		x = -1	5	A1 dep on last M1
		x = 5.5 oe		
				Total 5 marks

		TOTAL FOR PAPER: 100 MARKS

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